

INTERNATIONAL TELECOMMUNICATION UNION



Z.100 Annex F1

THE INTERNATIONAL TELEGRAPH AND TELEPHONE CONSULTATIVE COMMITTEE (11/1988)

ANNEX F1 TO RECOMMENDATION Z.100: SDL FORMAL DEFINITION INTRODUCTION

SDL FORMAL DEFINITION

Reedition of CCITT Recommendation Z.100, Annex F1 published in the Blue Book, Fascicle X.3 (1988)

NOTES

1 CCITT Recommendation Z.100, Annex F1 was published in Fascicle X.3 of the *Blue Book*. This file is an extract from the *Blue Book*. While the presentation and layout of the text might be slightly different from the *Blue Book* version, the contents of the file are identical to the *Blue Book* version and copyright conditions remain unchanged (see below).

2 In this Recommendation, the expression "Administration" is used for conciseness to indicate both a telecommunication administration and a recognized operating agency.

© ITU 1988, 2008

All rights reserved. No part of this publication may be reproduced, by any means whatsoever, without the prior written permission of ITU.

CONTENTS OF FASCICLE X.3 OF THE BLUE BOOK

Annex F1 to Recommendation Z.100

PRELIMINARY NOTES

1 The Questions entrusted to each Study Group for the Study Period 1989-1992 can be found in Contribution No. 1 to that Study Group.

2 In this Fascicle, the expression "Administration" is used for shortness to indicate both a telecommunication Administration and a recognized private operating agency.

Contents

1	Preface			1
2	Motivation			1
	2.1	The Me	ta Language	. 1
3	Mod	lelling T	echnique	2
	3.1	Static S	emantics	. 3
	3.2	The Dy	namic Semantics	. 3
	3.3	Exampl	e	. 5
	3.4	Physica	l Structure of The Formal Definition	. 5
4	How	v to Use	the Formal Definition	7
	4.1	The SD	L Users	. 7
	4.2	The Im	plementors	. 7
5	Intr	oductior	a to Meta-IV	7
	5.1	General	Structure	. 7
	5.2 Function Definitions			
	5.3	Variabl	e Definitions	. 9
	5.4	Domair	S	. 9
		5.4.1	Synonyms	. 10
		5.4.2	Unnamed Trees	. 11
		5.4.3	Branching Constructs	. 12
		5.4.4	Elementary domains	. 13
		5.4.5	Set Domains	. 15
		5.4.6	List Domains	. 17
		5.4.7	Map Domains	. 18
		5.4.8	Pid Domains	. 20
		5.4.9	Reference Domains	. 21
		5.4.10	Optional Domains	. 21
	5.5	The let	and .def Constructs	. 22
	5.7	Auxilia	ry Statements	. 24
	5.8	Deviati	ons from the notation used in the Formal Definition of CHILL	. 25
	5.9	Exampl	e: Demon game specified in Meta-IV	. 25

FASCICLE X.3

Annex F.1 to Recommendation Z.100

SDL FORMAL DEFINITION

1 Preface

This Formal definition of SDL provides a language definition which supplements the definition given in the recommendation text. This annex is for use by those who require a very precise and detailed definition of SDL such as maintainers of the SDL language and designers of SDL tools.

The formal definition consist of three volumes:

Annex F.1	(This volume)		
	Which states the motivation, describes the overall structure, provides guidelines for how to use the Formal Definition and describes the notation used.		
Annex F.2	Which defines the static properties of SDL		
Annex F.3	Which defines the dynamic properties of SDI,		

2 Motivation

Natural languages in general are ambiguous and incomplete, that is, more than one interpretation, can be given to some of the sentences in the language, no matter whether the reader is a computer or a human being.

A definition or specification is formal if its meaning (semantics) is unambiguous and complete. As natural languages cannot be used for that purpose, special languages, known as specification languages (like SDL and LOTOS) have been developed. An implementation language like CHILL or PASCAL could also be used as a specification language (for instance a compiler specifies formally the semantics of another language), but often it is essential to separate the implementation details, irrelevant for the understanding, from the semantics of a specification.

Formal languages specially suitable for defining languages are known as meta languages. For example, The Backus Naur form (BNF) is a meta language specially suitable for defining formally the syntax of programming languages.

In spite of the ambiguity of natural languages, natural languages are usually more readable for human beings than formal languages and can more easily express rationale giving a framework in which the formal specification can be understood. For these reasons both a definition in natural language and a definition in a formal specification language often are given.

This annex constitutes a formal definition of SDL. If any properties of an SDL concept defined in this document, contradicts the properties defined in Z.100 and the concept is consistently defined in Z.100, then the definition in Z.100 takes precedence and this formal definition requires correction.

2.1 The Meta Language

The meta language used in this Formal Definition is Meta-IV [1). The reasons for choosing this language are the following:

- It builds upon a very strong and extensively researched mathematical foundation.
- It has very convenient and powerful facilities for object manipulations.
- It has a "programming like" notation which means that it is oriented towards programmers and implementors.
- It is in the process of being standardised within the European Community.
- It is well reported in books, proceedings and scientific journals and it has been used in the CCITT manual The Formal Definition of CHILL [2]- which also contains a summary of the Meta-IV notation.
- Meta-IV tools are available which allow for syntax checking, visibility analysis, document generation, cross referencing etc.

In section 5, an informal introduction to the parts of Meta-IV used in the Formal Definition can be found. A complete definition of Meta-IV can be found in [1].

3 Modelling Technique

When considering what is meant by "semantics of SDL" it is convenient (conceptually) to decompose the language definition into several parts:

- The definition of the syntax rules.
- The definition of the static semantic rules (so-called well-formedness conditions) such as which names it is allowed to use at a given place, which kind of values it is allowed to assign to variables etc.
- The definition of the semantics of the constructs in the language when they are interpreted (the dynamic semantics).

There is no need for including the syntax rules in the Formal Definition as the BNF rules and Syntax diagrams found in Z.100 already serve as formal definitions of the syntax rules, which means that the input to the Formal Definition is a syntactically correct SAL specification. The input is represented by an Abstract Syntax. This abstract syntax is based on the SDL textual concrete syntax parse-tree (BNF rules) with irrelevant details such as separators and lexical rules removed. Therefore, this Abstract syntax is not the Abstract Syntax of Z.100 appearing in the recommendations which is an abstraction of the SDL model concept.

For example the Abstract Syntax production rule:

1 Transstring :: Actstmt+ [Termstmt]

expresses that a Transistion string consists of a non-empty list of Action statements and an optional Terminator statement (the italicised letters also occur in the production rule). The complete set of production rules (so-called Domain Definitions) defining the SDL-syntax on an abstract form is called AS_0 . In some respect it defines the language syntax on a more basic level than the syntax rules found in Z.100 since the concrete textual syntax in Z.100 contains a lot of semantic information (it is context sensitive) as opposed to AS_0 . It should be noted that AS_0 is an abstraction of the concrete textual syntax. The concrete graphical syntax has not been used for reasons of economy in time and space rather than any difficulty in the task.

As an example a signal list in Z.100 is defined to be:

```
<signal list> ::= <signal item> {,<signal item>}
<signal item> ::= <<u>signal</u> identifier> | (<<u>signal list</u> identifier>) | <<u>timer</u> identifier>
```

whereas the corresponding definitions in AS_o are:

² Signallist	:: Signalitem ⁺
3 Signalitem	= Id Signallistid

A *Signallist* consists of a list of Signaliterns. A Signalitem is either an identifier or a signal list identifier. As opposed to the context sensitive BNF production <signal item> no distinction is made between a signal identifier and a timer identifier in ASo because syntactically they are both identifiers as opposed to signal lists which are distinguished by the use of parenthesis.

The starting point for the FD is syntactically correct SDL-specifications. The tasks of the Formal Definition are to

- Define the well-formedness conditions for SDL-specifications. This task, referred to as the Static Semantics, constitutes Annex F.2
- Define the dynamic properties for SDL-specifications. This task, referred to as the Dynamic Semantics, constitutes Annex F.3

The steps are shown in figure 1. The result from the Static Semantics (i.e. AS_1) is explained below.



Figure 1: Objectives of Static Semantics and Dynamic Semantics

The step of translating from the concrete textual syntax to AS_0 is not formally defined, but is derived from the correspondance between names in the two syntaxes as previously illustrated for Signallist.

3.1 Static Semantics

In Z.100, the dynamic semantics of the various constructs are defined in terms of an Abstract Syntax.. Common subsections, Concrete textual grammar and Concrete graphical grammar define the concrete syntax rules, state the appropriate well-formedness conditions and relate the concrete syntax rules to the abstract syntax in 2.100. It is defined using Meta-W (in the common subsections Abstract grammar). The same abstract syntax is used in the Formal Definition (where it is referred to as AS_1). A summary of this abstract syntax can be found in Annex B of Z.100.

In addition to defining the well-formedness conditions, the Static Semantics must therefore define how the AS_0 representation of a specification is transformed into the AS_1 representation, that is, given an AS_0 representation, an AS_1 representation is returned by the Static Semantics if the AS_0 representation was well-formed. The Static Semantics can be regarded as an "abstract cortnpiler" where the AS_0 representation is the source language and the AS_1 representation is the object language.

In addition to AS_0 and AS_1 , the Static Semantics uses some internal utility domains, known as the Semantic Domains, which hold the information required at any place about a given entity. For example, when a process definition is transformed, information about its formal parameters is kept in the Semantic Domains and the information is retrieved during trans-formation of the Create Request action. The AS_0 domains could have been used for that purpose, as the Semantic Domains anyway are deduced from AS_0 , but a tree representation is not useful when information of a certain entity (say a process definition) occurring some-where in the tree is required. Therefore Semantic Domains are usually mappings modelling tables.

For instance, the Semantic Domains include a mapping (further explained in section 5.4.7) of identifiers into some descriptor containing information about the identifiers:

4 Descriptordict = Qual \equiv Descr

where Qual is the identifier representation used internally in the Formal Definition and Descr is any descriptor. The descriptor may for instance be a process descriptor;

5	Descr		ProcessD
6	ProcessD	::	ParameterD* Validinputset Outputset

expressing that a Process Descriptor contains a list of Parameter Descriptors, information about the Valid input signal set and information about the Output signals. The definitions of these three (sub)descriptors are not shown here.

The transformation itself is performed by a set of Meta-IV functions using the three Domains AS_0 , AS_1 and the Semantic Domains.

3.2 The Dynamic Semantics

The task of the Dynamic Semantics is to define the behaviour of an SDL specification on AS₁ form.

The Dynamic Semantics is divided into three major sections:

- The Model for the underlying system (the abstract SDL-machine)
- The Interpretation of the process graphs
- Transformation of AS_1 into a more appropriate representation; that is, a mapping is constructed (a Semantic Domain) which contains the information required during the interpretation such as information about the sort of variable, possible communication paths between processes, equivalence classes for types etc. The mapping is named Entity-diet (or more correctly, the domain of the mapping is named Entity-diet).

Concurrency in SDL in the Dynamic Semantics is modelled by using Meta-processes; that is concurrently executing Meta-processes in Meta-IV model concurrently executing processes in SDL.

Six different Meta-process types are used:

• system

To handle the signal routing and the creation of sdl-processes.

• path

To handle the non-deterministic delay of channels.

• timer

To keep track of the current time and handle time-outs.

• view

To keep track of all revealed variables.

• sdl-process

To interpret the behaviour of an SDL-process.

• input-port

Which handles the queueing of signals in an SDL-process. For each instance of sdlprocess there exists exactly one instance of input-port

The four Meta-process types system, path, timer and view can, as a whole, be regarded as modelling the underlying system.

There is no shared data between Meta-processes - they interact by transmitting values conveyed by instances (objects) of Communication Domains (correspond to the SDL concept signals).

Communication Domains are defined in the same way as other domains; for example, objects of the Communication Domain Input-Signal are directed to an sdl-process instance from its attached input-port instance. The Communication Domain is defined like this:

7 Input-Signal :: Signal-Identifier₁ [Value]* Sender-Value

Instances of Input-Signal convey the identifier of the SDL signal which is sent, the list of values conveyed by the SDL signal and the PID value of the sender.

Figure 2 shows the complete "Meta-process interaction scheme". The communication mechanism is synchronous and the notation is known as CSP (see [3] and [4]) (Communicating Sequential Processes).



Figure 2: Communication scheme

3.3 Example

Figure 3 shows the communication between meta-processes in the formal definition for the following (partial) SDL-process, when a signal ("b") arrives from the environment, and the process responds by sending a signal ("a") back to the environment:

•••

- state S;
- input b;
- output a;

•••

The communication is informally illustrated by means of a message sequence chart. Path(1) and Path(2) denotes two instances of the path-processor, corresponding to the path from the environment to the sdl-process (Path(1)) and vice versa (Path(2)).



Figure 3: Example of communication between meta-processes

3.4 Physical Structure of The Formal Definition

The Static Semantics (Annex F.2) is divided into three main parts:

- 1. The Domain definitions for AS_0
- 2. The Domain definitions for the Semantic Domains
- 3. The Meta-IV functions checking well-formedness conditions and defining how AS_0 is transformed into AS_1 .

The Domain definitions for AS_1 which are used in part 2 and 3 are to be found in Z.100 and summarized in Annex B of Z.100. They are not repeated in the formal definition. Annex F.2 also includes cross-indices on Meta-IV function names and domain names (both defining occurrence and applied occurrences) and a cross index on the well-formedness conditions applied.

The Dynamic Semantics (Annex F.3) is divided into five major sections:

- 1. Domain definitions for the Communication Domains
- 2. Domain definitions for the Semantic Domains (Entity-diet)
- 3. The Meta-process definitions and attached functions for the model of the underlying system
- 4. The Meta-process definitions and attached functions for the interpretation of the SDL-process
- 5. The creation of the internal, domain Entity-diet. Entity-diet is used by the SDL-processes and it is therefore created before any SDL-processes are interpreted.
- 6 Fascicle X.3 Rec. 2.100 -. Annex F.1

Annex F.3, like Annex F.2 also contains a number of indices covering domain names, function names, Meta-process names, error conditions etc.

The volume of material (especially in Annex F.2) might seem frightening at a first glance. However, more than half of the space contains annotations for the Domains, function and process definitions.

The layout for a function and process definition follows a scheme:

1. First, the function or process definition is specified, by:

(a) heading defining the process or function name and the names of its formal parameters

- (b) its body (algorithm)
- (c) a type clause specifying the type (domain) of the formal parameters and the type of the result (if any).

,,

2. Then follows the itemized (plain english) annotations attached to the process or function definition:

Objective	Explains the purpose of the function or process
Parameters	Explains the purpose of every formal parameter to the function or process
Result	Explains the object returned (if any).
Algorithm	Explains, on a line by line base, the algorithm used in the function or process.

Example

The outermost function definition-of-SDL from Annex F.2 which ties together the Static Semantics (transform-system) and the Dynamic Semantics (by starting the Meta-process system) is as follows:

definition of $-SDL(extparms, systemdef, predefsorts) \triangleq$

```
1 (let (as_1, auxinf) = transform-system(systemdef, predefsorts, extparms) in
```

```
2 if as_1 = nil then
```

- 3 undefined
- 4 else
- 5 (let subsetcut = select-consistent-subset(as1, extparms) in
- 6 start system(as₁, subsetcut, auxinf)))

type: External-Information Sys₀ Datadef₀⁺ \Rightarrow

Objective Define the properties of SDL

Parameters

extparms	Some External-Information (see annex F.2 section 2.3).
systemdef	The AS_0 -tree representing the SDL system
predefsorts	The predefined data in AS_0 form.

Algorithm

Line 1	Transform the system into the abstract syntax form $(AS_1 \text{ form})$.	
Line 2	If static errors are found (i.e. if no AS_1 representation could be derived) then the behavior is not defined.	
Line 4	If no static errors are found then	
Line 5	Select the set of Block-identifaerls denoting the consistent subset.	
Line 6	Create a system instance, i.e. create a Meta-IV process which behaves like the underlying system.	

4 How to Use the Formal Definition

4.1 The SDL Users

The Formal Definition is not intended as a users reference manual on SDL. Newcomers on SDL may find the User Guidelines (annex D in Z.100) appropriate for achieving an overview of concepts (and their rationale) in the language, while the Z.100 Recommendation itself serves as a reference manual on SDL, but there might be some cases where Z.100 is inadequate. For instance

- if some properties are missing (e.g. some expected static condition), if some stated properties contradict other properties or
- if the exact meaning of some stated properties is difficult to understand or
- if some properties (due to the lack of cross index in Z.100) are difficult to find or
- if the user wants to achieve a deeper understanding of more complex matters like the abstract SDL machine, when and how to select a consistent subset, resolution by context, the inheritance mechanism etc.

In such cases the Formal Definition might be a useful supporting document. The user must of course first gain insight in the structure of the Formal Definition, how the functions are organized and what the Domains are used for. A certain amount of knowledge about the Meta-IV notation is also required, but as the functions are extensively annotated, it may be possible to read Meta-IV by reading the functions in conjunction with the annotations after having read the introduction on Meta-IV (section 5 below). When looking up in the Formal Definition, the users may take advantage of using the table of contents and the cross indices.

4.2 The Implementors

As mentioned earlier, the Meta-IV approach allows implementors to derive an implementation systematically (i.e. static analyzer, simulator etc.) from the Meta-IV specification. For SDL, it is possible to derive a static analyzer from Annex F.2 and a simulator from Annex F.3. It is advised to use the AS_1 representation (generated by the static analyzer) as a basis for simulation. The reasons are that context information for identifiers is missing in AS_0 (they are normally not qualified in AS_0) and that the dynamic semantics of a specification on ASo form may be difficult to derive due to the large number of shorthands in SDL (especially for concepts like data types).

It should be noted that the derivation into an implementation is systematical, but it is not mechanical.

The following points must be considered:

- Appropriate datatypes must be found for representing the ideal data types (domains) in Meta-IV such as mappings, lists and sets used in AS_0 , AS_1 and the Semantic Domains.
- Due to the visibility rules in SDL (the fact that identifiers may be used before they are defined) a so-called "fixpoint equation" is (for convenience) used in the Static Semantics (see section 3.1 of Annex F.2). In an implementation, the Semantic Domains may be created gradually by going through the ASo tree a number of times (e.g. descriptors for signals must be created before any descriptors for channels are created as channels refers to signals in their definitions).
- The initial algebra approach implies that the Formal Definition manipulates infinite objects. Also AS_1 contains infinitely objects. It is therefore necessary to modify AS_1 slightly and to impose restrictions on the use of data types or to use some abstraction technique in which these objects can be encoded.

5 Introduction to Meta-IV

This section contains an informal introduction to Meta-IV and to how Meta-IV has been used in the Formal Definition, i.e. Meta-IV is explained in terms of the Formal Definition (abbreviated as FD) which means that only those parts of Meta-IV which have been used in the FD are explained.

5.1 General Structure

The FD consists of:

A set of function and process definitions defining the semantics of SDL. Processes (in Meta-IV and in the FD called processors) are used for modelling concurrency and are therefore only used in the Dynamic Semantics. Syntactically, processor definitions look like function definitions (except for the keyword processor following the processor name), therefore, the following description of the function concept also applies for processors.

7

- A set of domain definitions which define the type of the objects manipulated with by the functions. Terms denoting certain groups of domain definitions are introduced in order to classify them logically. We have the AS₀ domains denoting the representation of the concrete syntax, the ASI domains denoting the abstract syntax of SDL and the sets of domains Diet and Entity-did denoting the "internal" utility domains (semantic domains) of the Static- and Dynamic Semantics respectively. In this section, we will often use "value" as a synonym for object and "type" as a synonym for domain.
- A set of global constant definitions. In the FD, only two such definitions are present. They are defined in section 3.13 of the Static Semantics. They are not essential for understanding the FD.

Definitions may be specified in any order and names introduced in definitions may be used before they textually are defined.

5.2 Function Definitions

A function definition consists of three parts:

- 1. The heading starts with the function name and is followed by one or two formal parameter lists. Each formal parameter list is enclosed in parenthesis. There is no formal significance in dividing the parameters between two lists. Often some parameters are put into a separate (second) parameter list if they are of secondary importance for the evaluation. For instance in the case of the semantic domains which often are used by the functions and supplied in a separate parameter list.
- 2. The body of the function which can either be an expression or a sequence of statements. A function does not have to deliver any result (see below).
- 3. The type clause specifying the type of the formal parameters and the type of the result. First, the type of the first parameter list is specified, then the type of the second parameter list (if any) separated by the first parameter list by an arrow (\rightarrow or \Rightarrow), then another arrow and then the result.

Example

$f(a,b)(d) \triangleq$

1 /* expression */

type: $Dom X \ Dom Y \rightarrow Dom Z \rightarrow Dom W$

f is the name of the function

a, b, d are formal parameters. a and b are contained in the first formal parameter list and d is contained in the second parameter list. The type of a is DomX, the type of b is DomY and the type of d is DomZ. The type of the result is Dom W. The domains DomX, Dom Y, DomZ and DomW must be defined in some domain definitions.

If the formal parameters or the result are not used in accordance with the type clause, there is an error in the Meta-IV specification. In the example above informal Meta-IV text (the text enclosed in /* */) is used to denote some Meta-IV expression which for reasons of economy in space has been left out. Informal Meta-IV text is similar to informal text in SDL and it is extensively used in the examples of this section.

Normally, a distinction is made between applicative and imperative functions. Applicative functions are functions which do not refer to parts of the global state (variables), that is, the result of such functions are only depending on the value of the applied actual parameters. The body of an applicative function is restricted to be an expression as statements impose some change of state. Applicative functions must always deliver a result. Imperative functions are functions which refer to or even change- the global state (functions with side effects). If a function is imperative, it must be reflected in the type clause by using \Rightarrow instead of \rightarrow when specifying the result.

That is:

$f(a,b)(d) \triangleq$

1 /* expression referring to the global state or sequence of statements */

type: $Dom X Dom Y \rightarrow Dom Z \Rightarrow Dom W$

In the FD, the Static Semantics and the creation of the internal Domain Entity-diet in the Dynamic Semantics are applicative.

5.3 Variable Definitions

Global variables are defined at the outermost level in processor definitions. They are visible to all functions used by the processor defining the variable even though the functions normally are defined outside processor definitions. However, a function which is shared by two or more processors is not allowed to access variables. When several instances of a given processor exist, several instances of variables defined by the processor also exist. (There are no shared variables).

Variable definitions are introduced by specifying the keyword dcl followed by a list of variable names, optionally followed by an initial expression and ending with the type of the variable.

Example

dcl vi := 5 type Intg; dcl v2 type DomD;

Here we have defined two variables v1 and v2, vl is of type integer and is initialized to 5. v2 is of type DomD. Note that variables can always be distinguished syntactically from other names since they are not italicised. An alternative syntax of variable definitions is:

dcl vl := 5 type *Intg*, v2 type *DomD*;

The value associated to variables is accessed by using, the contents operator which is the keyword c.

Example

 $f() \stackrel{\triangle}{=} \\ 1 \quad cv1 + cv2 \\ type: \quad () \Rightarrow Intg$

5.4 Domains

Domains are usually defined in the beginning of a document. Domain names can be distinguished syntactically from other names since the first letter is in capital. A. domain is defined by specifying the domain name followed by a "::" symbol (or by a "=" in the case of a synonym name as explained in section 5.4.1) and then followed by a domain expression reflecting its properties (for an introduction to the domain notation see also §1.5.1 of Z.100).

Example

8	Output-node1	:: Signal-identifier ₁
		$[Expression_1]^*$
	-	$[Signal-destination_1]$
		$Direct-via_1$

This example is taken from the abstract syntax of SDL (for clarity, all the names of AS_1 are suffixed by a "₁" in the FD). It defines a named tree, that is, a record-like datatype where the name of the record type is *Output-node*₁ and it's fields are of the type *Signal-identifier*₁, [*Expressions*₁]*, [*Signal-destinations*₁] and *Direct-via*₁.

The most important operator for named trees is the mk- (make) operator which is used for composing and decomposing tree objects (i.e. record values).

For example, if a name sigid denotes an object of domain *Signal-identifier*₁, a name exprlist denotes an object of domain $[Expressions_1]^*$, a name dest denotes an object of type $[Signal-destination_1]$ and a name via denotes an object of domain *Direct-via*₁ then an object of domain *Output-node*₁ is constructed by writing:

mk-Output-node1 (sigid, exprlist, deal, via)

which can be used in Meta-IV expressions. Note that the order in which the arguments are specified in the mk- operator is significant. This applies for function calls as well. Similarly, if we have an object, named *outputnode*; of domain *Output-node*₁ and we want to access the fields, we can introduce names for the fields by decomposing it (the same names as above are chosen here):

let mk-Output-node1(sigid, exprlist, dest, via) = outputnode in
/* some expression using the fields */

By means of the let construct we have introduced names to denote the fields in the object *outputnode*. Using the let construct is the general way of introducing names for objects (not only in combination with the mk- operator). The let construct is explained further in section 5.5

9

If some of the fields are not used in the expression we can omit the corresponding names in the decomposition. For instance, if sigid is not used in the expression, we can write:

let mk-Output-node1 (, exprlist, dest, via) = outputnode in
/* some expression using exprlist and dest */

If we only want to use the Signal-Identifier₁ in the expression we can alternatively use the field select operator s-:

let sigid s-Signal-Identifier1 (outputnode) in
/* some expression using sigid */

The field select operator can only be used if the field can be uniquely determined by mentioning the domain name.

We can choose to decompose (i.e. introduce names for the contained elements) the formal parameters in the function head instead of in the body if we find it more readable. That is

 $int-create-node(mk-Create-request-node_1(pid, exprl))(dict) \triangleq$

- 1 /* body of int-create-node */
- type: Create-request-node₁ \rightarrow Entity-dict \Rightarrow

is equivalent to

int-create-node(createnode)(dict) \triangleq

- 1 (let mk-Create-request-node1 (pid, exprl) = createnode in
- 2 /* body of int-create-node */)

type: Create-request-node₁ \rightarrow Entity-dict \Rightarrow

Note that in this example we also have a second parameter list containing the formal parameter diet of the domain Entity-diet.

5.4.1 Synonyms

Using the field select operator is only possible if the field in the domain definition is rep-resented by a name. If for instance we want to use the select operator on the second field of objects of the domain Output-node₁, we must define Output-node₁ in a slightly different way:

9	$Output-node_1$:: Signal-identifier ₁
		Valuelist
		$[Signal-destination_1]$
		Direct-Via ₁
10	Valuelist	$= [Expression_1]^*$

This *Output-node*₁ is exactly the same domain as the *Output-node*₁ previously defined. The only difference is that we have given the second field a name i.e. we have defined a synonym or shorthand for the domain expression $[Expressions]^*$ (the "=" symbol is used when defining synonyms). Often there are other reasons for defining synonyms such as if the same domain expression is used at several places or for the sake of readability. For instance, in the abstract syntax of SDL, we have *Channel-name*₁, *Block-name*₁, *Process-name*₁ etc. which all are synonyms for the domain Names, but which carries information to the reader about the objects represented by the various Name's being of certain entity classes. Another typical case is where we have a long list of alternatives. For instance, the abstract syntax for Expression₁ is

11	Expression ₁	= Ground-expression ₁	
		$Active-expression_1$	
12	$Active-expression_1$	$= Variable - access_1$	
		Conditional -expression	41
		$Operator$ - $application_1$	
		$Imperative-operator_1$	
13	$Imperative-operator_1$	$= Now-expression_1$	
		Pid-expression ₁	
		View-expression ₁	
		Timer-active-expression	n_1

which better reflects the grouping of the various kinds of expressions than

14 Expression ₁	= Ground-expression ₁
	Variable-access1
	Conditional-expression ₁
	Operator-application ₁
	Now-expression ₁
	Pid-expression1
	View-expression ₁
	$Timer-active-expression_1$

5.4.2 Unnamed Trees

In some cases, we don't need to name a tree definition. Unnamed trees are extensively used in the FD, but they are anonymous since they often don't have to be defined explicitly.

Example

The first line in the definition of Entity-dict in the Dynamic Semantics is:

15 Entity-dict = (Identifier₁ Entityclass) \Rightarrow Entitydescr

which expresses that the *Entity-diet* includes a mapping from the two domains *Identifier*₁ and Entityclass into some descriptor (Entitydescr). These two domains constitute an unnamed tree. If a named tree should be used, we would have to rewrite the definition into:

16	Entity-dict	=	Pair ⇒Entitydescr
17	Pair	::	Identifier ₁ Entityclass

Example

Reachability in the dynamic semantics is defined as

18	Reachability	= (Process-identifier ₁ ENVIRONMENT)
		Signal-identifier ₁ -set Path

Here we have defined a synonym for an unnamed tree containing three fields:

- 1. A field which can contain either a process identifier or the quotation literal ENVIRONMENT
- 2. A field which contains a set of signal identifiers
- 3. A field of the domain Path

As shown, parenthesis are in the domain definitions both used for defining unnamed trees and for grouping alternatives.

Example

The function make-formal-parameters in the Dynamic Semanticsis defined as:

make-formal-parameters(parml, level) \triangleq

1 /* The body, which is not shown here */

type: Procedure-formal-parameter $_1^*$ Qualifier $_1 \rightarrow$ Formparm D^* Entity-dict

This function returns two *objects- FormparmD** and Entity-diet which means that it in fact returns an unnamed tree consisting of two objects.

The mk- operator cannot be used on unnamed trees. Composition and decomposition of these is obtained by enclosing the fields in parenthesis.

Example

composition of a Reachability object where a denotes a *Process-Identifier*₁, b denotes a signal identifier set and d denotes a Path:

(a, b, d)

if, for the sake of readability, we want to denote the object by a name (it is easier to deal with a name than with (a,b,d), especially if (a,b,d) is used several times in an expression) then we can again use the let construct, that is, the expression:

/* some expression using "(a,b,d)" */

is equivalent to

(let reach = (a, b, d) in
/* some expression using "reach" */)

The let construct is also used for decomposing objects of unnamed trees. For example a decomposition of a Reachability object named reach where we for some reason don't use the signal identifier set is:

let (a, , d) = reach in
/* some expression using a and d */

When we call a function, it is usual to decompose unnamed trees which are the result of the function call i.e.:

let (*parmlist*, *pathlist*) = *make-formal-parameters* (...,..) **in** /* some expression using the function results parmlist and pathlist */

is equivalent to:

let parminf = make-formal-parameters (...,..) in
let (parmlist, pathlist) = parminf in
/* some expression using the function results parmlist and pathlist */

5.4.3 Branching Constructs

In some cases, it must be possible to distinguish a number of tree objects from each other. For instance, objects of the Imperative-operators synonym previously defined is either a *Now-expression*₁, a *Pid-expression*₁, a *View-expression*₁ etc. With an Imperative-operators in hand, we must first determine the type of the Imperative-operators before we can evaluate it. For that purpose, we can use the case expression/statement. For instance, the function which evaluates the imperative SDL expressions could look like:

```
eval-imperative-expression(expr) \triangleq
```

```
    cases expr:
    (mk-Now-expression<sub>1</sub>()
    → eval-now-expression(),
    mk-View-expression<sub>1</sub>(vid, pidexpr)
    → eval-view-expression(vid, pidexpr),
    mk-Timer-active-expression<sub>1</sub>(tid, actlist)
    → eval-timer-expression<sub>1</sub>(tid, actlist).
```

8 $\mathbf{T} \rightarrow eval-pid-expression(expr))$

```
type: Imperative-operator<sub>1</sub> \Rightarrow
```

Note that we branch on the type of the *Imperative-operator*- not on the actual value of the fields in the tree. **T** denotes an "otherwise" clause which is used here because the final alternative in *Imperative-operator*₁ (*Pid-expression*₁) is a synonym representing four other alternatives which we don't want to distinguish here. The evaluation of these alternatives is deferred to *eval-pid-expression*.

Another way of doing it is by using the boolean operator is- which returns true if the object given as argument is of a certain domain, e.g.

```
eval-imperative-expression(expr) \triangleq
```

```
if is-Now-expression<sub>1</sub>(expr) then
1
2
      eval-now-expression()
3
      else
      if is-View-expression1(expr) then
4
         eval-view-expression(s-Variable-identifier1(expr), s-Expression1(expr))
5
6
        else
         if is-Timer-active-expression<sub>1</sub>(expr) then
7
           (let mk-Timer-active-expression1(tid, actlist) = expr in
8
            eval-timer-expression(tid, actlist))
9
10
           else
           eval-pid-expression(expr)
11
```

type: Imperative-operator₁ \Rightarrow

Note that both access to the fields by decomposition (line 8) and access to the fields by means of the field selection operator (line 5) are illustrated here.

As in most other programming- and specification languages, it is required that the alternatives in the case expression/statement are "constant" (as they are when we branch on the tree type) which means that if the alternatives are of a dynamic nature (say variables or formal parameters) the if-then-else construct must be used. However, there is another notation for the if-then-else construct, the so-called Mc-Carthy construct which is more convenient if there are many alternatives:

$eval-imperative-expression(expr) \triangleq$

```
(is-Now-expression1(expr)
1
2
        \rightarrow eval-now-expression(),
3
     is-View-expression_1(expr)
        \rightarrow (let mk-View-expression<sub>1</sub>(vid, pidexpr) = expr in
4
             eval-view-expression(vid, pidexpr)),
5
6
     is-Timer-expression<sub>1</sub>(expr)
        \rightarrow (let mk-Timer-expression<sub>1</sub>(tid, actlist) = expr in
7
             eval-timer-expression(tid, actlist)),
8
      T \rightarrow eval-pid-expression(expr))
9
```

type : Imperative-operator $_1 \Rightarrow$

Note that, some FD function names also start with "is-". These cases can easily be distinguished from the "is-" operator since they are not in boldface.

5.4.4 Elementary domains

Meta-IV provides a number of predefined elementary domains. Their notation and the associated operators are described in the following.

5.4.4.1 Boolean

The Meta-IV name Bool denotes the domain of truth values, i.e. the set {true,false} Operators for Boolean:

Notation	type			operation
-	Bool	\rightarrow	Bool	negate
^	Bool	\rightarrow	Bool	and
\vee	Bool	>	Bool	OI
С	Bool	\rightarrow	Bool	imply
=	Bool Bool	>	Bool	equal
_ /	Bool Bool	\rightarrow	Bool	different

Example

In terms of Meta-IV expressions, the properties of the *Bool* operators \neg , \land , \lor and \supset can be illustrated as follows:

 $\neg a = (\text{if } a \text{ then false else true})$ $a \lor b = (\text{if } a \text{ then true else } b)$ $a \land b = (\text{if } a \text{ then } b \text{ else false})$ $a \supset b = (\text{if } a \text{ then } b \text{ else true})$

5.4.4.2 Integer

Three domain names are predefined for the integer values:

- The name *Intg* denotes the domain of all integer values, i.e. the set {... -2,-1,0,1,2,...}
- The name N_0 denotes the domain of non-negative integer values, i.e. the set $\{0,1,2,...\}$
- The name N_1 denotes the domain of positive integer values, i.e. the set $\{1,2,...\}$

Operators for Integer:

Notation	type			operation
—	Intg	\rightarrow	Intg	negate
	Intg Intg	\rightarrow	Intg	subtract
+	Intg Intg	>	Intg	add
*	Intg Intg	\rightarrow	Intg	multiply
1	Intg Intg	\rightarrow	Intg	integer divide
mod	$N_0 N_1$	\rightarrow	N_0	modulus
=	Intg Intg	\rightarrow	Bool	equal
≠	Intg Intg	\rightarrow	Bool	different
<	Intg Intg	\rightarrow	Bool	less than
$ \leq$	Intg Intg	>	Bool	less than or equal
>	Intg Intg	\rightarrow	Bool	greater than
\geq	Intg Intg	\rightarrow	Bool	greater than or equal

5.4.4.3 Character

The Meta-IV name Char denotes the domain of ASCII character values. For the printable characters, there exist object representations which are enclosed in quotation marks, e.g. "a", "Z", " ".

Operators for Character:

Notation	type	operation
=	Char Char \rightarrow Bool	equal
≠	Char Char \rightarrow Bool	different
<	Char Char \rightarrow Bool	less than
≤	Char Char \rightarrow Bool	less than or equal
>	Char Char \rightarrow Bool	greater than
<u> </u>	Char Char \rightarrow Bool	greater than or equal

The relational operators are applied on the associated ASCII numerical values.

For the sake of readability, objects of the domain $Char^+$ may be represented by a sequence of characters enclosed in quotation marks e.g "abc" is the same as ("a","b","c") (see section 5.4.6)

5.4.4.4 Quotation

The Meta-IV name *Quot* denotes the domain of quotations. They are distinct elementary objects and they are represented as any bold-face sequence of uppercase letters and digits e.q. **ENVIRONMENT**, **REVERSE**.

Operators for Quotations:

Notation	type	operation
=	$Quot \ Quot \rightarrow Bool$	equal
_≠	$Quot \ Quot \rightarrow Bool$	different

As opposed to other domains, objects of Quot may occur in domain definitions when only certain object(s) of Quot are possible in the given context, for example, in the abstract syntax of Z.100, Originating-blocks is defined to be

1 $Originating-block_1 = Block-identifier_1 | ENVIRONMENT$

alternatively, Originating-blocky could have been defined using Quot:

2 $Originating-block_1$ = $Block-identifier_1 | Quot$

however, using ENVIRONMENT in the domain definition is more precise, since this object is the only Quot value possible in that context.

54.4.5 Token

The Meta-IV name Token denotes the domain of tokens. This domain can be considered as consisting of a potentially infinite set of distinct elementary objects for which no representations are required.

Operators for Tokens:

Notation	type	operation
=	Token Token \rightarrow Bool	equal
_ /	Token Token \rightarrow Bool	different

Example

 $Name_1$ in the abstract syntax of Z.100 is defined to be

1 $Name_1$

:: Token

The only property needed for Name's during interpretation is equality. A *Name*₁ therefore consist of a Token value (the actual spelling of names is irrelevant).

5.4.4.6 Ellipsis

The Ellipsis domain (represented by ...) denotes an unspecified construct. It is used in domain definitions or in expressions

- whenever the actual domain or expression is of no importance for the semantics or
- whenever the elaboration of the domain or expression is outside the scope of the specification.

Example

Informal-text₁ in the abstract syntax of Z.100 is defined to be

Informal-text₁ :: ...

Informal-text₁ cannot be interpreted using Meta-IV. Informal-text₁ therefore contains some further unspecified object.

5.4.5 Set Domains

1

A set domain is constructed by postfixing the element domain by the keyword -set (the dash is significant). For example

2	$State-node_1$:: $State-name_1$
		$Save-signalset_1$
		Input-node ₁ -set
3	Save-signalset	:: Signal-Identifier ₁ -set

expresses that objects of the domain $State-node_1$ consist of a state name, a save signalset, which contains a set of signal identifiers, and a set of Input-nodes. Set values can be constructed by using an explicit set constructor which is an expression list enclosed by braces, i.e.

{1,3,5,1}

denotes an object of the domain *Intg-set* and it contains the three Intg values 1,3,5. A more usual form is the so-called implicit set constructor where the set includes all those elements which satisfy a certain condition (predicate). For example

$\{i \in Intg \mid 0 \le i \le 5 \lor i \mod 2 = 0\}$

defines the set

 $\{0, 1, 2, 3, 4, 5, 6, 8, 10, 12, 14, 16, ...\}$

It reads: The set of those values on the left hand side of the vertical bar (possibly qualified by a value or by a domain) for which the expression on the right hand side of the vertical bar holds.

The empty set is denoted by { }.

In the following explanation of the semantics of the operators on sets, s denotes the set {1,3,5}:

E	Membership operator. Test whether a given element of the element domain is contained in a set, that is, $1 \in s \equiv$ true and $2 \in s \equiv$ false.
¢	Test whether a given element of the element domain is excluded in a set, that is, $1 \notin s \equiv$ false and $2 \notin s \equiv$ true.
U P	Union operator. Join two sets, that is, $\{2,3\} \cup s \equiv \{1,2,3,5\}$ and $s \cup s \equiv s$.
\cap	Intersection operator. Return the intersection of two sets, that is, $\{2,3\} \cap s \equiv \{3\}$ and $\{\} \cap s \equiv \{\}$.
λ	Complement operator. Exclude a given set of values from a set, that is, $s \setminus \{1,2\} \equiv \{3,5\}$ and $\{1,2\} \setminus s \equiv \{2\}$.
Ç	Proper subset operator. Test whether the elements of a given set are contained in a set, that is, $\{1,5\} \subseteq s \equiv \text{true}, s \subseteq \{1,5\} \equiv \text{false and } s \subseteq s \equiv \text{false}.$
С	Subset operator. Test whether the elements of a given set are contained in or equal to a set, that is, $\{1,5\} \subset s \equiv \text{true}, s \subset \{1,5\} \equiv \text{false and } s \subset s \equiv \text{true}.$
card	Cardinality operator. Return the number of elements in a set, that is, card $s \equiv 3$ and card $\{\} \equiv 0$.
union	Distributed union operator. The argument is a set of sets and the result is the union of all the sets contained in the argument, that is, union $\{s,\{5,6\},\{1,5,8\}\} \equiv s \cup \{5,6\} \cup \{1,5,8\} \equiv \{1,3,5,6,8\}.$
=,≠	Test for equality and inequality of sets.

Example

In terms of Meta-IV expressions, the properties of the set operators $\notin \cup, \cap, \subseteq, \subset$, card and union can be illustrated as follows:

```
\begin{array}{l} element \notin s1 = (\neg(element \in s1))\\ s1 \cup s2 = \{element \mid element \in s1 \lor element \in s2\}\\ s1 \cap s2 = \{element \mid element \in s1 \land element \in s2\}\\ s1 \cap s2 = \{element \mid element \in s1 \land element \notin s2\}\\ s1 \subseteq s2 = (\forall element \in s1)(element \in s2) \land s1 \neq s2\\ s1 \subseteq s2 = (\forall element \in s1)(element \in s2) \land s1 \neq s2\\ s1 \subseteq s2 = (\forall element \in s1)(element \in s2)\\ card s1 = (if s1 = \{\}\\ then 0\\ else (let element \in s1 in\\ 1 + card (s1 \setminus \{element\})))\\ union s1 \equiv \{element \mid (\exists set \in s1)(element \in set)\}\\ \end{array}
```

The quantifiers (\forall and \exists) are explained in section 5.6

5.4.6 List Domains

A list or tuple domain is constructed by postfixing the element domain by a "*" in the case of a possibly empty list and otherwise by a "+"

Example

```
4 Signal-definition<sub>1</sub>
```

:: Signal-name₁ Sort-reference-identifier₁*

This domain definition expresses that a signal definition consists of a signal name and a possibly empty list of sort identifiers.

A list value can be constructed by using an explicit tuple constructor. This is an expression list enclosed in angular brackets, i.e.

(11, 12, 13, 14)

denotes an object of the domain $Intg^+$ (or $Intg^*$) and it contains 5 ordered elements.

The empty list is denoted by $\langle \rangle$.

There are also implicit list constructors similar to those for sets. For instance, in the function int-output-node in the Dynamic Semantic we construct a tuple (*vall*) which contains the values of all the actual parameters (*exprl*) in an output node:

```
let vall = (eval-expression(exprl[i])(dict) | 1 \le i \le len exprl) in
```

which corresponds to an explicit enumeration of all the elements in the list:

```
let vall = \le verile val - expression( exprl[1])(dict),
      eval - expression( exprl [21)(did),
      eval - expression (exprl[3])(dict ),
      ....\ in
```

Note that the tuple brackets (\langle and \rangle) have a different shape than the relational operators < and >.

In the following explanation of the semantics of the operators on lists l denotes the list (11,12,11,13,14):

hd Return the first element (the head of a list). That is, hd $l \equiv 11$. The argument to hd must not be an empty list $(\langle \rangle)$.

tl	Return the list where the first element has been removed (return the tail). That is that $l \equiv (12,11,13,14)$.
[1]	Return element number <i>i</i> in a list. That is, $l[3] \equiv 11$ and $l[5] \equiv 14$. The index value must not be less than 1 or greater that the length of the list.
len	Return the length of a list. That is, len $l \equiv 5$.
elems	Return the set which consist of those elements which are in a list. That is, elems $l \equiv \{11, 12, 13, 14\}$.
ind	Return the set of integer objects which are the legal index values for a list. That is, ind $l \equiv \{1,2,3,4,5\}$.
\sim	Concatenate two lists. That is $l \frown \langle 0,1 \rangle \equiv \langle 11,12,11,13,14,0,1 \rangle$.
conc	Concatenate all those list which are elements of the list given as argument. That is conc $\langle \langle 0,7 \rangle, l, \langle 9 \rangle \rangle \equiv \langle 0,7,11,12,11,13,14,9 \rangle$
=, ≠	Test for equality and inequality of lists.

Example

In terms of Meta-IV expressions, the properties of the list operators hd, tl, ind, dents and cone can be illustrated as follows:

hd $l = (\text{if } l = \langle \rangle \text{ then undefined else } l[1])$ tl $l = \langle l[i] \mid 2 \le i \le \text{len } l \rangle$ ind $l = \{i \mid 1 \le i \le \text{len } l\}$ elems $l = \{l[i] \mid i \in \text{ind } l\}$ conc $l = (\text{if } l = \langle \rangle \text{ then } \langle \rangle \text{ else hd } l \frown \text{ conc tl } l \rangle$

5.4.7 Map Domains

A map Domain (i.e. a table) is constructed by specifying the domain of entry objects, followed by the m operator and followed by the domain of the objects contained in the mapping (the range values)

Example

```
5 Entity-dict = (Identifier₁ Entityclass) = Entitydescr ∪
ENVIRONMENT = Reachability-set ∪
EXPIREDF = Identifier₁ ∪
PIDSORT = Identifier₁ ∪
NULLVALUE = Identifier₁ ∪
TRUEVALUE = Identifier₁ ∪
FALSEVALUE = Identifier₁
```

The full definition of the *Entity-dict* mapping is given above. It shows how the m-operator is used and also that composite mappings can be constructed by using the domain merge operator \cup , that is, given a mapping of domain *Entity-dict*:

- we lookup in the mapping by applying an object of the unnamed tree (*Identifier*₁ *Entityclass*) and the result is an object of domain *Entitydescr* or
- we apply the Quot value ENVIRONMENT and the result is an object of domain Reachability-set or
- we apply the Quot value EXPIREDF and the result is an object of domain Is-expired or
- we apply the *Quot* value PIDSORT and the result is an object of domain *Identifier*₁ or
- we apply the *Quot* value NULLVALUE and the result is an object of domain *Identifier*₁ or
- we apply the *Quot* value TRUEVALUE and the result is an object of domain *Identifier*₁ or
- we apply the *Quot* value FALSEVALU E and the result is an object of domain *Identifier*₁.

We can only apply a value if it previously has been put into the mapping object, as opposed to functions where the correspondence between argument values and result values are fixed and defined when the function is defined.

Mapping values can be constructed by using an explicit mapping constructor which is a list of pairs of entry values and range values enclosed in square brackets, i.e.

 $[1 \rightarrow \mathbf{D}, 2 \rightarrow \mathbf{AA}, 4 \rightarrow \mathbf{BB}, 9 \rightarrow \mathbf{ABC}, 5 \rightarrow \mathbf{XYZ}]$

denotes a mapping value of domain Intg m Quot.

Also implicit mappings may be constructed. For example the implicit mapping

 $[a \mapsto b \mid a \in N_1 \land a * a = b]$

is equivalent to the infinite mapping

 $\begin{array}{l} [1 \rightarrow 1, \\ 2 \rightarrow 4, \\ 3 \rightarrow 9, \\ \dots \rightarrow \dots \end{array}]$

In the following explanation of the semantics of the operators on mappings in denotes the first of the mapping specified explicitly above:

m(entryvalue)	Return a value from a mapping, that is, $m(1) \equiv D$ and $m(9) \equiv ABC$.
+	Overwrite a mapping with another mapping. This operator is not com- mutative, that is
	$m + [0 \mapsto XX, 1 \mapsto B] \equiv$
	$[0 \mapsto XX, 1 \mapsto B, 2 \mapsto AA, 4 \mapsto BB, 9 \mapsto ABC, 5 \mapsto XYZ]$
	whereas
	$[0 \mapsto XX, 1 \mapsto B] + m \equiv$
	$[0 \mapsto XX, 1 \mapsto D, 2 \mapsto AA, 4 \mapsto BB, \ 9 \mapsto ABC, 5 \mapsto XYZ]$
\mathbf{N}	Exclude a given set of entry values from a mapping, that is
	$m \setminus \{1,2,3\}$ is
	$[4 \mapsto BB, 9 \mapsto ABC, 5 \mapsto XYZ]$
dom	Return the set which contains exactly those entry values which are present in a given mapping, that is
	dom $m \equiv \{1, 2, 4, 5, 9\}$
rng	Return the set which contains exactly those range values which are contained in a given mapping, that is
	rng $m \equiv \{D,AA,BB,ABC,XYZ\}$
=,≠	Test for equality and inequality of two mappings.
merge	From the given set of mappings, return the mapping which is con- structed by merging all the mappings contained in the set, that is $\{m, [0 \mapsto WE], [10 \mapsto D]\} \equiv$
	$[0 \mapsto WE, 10 \mapsto D, 1 \mapsto D, 2 \mapsto AA, 4 \mapsto BB, \ 9 \mapsto ABC, 5 \mapsto XYZ]$
	If any of the mappings contained in the set have overlapping entries, an arbitrary value among the possible values is chosen.

The empty mapping is denoted by [] (two square brackets very close to each other)

Example

In terms of Meta-IV expressions, the properties of the mapping operators \, + and merge can be illustrated as follows:

 $\begin{array}{l} m1 \setminus s = [a \mapsto b \mid a \in \operatorname{dom} m1 \setminus s \wedge m1(a) = b] \\ m1 + m2 = [a \mapsto b \mid (a \in \operatorname{dom} m2 \wedge m2(a) = b) \vee (a \in \operatorname{dom} m1 \setminus \operatorname{dom} m2 \wedge m1(a) = b)] \\ merge m1 = (if m1 = \{\} \\ & then [] \\ & else (let element \in m1 in \\ & element + merge m1 \setminus \{element\})) \end{array}$

5.4.8 Pid Domains

A Pid domain (corresponding to the Pid sort in SDL) is constructed by means of the II symbol. Optionally it may be qualified by the processor type to indicate which kind of Pid values the domain denotes, for example

6 Discard-Signals :: Π (input-port)

The Discard-Signals domain (defined in the Dynamic Semantics) contains Pid objects qualified by the processor type *input-port*. The Meta-IV Pid values should not be confused with the SDL Pid values which in SDL are *Ground-term*₁s, i.e. The domain of the SDL Pid values are defined in the Dynamic Semantics to be:

7	Pid-Value	=	Value
8	Value	=	Ground-term ₁

Meta-IV Pid values are created when applying the start statement/expression. It corresponds to the create request action in SDL. For example, when the *system* processor creates an instance of a *timer* processor with the actual parameter *timerf*, it looks like:

example

start timer(timerf)

When the start construct is used as an expression, it creates a processor instance and returns the Meta-IV Pid value of this instance (corresponding to the OFFSPRING value in SDL). For example when the sdl-process processor starts its inputport processor:

start input-port(selfp, dict(EXPIRED))

an instance of the input-port processor is created and the resulting Meta-IV Pid value is used by the *sdl-process* for identifying the *input-port*. The parameters *selfp* and *dict*(EXPIRED) are given to the created instance.

Communication is performed by the synchronous communication primitives input and out-put. In the output construct, we can either choose to communicate with a specific processor instance or we can choose to communicate with an unspecified instance of a specific processor type.

Example

output mk-Some-tree(somevalue, someothervalue, ...) to p

where p either denotes a Pid value or p is the name of a processor type. The values sent by the processor are usually encapsulated in a named tree object (of some **communication** domain) and such trees can therefore be equated to the signal concept in SDL, i.e. *Some-tree* can be regarded as a signal.

In the input construct, we both specify the communication object we want to receive and the action which should be taken when the object is received. In addition, we may specify a name which after the reception of the object denotes the Pid value of the sending processor (corresponding to SENDER in SDL) or which restricts the possible senders i.e.

After reception of Some-tree, *a*, *b* and *d* will denote the values conveyed by *Some-tree* and for *p* there are three possible interpretations:

- If p is a processor type name then the input should be received from an instance of that particular processor type
- If *p* is a name which is not already defined then this occurence is the defining occurence of the name and it is visible in the expression or statements which follow the input clause. It denotes the Meta-IV Pid value of the sender.

If p is an expression then it must be of the type II and the input will be received from the processor instance denoted by the expression.

If one of several inputs may be received, a number of input constructs separated by comma are specified and the number is enclosed by braces, i.e.

In some cases we may want to specify that either an input or an output should be made, depending on which communication first is possible (not applicable in SDL due to the fact that in SDL communication is asynchronous). In such cases, output constructs are included in the set of communication events, i.e.

Often the cycle construct is used in conjunction with input and output, if the communication should be repeated, i.e.

which means that after a communication event, the processor instance will take the appropriate action and then start waiting for a new event to happen.

5.4.9 Reference Domains

When a Meta-IV variable is declared by

dcl v type Intg;

a Meta-IV storage location is allocated and the variable (v) will denote a reference to the location. When the content of the location is accessed, the c operator (contents operator) is used as shown earlier. When the variable is used without the contents operator the result is a value of the ref domain, that is, a reference to the storage location. ref domains are specified by using the keyword ref, followed by the appropriate domain. For example

9 VarD ::: Variable-identifier₁ Sort-reference-identifier₁ [**REVEALED**] ref Stg

The variable descriptor includes a reference to the domain Stg. The VarD descriptor is defined in the Dynamic Semantics and it is described further in the associated annotations.

5.4.10 Optional Domains

The square brackets which are extensively used in the domain definitions mean optionality.

Example

10	Signal-definition ₁	:: Signal-name ₁ Sort-reference-identifier	r ₁ •
		[Signal-refinement ₁]	

expresses that in objects of the tree *Signal-definition*₁, the object of the domain *Signal-refinement* may or may not be present. If it is not present, the field will contain the type-less value **nil**

```
(let mk-Signal-definition1(name, sort, refinement) = /* some Signal-definition1 object */ in
if refinement = nil then
    /* some actions */
    else
    (let mk-Signal-refinement1(...) = refinement in
        /* some other actions using the signal refinement */))
```

5.5 The let and def Constructs

As shown earlier, the let construct can be used for composing and decomposing objects. The let construct is more generally used whenever we want some name to denote some specific object (often it is just in order to avoid too complicated and unreadable expressions). The names occuring on the left •hand side of the equal sign in the let construct are the defining occurences (except for domain names which must always be defined somewhere in a domain

definition). An introduced name can also be used on the right hand side of the equal sign (the name is then recursively defined) and in the expression which follows the let construct. In the example below, name1 is visible (i.e. may be used) in /*expression1*/, /*expression2*/, /*expression3*/ and /*expression4*/, name2 is visible in /*expression2*/, /*expression3*/ and /*expression3*/ and /*expression4*/. For the sake of restricting the visibility of the names introduced by a let, the let construct is enclosed by parenthesis. In the example above a signal refinement constitutes an expression and it starts with left parenthesis because a let construct is used.

There are two ways of specifying a sequence of lets:

```
let name1 = /* expression1 */ in
let name2 = /* expression2 */ in
let name3 = /* expression3 */ in
/* expression4 */
```

or

```
let name1 = /* expression1 */,
name2 = /* expression2 */,
name3 = /* expression3 */ in
/* expression4 */
```

The first form showing three lets is usually used in the FD when the order is important, that is if $/*expression2^*/$ uses name1 and if $/*expression3^*/$ uses name2 whereas the second form is used when the various lets are independent.

There are several different forms of a let construct. We have already seen how it can be used for decomposing objects. Other relevant forms are:

```
let name ∈ setorname1 in
/* some expression using name */
let name bes.t. /* condition using name */ in
/* some expression using name */
let name ∈ setorname2 bes.t. /* condition using name */ in
/* some expression using name */
let name(parameters) = /* function body */ in
/* some expression applying name */
```

The first form reads: Extract an arbitrary value belonging to the set or belonging to the domain denoted by setorname1 and denote the value by name.

The second form reads: Construct a value, i.e. let name be such that the specified condition holds for the value.

The third form is a combination of the two previous forms, where both restrictions apply. If no such value exists, the specification is erroneous.

The fourth form reads: Construct a local function (called *name*) which has some formal parameters (*parameters*) and a body.

Example

Define the square root of 3:

let $r \in Real$ be s.t. $r > 0 \land r * r = 3$ in

Example

Define the factorial function where n is the formal parameter:

let fact(n) = if n < 0 then error else if n = 0 then 1 else n * fact(n-1) in

When defining a name for an object which is constructed by referring to the global state (i.e. if the name is defined in terms of an imperative expression) the def notation is used instead of the let notation, that is, the keyword let is replaced by the keyword def, the equal symbol is replaced by a colon and the keyword in is replaced by a semicolon (because the def construct is used in statement context, see section 5.7). For instance, if we want to denote a created processor instance value by a name, we write:

(def pid : start input-port(somevalue);
/* some statements using the pid value */)

or if we want to decompose the result of an imperative function we write:

(def mk-Some-tree(a, b) : some-imperative-function(...);
/* some statements using a and b */)

There also exist a def version of the "be such that" construct:

(def $r \in Real \text{ s.t. } r > 0 \land r * r = c v1;$ /* some statements using r */)

where we use def because we use a variable (v1) in the evaluation of r. It reads: Define a *Real* value r such that the square of r equals the contents of the variable v1.

It should be noted that the names introduced in let and def are not variables. They are names representing a specific value and it is not allowed to assign a new value to such names.

5.6 Quantification

Meta-IV also provides the mathematical quantifiers- the universal quantifier represented by the symbol \forall , the existential quantifier represented by the symbol \exists and the unique quantifier represented by the symbol \exists !. These quantifiers may be used in quantified expressions which return the boolean value true if a specified condition (a predicate) on an object is satisfied.

Example

identifiers-defined-on-system-level $(p) \triangleq$

1 $(\forall \mathbf{mk} \text{-Identifier}_1(q,) \in p)(\text{len } q = 1)$

```
type: Identifier_1-set \rightarrow Bool
```

This function returns true if and only if for all identifiers $(Identifier_1)$ in the set p it holds that the length of its qualifier (q) is equal to 1 (the second pair of parenthesis encloses the predicate expression).

Example

one-identifier-defined-on-system-level(p) \triangleq

```
1 (\exists \mathbf{mk} - Identifier_1(q, ) \in p)(len q = 1)
```

```
\textbf{type}: \quad \textit{Identifier}_1 \textbf{-set} \rightarrow \textit{Bool}
```

This function returns true if and only if there exist at least one identifier (*Identifier*₁) in the set p for which the length of its qualifier (q) is equal to 1.

Example

```
exactly-one-identifier-defined-on-system-level(p) \triangleq
```

```
1 (\exists !mk-Identifier_1(q, ) \in p)(len q = 1)
```

```
type: Identifier_1-set \rightarrow Bool
```

This function returns true if and only if there exist exactly one (*Identifier*₁) in the set p for which the length of its qualifier (q) is equal to 1.

Alternatively, we can choose to decompose the identifier in the predicate expression instead of in the quantification, that is

```
identifiers-defined-on-system-level(p) \triangleq
```

```
1 (\forall p' \in p)

2 ((\text{let mk-Identifier}_1(q, ) = p' \text{ in})

3 \text{len } q = 1))

type: Identifier_1-set \rightarrow Bool
```

Note that apostrophe and. dash are legal characters in Meta-IV names.

5.7 Auxiliary Statements

- Identity statement The keyword I indicates an empty statement i.e. a statement which doesn't do anything.
- Undefined statement/expression The keyword undefined indicates that no semantics can be given.
- Return statement The keyword return followed by an expression terminates the elaboration of an imperative function and the result is the given expression.

- Error statement/expression. The keyword error indicates in the FD a dynamic SDL error.
- Assign statement. Like in SDL. The contents operator (c) is not used when assigning to variables.
- For and while statement. Same (well-known) concept as in CHILL. The statements to be repeated are enclosed in parenthesis.
- Trap and exit statement/expression. Trap (handle) any exits caused by an exit statement/expression. If an argument is given to the exit statement, it is only trapped if the expression given matches the value given in the trap exit statement. A special version of the trap exit mechanism- the tixe construct have been used in the functions *int-process-graph* and *int-procedure-graph*. The **tixe** construct is explained in the associated annotations.

5.8 Deviations from the notation used in the Formal Definition of CHILL

• In the formal definition of CHILL, the predefined domain names consist of boldface uppercase letters (e.g. **BOOL**, **INTG**) and names denoting semantic domains may consist of uppercase letters only.

In the formal definition of SDL, all domain names are in italic, the first letter is in uppercase and they contain at least one lowercase letter.

• In the formal definition of CHILL, all objects are finite.

In the formal definition of SDL, objects may be infinite. The semantics of some of the operators are not well-defined when applied on such objects, e.g. operators like cardinality and equality have not been used on potentially infinite objects.

In addition, a special constant *infinite* has been used in *transform-process* in Annex F.2. for representing the "unbounded number of instances" in AS_1 .

- In the formal definition of SDL, the Meta-IV notation has been extended to include the elementary domain *Char* and the character strings objects (see section 5.4.4.3).
- In the *path* processor in Annex F.3. a so-called "output guard" has been used. The concept is described in the annotations attached to the *Path* processor as well as in [4].

5.9 Example: Demon game specified in Meta-IV

In the following, it is shown how Meta-IV can be used for defining the semantics of Demon game. For further details about Demon game, refer to Z.100 §2.9.

Communication demon \rightarrow monitor and monitor \rightarrow game

	Bump nication user \rightarrow monitor	÷ ()	
	Newgame	: ()	
Communication game \rightarrow monitor			
13	Gameover	:: П	
Communication monitor \rightarrow game			
14	Gameoverack	:: ()	
Communication game \rightarrow user			
15	Gameid	:: ()	
16	Win	: () : ()	
17	Lose	: () : ()	
18	Score	:: () :: Intg	
Communication user \rightarrow game			
	Probe	:: ()	
20	Result	жŎ	
21	Endgame	= Ö	
$int-demon-game() \triangleq$			

1 start monitor()

 $\texttt{type:} \quad () \Rightarrow ()$

monitor processor () \triangleq

2 gameset := {} type Π -set;	
3 cycle (input mk-Newgame() from sender	
4 \Rightarrow if sender \notin cuserset then	
5 (def offspring : start game(sender)	
6 $gameset := c gameset \cup \{offspring$	};
7 $userset := c userset \cup {sender})$	
8 else	
9 I ,	
10 input mk-Gameover(player) from sender	
11 \Rightarrow (gameset := c gameset \ {sender};	
12 $userset := c userset \setminus \{player\};$	
13 output mk-Gameoverack() to send	:r),
14 input mk-Bump() from demon	
15 \Rightarrow for all $pid \in gameset$ do	
16 output mk-Bump() to pid))	

```
type: () \Rightarrow
```

game processor (player) \triangleq

1	(dcl count := 0 type Intg;
2	dcl even := true type Bool;
3	output mk-Gameid() to player;
4	cycle (input mk-Probe() from user
5	\Rightarrow if c even
6	then (output mk-Win() to player;
7	$\operatorname{count} := \operatorname{count} + 1)$
8	else (output mk-Lose() to player;
9	$\operatorname{count} := \operatorname{c} \operatorname{count} - 1),$
10	input mk-Result() from user
11	\Rightarrow output mk-Score(count) to player,
12	input mk-Endgame() from user
13	\Rightarrow (output mk-Gameover(player) to monitor;
14	input mk-Gameoverack() from monitor
15	\Rightarrow stop),
16	input mk-Bump() from monitor
17	\Rightarrow even := $\neg c$ even))

 $\texttt{type}: \quad \varPi \Rightarrow ()$

References

- [1] Dines Bjorner and Cliff B. Jones Formal specification and software development Prentice-Hall Publ. 1982
- [2] The Formal Definition of CHILL CCITT Manual ITU, Geneva 1981
- P. Folkjaer, D. Bjorner

 A formal model of a generalized CSP-like language, IFIP 8th World Computer Conference Proceedings, North-Holland Publ. 1980
- [4] C.A.R. Hoare Communicating Sequential Processes Prentice-Hall 1985

ITU-T RECOMMENDATIONS SERIES Series A Organization of the work of the ITU-T Series B Means of expression: definitions, symbols, classification Series C General telecommunication statistics Series D General tariff principles Series E Overall network operation, telephone service, service operation and human factors Series F Non-telephone telecommunication services Series G Transmission systems and media, digital systems and networks Series H Audiovisual and multimedia systems Series I Integrated services digital network Series J Transmission of television, sound programme and other multimedia signals Series K Protection against interference Series L Construction, installation and protection of cables and other elements of outside plant Series M TMN and network maintenance: international transmission systems, telephone circuits, telegraphy, facsimile and leased circuits Series N Maintenance: international sound programme and television transmission circuits Series O Specifications of measuring equipment Series P Telephone transmission quality, telephone installations, local line networks Series Q Switching and signalling Series R Telegraph transmission Series S Telegraph services terminal equipment Series T Terminals for telematic services Series U Telegraph switching Series V Data communication over the telephone network Series X Data networks and open system communications Series Y Global information infrastructure and Internet protocol aspects Languages and general software aspects for telecommunication systems Series Z