Full Availability Group,

Loss System

(Solutions to Exercises)

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A = traffic offered = $\lambda \cdot \tau$ erl.	TXA 1
where	
λ = Calling rate = Expected no. of calls per unit of time;	
τ = Mean holding time expressed in the same unit of time.	
$\lambda = 1000 \text{ calls/hour}$	a
$\tau = 90 \text{ sec.}$	
$A = \frac{1000 \cdot 90}{3600} = \underline{25 \text{ erl.}}$	
$\lambda = 1200 \text{ calls/hour}$	b
$\tau = 2 \min.$	
$\mathbf{A} = \frac{1200 \cdot 2}{60} = \underline{40 \text{ erl.}}$	
$\lambda = 4$ calls/sec.	c
$\tau = 1.6 \text{ min.}$	
$A = 4 \cdot 1.6 \cdot 60 = \underline{384 \text{ erl}}.$	
A = 35 erl.	TXA 2
$\tau = 140$ sec.	
$\lambda = \frac{35}{140} \text{ calls/sec.} = \frac{35 \cdot 3600}{140} = \underline{900 \text{ calls/ hour}}$	
A = 33 erl.	TXA 3
$\lambda = 1100$ calls/hour	
$\tau = \frac{33 \cdot 3600}{1100} = \underline{108 \text{ sec.}}$	

n	=	Number	of devices $= 10$.		TXA 4
		Number of bury devices			a
p	=	= Number of busy devices.			
tp	, =	Total tin	ne during the period with exact	ly p busy devices.	
Т	$T = Total period.$ $\sum_{p=0}^{n} t_p = T$				
A	$^{1} =$	Traffic h	andled by the group during the	e period.	
A	¹ =	$\frac{1}{T} \cdot \sum_{p=0}^{n} p$	$\mathbf{t} \cdot \mathbf{t}_{p} = \sum_{p=0}^{n} p \cdot \frac{\mathbf{t}_{p}}{T}$		
	No.	of busy	Proportion of the total time	t _p	
	d		with exactly P busy devices	$p \cdot \frac{t_p}{T}$	
		P	t _p /T		
		0		—	
		1		—	
		2			
		3			
		4	—		
		5	0.10	0.50	
		6	0.20	1.20	
		7	0.25	1.75	
		8	0.15	1.20	
		9	0.20	1.80	
		10	0.10	1.00	
		Sum	$\sum \frac{t_p}{T} = 1.00$	$\sum p \cdot \frac{t_p}{T} = 7.45$	

 $A^1 = \underline{7.45 \text{ erl.}}$

E = Time congestion during the period = Proportion of time, when all devices are busy

 $= \frac{t_n}{T} = \frac{t_{10}}{T} = \underline{0.10}$

cont.

		cont	t:
Observation	No. of busy devices	TXA	44
no.		b	
1	8		
2	8		
3	10		
4	10		
5	9		
6	7		
7	7		
8	6		
9	5		
10	5		
Sum	75		
$A^1 = Traffic P$	nandled $\approx \frac{75}{10} = \underline{7.5 \text{ erl.}}$	_	
E =Time conge	estion $\approx \frac{2}{10} = \underline{0.20}$		

Erlang Distribution

 $\lambda = Calling rate$

 τ = Mean holding time

A = Traffic offered =
$$\lambda \cdot \tau$$

$$E = Time congestion = Call congestion = B =$$

$$= E_n(A) = \frac{A^n}{n!} / \sum_{\nu=0}^n \frac{A^{\nu}}{\nu!}$$

Where n = Number of devices. <u>n = 10</u>

Using the Erlang Table, we find:

A erl.	E ₁₀ (A)
1	0.0000
3	0.0008
5	0.0184
10	0.2146
15	0.4103
25	0.6224
50	0.8047
100	0.9011
200	0.9503
300	0.9668

TXA 5

Erlang Distribution

See Example TXA 5

 $\underline{A} = 10 \text{ erl.}$

Using the Erlang Table, we find:

n	E _n (10)
1	0.9091
2	0.8197
3	0.7321
5	0.5640
7	0.4090
10	0.2146
15	0.0365
20	0.0019
25	0.0000
30	0.0000

Erlang Distribution	TXA 7
$E_{20}(A) = 0.005$	
Using the part of the Erlang Table where E is an input parameter, we find:	
$A = \underline{11.092 \text{ erl.}}$	

TXA 6

Erlang Distribution	TXA 8
We want to find the smallest value of n, number of devices, for which $E_n (48) \le 0.002$	
Using the part of the Erlang Table where E is an input parameter, we find $E_{66} (47.51) = 0.002$ $E_{67} (48.38) = 0.002$	
We conclude: $n = \underline{67 \text{ devices}}$	
The other part of the Erlang Table could of course be used as well, but in that case interpolation has to be done. Erlang Distribution	TXA 9
n = Number of devices = 18	
λ = Calling rate = 480 calls/hour	
τ = Mean holding time = 105 sec.	
A = Traffic offered = $\lambda \cdot \tau$ = = $\frac{480 \cdot 105}{3600} = \underline{14 \text{ erl.}}$	
E = Time congestion	
B = Call congestion	
$E = B = E_{18} (14) = 0.0628$ (from the Erlang Table)	
	cont.

$A^{1} = \text{Traffic handled} = A \cdot [1 - E_{n}(A)] =$ = $14 \cdot [1 - E_{18}(14)] = 14 \cdot [1 - 0.0628] = \underline{13.12 \text{ erl}}$	cont: TXA 9
a = Mean of traffic handled per device =	
$= \frac{A \cdot (1 - E_n(A))}{n} = \frac{A^1}{n} = \frac{13.12}{18} = \underbrace{0.729 \text{ erl.}}_{n}$	
Traffic rejected = $A \cdot E_n (A)$ = $14 \cdot E_{18} (14) = 14 \cdot 0.0628 = 0.88 \text{ erl.}$	
Expected number of rejected calls per hour =	
$= \lambda \cdot E_n (A) = 480 \cdot E_{18} (14) = 480 \cdot 0.0628 = 30.1 \text{ calls/ hour}$	
Erlang Distribution	TXA
n = 5 devices	10
A = 2 erl.	
a _v = Traffic handled by the v:th device (v = 1, 2, 3, 4, 5)	
$2 \text{ erl.} \longrightarrow \bigcirc $	
Random hunting:	
$\alpha_{v} = \frac{A \cdot (1 - E_n(A))}{n} = \frac{2 \cdot (1 - E_5(2))}{5} =$	
$=\frac{2\cdot(1-0.0367)}{5}=\underbrace{0.385 \text{ erl.} (\nu=1,2,3,4,5)}_{$	cont.

Sequential hunting

 $a_{\nu} = A \cdot \left[E_{\nu-1}(A) - E_{\nu}(A) \right]$ $(v = 1,2,3,4,5; E_0(A) = 1 \text{ if } A > 0)$ Using the Erlang Table, we find $(E_0(2) = 1)$ $E_1(2) = 0.6667$ $E_2(2) = 0.4000$ $E_3(2) = 0.2105$ $E_4(2) = 0.0952$ $E_5(2) = 0.0367$ $= 2 \cdot [E_0(2) - E_1(2)] = 2 \cdot [1 - 0.6667] = 0.667$ erl. a_1 $= 2 \cdot [E_1(2) - E_2(2)] = 2 \cdot [0.6667 - 0.4000] = 0.533 \text{ erl.}$ a_2 etc. Result: = 0.667 erl. $a_2 = 0.533$ erl. $a_3 = 0.379$ erl. a_1 $a_4 = 0.231 \text{ erl.}$ $a_5 = 0.117 \text{ erl.}$ Note that $\frac{1}{5} \cdot \sum_{\nu=1}^{5} a_{\nu} = \frac{1}{5} \cdot 1.927 = 0.385 \text{ erl.}$ We conclude that the mean value of the traffic handled per device is the same for sequential hunting and for random hunting.

cont: TXA 10

Erlang Distribution TXA 11 A erl. \longrightarrow \bigcirc \bigcirc \bigcirc \bigcirc \bigcirc \bigcirc 2 3 1 n-1 n (sequential hunting) = Traffic handled by the v:th device a,, $= \cdot \mathbf{A} \cdot \left[\mathbf{E}_{\nu-1}(\mathbf{A}) - \mathbf{E}_{\nu}(\mathbf{A}) \right]$ a, $(v = 1,2,...,n; E_0(A) = 1 \text{ if } A > 0)$ Let a = Mean of traffic handled by the different devices = $=\frac{1}{n}\cdot\sum_{\nu=1}^{n}a_{\nu}$ $= \frac{1}{n} \cdot \sum_{\nu=1}^{n} A \cdot [E_{\nu-1}(A) - E_{\nu}(A)] =$ a $= \frac{1}{n} \cdot A \cdot \left[1 + \sum_{\nu=1}^{n-1} E_{\nu}(A) - \sum_{\nu=1}^{n-1} E_{\nu}(A) - E_{n}(A) \right] =$ $=\frac{A\cdot[1-E_n(A)]}{n}=$ = Traffic handled per device in a group with random hunting, n devices and traffic offered = A erl.

Erlang Distribution			TXA
E_{10} (A) = 0.005 gives	$\Lambda = 3.061 \text{ orl}$		12
$E_{10}(A) = 0.005$ gives $E_{100}(A) = 0.005$ gives			
$2_{100}(R) = 0.005 \text{ gives}$	$A = \underline{00.91 \text{ cm}}$		
according to the Erla	ng Table)		
C	<i>c</i> ,		
	n = 10	n = 100	
А	3.961 erl.	80.91 erl.	
$E_n(A)$	0.005	0.005	
$A_1 = 1.1 \cdot A$	4.36 erl.	89.00 erl.	
$E_n(A_1)$	0.009	0.024	
$A_2 = 1.2 \cdot A$	4.75 erl.	97.09 erl	
$E_n(A_2)$	0.014	0.059	
L			
f "a" denotes traffic h	-		
	n = 10	n = 100	
Α	a = 0.394	a = 0.805	
$A_1 = 1.1 \cdot A$	a = 0.432	a = 0.869	
$A_2 = 1.2 \cdot A$	a = 0.469	a = 0.914	

Denote the length of the interval by T. The distribution function
$$F(x)$$
TXA
13 $F(x) = P\{T \le x\}$ 13Calculate the complementary distribution function:
 $1 - F(x) = P\{T > x\}$ a $0 \le j \le n$:
The interval may end by a call or a termination. Then $T > x$ ifa1) No call in $(0, x)$ and
2) No termination in $(0, x)$.aThe probability of 1) is $e^{-\lambda \cdot x}$
The probability of 2) is $e^{-j \cdot \frac{x}{\tau}}$ aConsequently,
 $1 - F(x) = e^{-\lambda \cdot x} \cdot e^{-j \cdot \frac{x}{\tau}} = e^{-\frac{A+j}{\tau} \cdot x}$ bi.e. an exponential distribution with the parameter
inverse of the parameter i.e. $\frac{A+j}{\tau}$ Cont. $\frac{\tau}{A+j}$ cont.

The state ends by a transition to (j+1) if the first event is a call.
The conditional probability that the first event is a call occuring in
(x, x+dx) is
$$P\{\text{the first event is a call/a call occurs in } (x, x + dx)\} = P\{\text{no termination in } (0, x), \text{ no call in } (0, x), \text{ one call in } (x, x + dx)\} = e^{-j \cdot \frac{x}{\tau}} \cdot e^{-\lambda \cdot x} \cdot \lambda \cdot dx$$
Taking away the condition, by the theorem of total probability, the required probability p is
$$p = \int_{0}^{\infty} e^{-j \cdot \frac{x}{\tau}} \cdot e^{-\lambda \cdot x} \cdot \lambda \cdot dx = \frac{\lambda}{\frac{A+j}{\tau}} = \frac{A}{\frac{A+j}{\tau}}$$
The probability that the state ends by a transition to (j-1) is
$$1 - \frac{A}{A+j} = \frac{j}{\frac{A+j}{2}}$$

$$\frac{j=0:}{1 - F(x)} = P\{\text{no call in } (0,x)\} = e^{-\lambda \cdot x}$$
The mean value is the inverse of the parameter =
$$\frac{1}{\frac{\lambda}{2}}$$
cont.

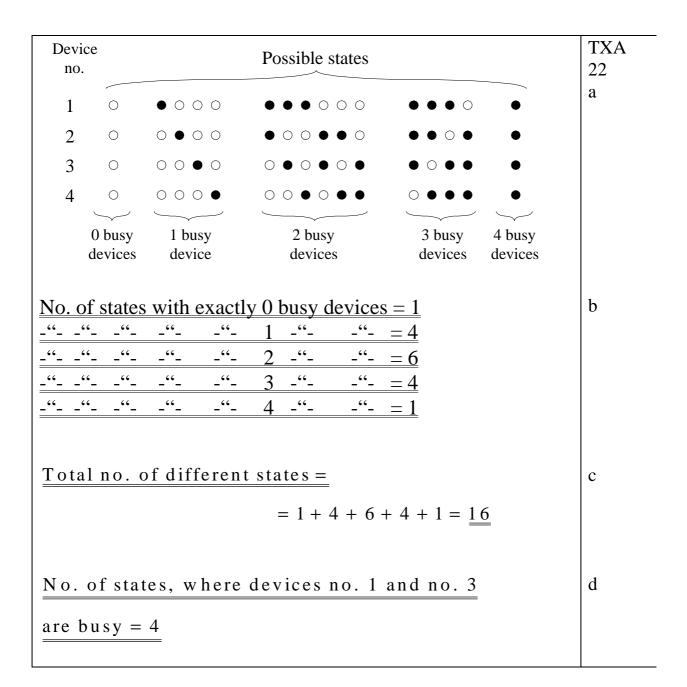
$P\{\text{state}(j=0) \rightarrow \text{state}(j=1)\} = \underline{1}$ $P\{\text{state}(j=0) \rightarrow \text{state}(j=-1)\} = \underline{0}$	cont: TXA 13
$\underline{\underline{j=n:}}$	c
$1 - F(x) = P\{\text{no termination in } (0, x)\} = e^{-n \cdot \frac{x}{\tau}}$	a
$F(x) = \underline{1 - e^{-\frac{n \cdot x}{\tau}}}$	
Mean value = $\frac{\tau}{\underline{n}}$	b
$P\{\text{state}(j=n) \rightarrow \text{state}(j=n+1)\} = \underline{0}$ $P\{\text{state}(j=n) \rightarrow \text{state}(j=n-1)\} = \underline{1}$	с
Denote the call length by X.	TXA
Exactly 2 pulses if $3 \le x < 6$:	14 a
$P\{3 \le x < 6\} = F(6) - F(3) =$	
$= \left(1 - e^{-\frac{6}{3}}\right) - \left(1 - e^{-\frac{3}{3}}\right) =$	
$= e^{-1} - e^{-2} = 0.3679 - 0.1353 = \underline{0.2326}$	
≤ 2 pulses if x < 3:	b
$P\{x < 3\} = 1 - e^{-\frac{3}{3}} = 1 - e^{-1} = \underline{0.6321}$	
\geq 2 pulses if x \geq 6:	с
$P\{x \ge 6\} = e^{-\frac{6}{3}} = e^{-2} = \underline{0.1353}$	cont.

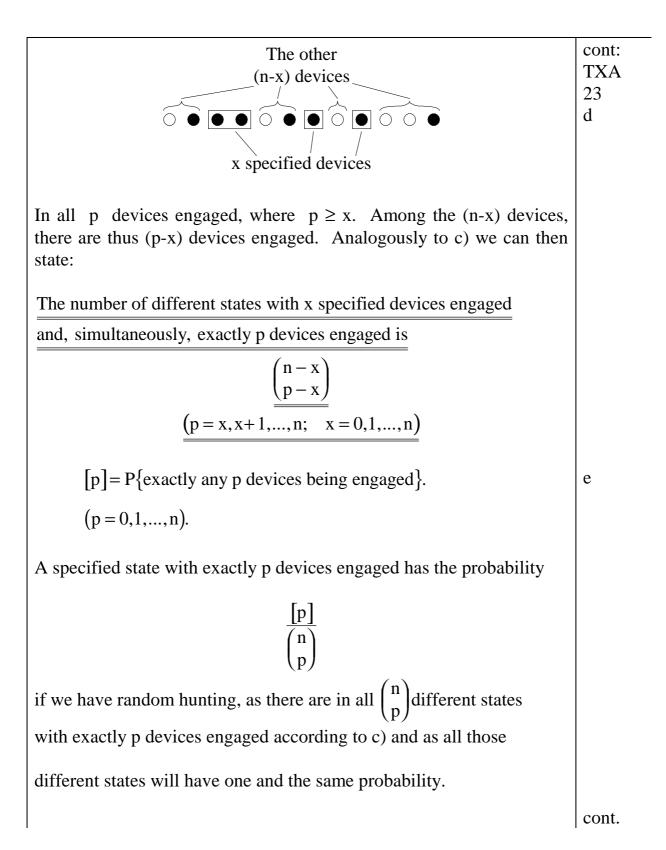
\geq 2 pulses if x \geq 3:	cont:
	TXA
$P\{x \ge 3\} = e^{-\frac{3}{3}} = e^{-1} = \underline{0.3679}$	14
	d
≤ 2 pulses if x < 6:	e
$-\frac{6}{2}$	
$P\{x < 6\} = 1 - e^{-\frac{6}{3}} = 1 - e^{-2} = \underline{0.8647}$	
Denote the number of pulses by K.	TXA
	15
K Probability	
$1 \qquad -\frac{m}{\tau}$	
$1-e^{-\tau}$	
$2 \qquad \frac{m}{e^{\tau} - e^{-\frac{2m}{\tau}}}$	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
$\int \frac{-2\pi n}{\tau} - \frac{-3\pi n}{\tau}$	
$i (i-1) \cdot m i \cdot m$	
$\begin{bmatrix} -\frac{-\sqrt{3}}{\tau} & -\frac{-\sqrt{3}}{\tau} \\ -\frac{-\sqrt{3}}{\tau} & -\frac{-\sqrt{3}}{\tau} \end{bmatrix}$	
$E\{K\} = \sum_{j=1}^{\infty} j \cdot \left(e^{-\frac{(j-1) \cdot m}{\tau}} - e^{-\frac{j \cdot m}{\tau}} \right) =$	
$\left F\{K\} = \sum_{i=1}^{\infty} i \cdot \left e^{-\frac{(3-\gamma)}{\tau}} - e^{-\frac{3-\gamma}{\tau}} \right =$	
$\begin{bmatrix} D_{i} \begin{bmatrix} \mathbf{r} \\ \mathbf{j} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{j} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{j} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \begin{bmatrix} \mathbf{r} \\ \mathbf{r} \end{bmatrix} \end{bmatrix} \begin{bmatrix} $	
$\begin{pmatrix} & m \end{pmatrix}$ $\begin{pmatrix} m & 2m \end{pmatrix}$ $\begin{pmatrix} 2m & 3m \end{pmatrix}$	
$= \left(1 - e^{-\frac{m}{\tau}}\right) + 2 \cdot \left(e^{-\frac{m}{\tau}} - e^{-\frac{2m}{\tau}}\right) + 3 \cdot \left(e^{-\frac{2m}{\tau}} - e^{-\frac{3m}{\tau}}\right) + \dots$	
$\begin{bmatrix} -1 & -2 & -2 & -2 & -2 & -2 & -2 & -2 &$	
$=1 \frac{m}{\tau} e_4 \frac{m}{\tau} 24 e_4 \frac{m}{\tau} \frac{-m}{\tau^2} e_4 \frac{-2m}{\tau^2} + \frac{2m}{\tau^2} e_4 \frac{-2m}{\tau^2} - \frac{3m}{\tau^2} - \frac{3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} e_4 \frac{-3m}{\tau^2} + \frac{3m}{\tau^2} $	
$\begin{bmatrix} -1 & -1 & -1 & -1 & -1 & -1 & -1 & -1 $	
$=1 + e^{-\frac{m}{\tau}} + e^{-\frac{2m}{\tau}} + e^{-\frac{3m}{\tau}} + \dots$	
$=1+e^{+}+e^{+}+e^{+}+e^{-}+\cdots$	
$-\frac{m}{r}$	
= a geometric series with quotient $e^{-\tau}$,	
/_	
so the sum is $\frac{1}{1} = \frac{e^{m/\tau}}{1}$	
so the sum is $\frac{1}{1 - e^{-\frac{m}{\tau}}} = \frac{e^{m/\tau}}{e^{m/\tau} - 1}$	
$1-e^{-t}$	

Denote length of conversation by x.	TXA 16
$P\{x > 6 \min.\} = P\{x > 6 \underline{and} A \rightarrow B\} +$	10
$+ P\{x > 6 \underline{and} B \rightarrow A\} =$	
$= P_{A \to B} \cdot P\{x > 6/A \to B\} + P_{B \to A} \cdot P\{x > 6/B \to A\} =$	
$= 0.55 \cdot e^{-\frac{6}{4}} + 0.45 \cdot e^{-\frac{6}{3}} = 0.55 \cdot e^{-1.5} + 0.45 \cdot e^{-2} =$	
$= 0.55 \cdot 0.2231 + 0.45 \cdot 0.1353 = \underline{0.184}$	
Take one of the conversations. The probability that it is still in progress after 1 min. is $e^{-\frac{1}{3}}$	TXA 17
The probability that it has ended before 1 min. is $1 - e^{-\frac{1}{3}}$	
The five conversations are independent of each other. So the problem is analog to the situation when we make 5 independent trials in which the probability of success is constant. In this example success = conversation in progress, so by the binomial distribution the required probability is	
$\left(\frac{5}{2}\right) \cdot \left(e^{-\frac{1}{3}}\right)^2 \cdot \left(1 - e^{-\frac{1}{3}}\right)^{5-2} =$	
$= 10 \cdot 0.7165^2 \cdot 0.2835^3 = \underline{0.117}$	

$$\begin{array}{ll} a_{9} = \underbrace{A(E_{8}(A) - E_{9}(A))}_{18} & \begin{array}{c} TXA \\ 18 \\ a \\ b \end{array} \\ P_{9} = \underbrace{A^{9}}_{9!} \Big/ \sum_{j=0}^{10} \underbrace{A^{j}}_{j!} = \underbrace{10}_{\underline{A}} \cdot E_{10}(A) \\ \hline E_{9}(A) & \begin{array}{c} c \\ P\{9 \text{ first trunks occupied}\} = \\ = P\{9 \text{ first occupied and 10th free}\} + \\ + P\{9 \text{ first occupied and 10th occupied}\} \\ \hline Left \text{ side} = E_{9}(A). \\ Last term on RHS = P\{all 10 \text{ occupied}\} = E_{10}(A). \\ \hline Consequently: \\ E_{9}(A) = P(9 \text{ first occ. and 10th free}) + E_{10}(A) \\ and \\ P\{9 \text{ first occ. and 10th free}\} = E_{9}(A) - E_{10}(A) \end{array}$$

	ГХА 19
$\underline{\text{Traffic offered}} = 6 \cdot 0.5 = \underline{3 \text{ erl.}}$	
$\underline{\underline{\text{Time congestion}}} = P\{\text{all 6 trunks are occupied}\} =$	
= P{all 6 sources are occupied} = $0.5^6 = \underline{0.016}$	
<u>Call congestion = 0</u> as no calls can arrive when all trunks	
are occupied.	
	ΓΧΑ
$\underline{N} >> n \Longrightarrow Erlang Distribution:$	20
A = 3 erl.	
$\underline{\text{Time congestion} = \text{Call congestion} =}$	
$= E_n(A) = E_6(3) = \underline{0.052}$	
	ГХА 21
No. of No. of Distribution Traffic Traffic Call Time	
Sources devices offered Offered Conges Conges-	
per -tion tion	
N n source erl. B E	
N n erl. erl. B E 6 6 BERNOULLI 0.5 3 0 0.016	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	





In order to find	cont:
$h(x,p) = P\{x \text{ specified devices engaged, and,}$	TXA
()r) [r · · · · · · · · · · · · · · · · · ·	23
simultaneously, exactly p devices engaged}	e
we shall thus add a certain number of equal probabilities,	
namely $\frac{[p]}{\binom{n}{p}}$; that number is, according to d), $\binom{n-x}{p-x}$.	
Therefore,	
$h(x,p) = {n-x \choose p-x} \cdot \frac{[p]}{{n \choose p}} \qquad (p = x, x+1,,n)$	
Now, we have that	
$H(x) = P\{x \text{ specified devices engaged}\}$	
must be equal to	
n	
$H(x) = \sum_{n=1}^{n} h(x,p)$	
p=x	
so the result is:	
$H(x) = \sum_{p=x}^{n} {n-x \choose p-x} \cdot \frac{[p]}{\binom{n}{p}}$	

The probability that 3 specified devices are engaged = the probability	TXA
that 3 specified sources are engaged = The probability of success in 3	24
specified trials out of 6 independent experiments where the probability	
of success = 0.5 in each trial, i.e.	
$0.5^3 = 0.125$	
Erlang Distribution:	TXA
	25
$E_n(A)$	
$H(x) = \frac{E_n(A)}{E_{n-x}(A)}$	
n = 6; A = 3 erl; x = 3	
$E_6(3) = 0.052157$	
$H(3) = \frac{E_6(3)}{E_3(3)} = \frac{0.052157}{0.346154} = \underline{0.151}$	