

Exchange Locations and Boundaries

Solution to Case Studies

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Case Study : Exchange Locations and Boundaries

Solution of CASE STUDY 1

EXCHANGE BOUNDARIES

For this simple case, the boundary between the exchanges will be situated in such a way that the distance from the OLD exchange and the NEW exchange to the boundary will be equal.

So we can simply, for each subscriber grid element, find out which exchange is closer, and then assign the element to that exchange.

The resulting boundary is shown on the next page.

0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 1 :



location of existing exchange (OLD)



location of new exchange (NEW)

Solution of CASE STUDY 2

EXCHANGE BOUNDARIES

This case is a little more complicated than the previous case. The optimal boundary will now not be at equal distance from the two exchanges, but at equal cost.

As the two exchanges use different ways of connecting subscribers, and the range and cost of the cables are expressed in km, the first thing to do is to express ranges and costs in grid elements instead, so that our calculations will be facilitated.

Table 1

TRANSMISSION MEDIA FOR SUBSCRIBER NETWORK

Type	Cost	Cost / km	max. distance (km)	Exchange
0.4 mm	0	2.4	2.5	OLD
0.5 mm	0	2.8	4.0	OLD
RSU	1.3	0.4	-	NEW

Adjusted Table 1 :

TRANSMISSION MEDIA FOR SUBSCRIBER NETWORK

Type	Cost	Cost / 250 m	max. distance (250 m)	Exchange
0.4 mm	0	0.6	10	OLD
0.5 mm	0	0.7	16	OLD
RSU	1.3	0.1	-	NEW

We can now start to investigate the individual grid elements.

Between the exchanges, the following relations can be observed :

$$d_1 \times 0.6 = d_2 \times 0.1 + 1.3$$

$$d_1 + d_2 = 21 \quad \text{i.e. the distance between the exchanges}$$

from which we get

$$d_1 = 4.8$$

$$d_2 = 16.2$$

Therefore, in the area between the exchanges, the boundary should be between $d_1 = 4$ and $d_1 = 5$.

For the area which is not between the exchanges, the grid elements have to be investigated individually. Obviously, we do not investigate all grid elements, but only those which are of interest.

The resulting boundary is shown on the next page.

0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 2 :



location of existing exchange (OLD)



location of new exchange (NEW)

Solution of CASE STUDY 3

EXCHANGE LOCATION

For the simple assumptions valid for this case study, the optimal location for one new exchange is situated at the point where

- the number of subscribers to the left of the exchange equals the number of subscribers on the right of the exchange;
- the number of subscribers below the exchange equals the number of subscribers above the exchange.

Therefore, we calculate the number of subscribers in each row and column of the matrix, and then we can easily find the optimal row and column for the exchange.

Row	Sum	Accumulated sum		Column	Sum	Accumulated sum
1	488	488		2	865	865
2	692	1180		3	2377	3242
3	651	1831		4	3147	6389
4	1042	2873		5	3864	10253
5	2036	4909		6	4192	14445
6	1929	6838		7	6139	20584
7	2605	9443		8	4824	25408
8	1763	11206		9	3949	29357
9	1679	12885		10	2777	32134
10	2078	14963		11	8566	37700
11	1732	16695		12	3171	40871
12	1719	18414		13	2387	43258
13	2205	20619		14	1549	44807
14	2731	23350		15	1686	46393
15	2343	25693	← median	16	1017	47410
16	3001	28694		17	421	47831
17	2828	31522				
18	2576	34098				
19	2697	36795				
20	2503	39298				
21	2326	41624				
22	2133	43757				
23	1713	45470				
24	1229	46699				
25	879	47578				
26	238	47816				
27	15	47831				

The median of this distribution is : 47831 divided by 2 = 23915.5

Then we find the proper column by looking which of the accumulated row sums contains the value 23915.5; this happens to be row 15.

The same for the accumulated column sums gives us column 8.

The exchange should thus be located in grid element (8,15)

See next page.

0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 3 :  optimal location of the new exchange

Solution of CASE STUDY 4

INTRODUCTION OF A NEW EXCHANGE

The optimization is done in the following steps :

- 1 Assume initial boundary, see Figure 4
- 2 Find optimal location of new exchange as in Case Study 3
Result shown in Figure 4 / Phase 1
- 3 Optimize boundary between exchanges, as in Case study 1
Result shown in Figure 4 / Phase 2
- 4 Find optimal location of new exchange
Result shown in Figure 4 / Phase 2
- 5 Re-optimize boundary
Result shown in Figure 4 / Phase 3
- 6 Find optimal location of new exchange
Result shown in Figure 4 / Phase 3
- 7 Re-optimize boundary
This time there is no change in the boundary, which means that the optimal solution has been found.

0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 4 a :



location of existing exchange (OLD)



initial boundary of new exchange, and corresponding location



0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 4 a :



location of existing exchange (OLD)



new boundary of the exchange, and corresponding location



0	0	0	0	0	0	0	0	0	81	326	81	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	122	407	163	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	81	366	204	0	0	0	0	0	0
0	0	0	0	0	0	117	156	40	323	284	122	0	0	0	0	0	0
0	0	0	0	0	0	195	391	236	323	323	326	41	43	43	72	43	0
0	0	0	0	0	43	121	234	235	194	150	132	190	222	188	148	72	0
0	0	0	0	0	175	218	38	208	326	310	240	283	317	317	101	72	0
0	0	0	0	0	190	263	263	125	332	155	141	36	61	69	62	66	0
0	0	0	0	76	381	264	224	0	133	142	84	74	77	87	84	53	0
0	0	0	0	229	381	305	300	270	57	192	47	74	35	60	88	40	0
0	0	0	17	140	267	341	271	203	0	112	51	55	61	88	100	26	0
0	0	0	102	339	170	226	86	164	0	187	96	69	61	87	106	26	0
0	0	0	106	203	204	427	192	204	0	201	192	190	51	83	129	23	0
0	0	20	356	267	79	400	192	204	0	328	235	338	99	142	71	0	0
0	0	88	212	356	267	253	97	85	0	178	200	338	99	142	28	0	0
0	0	300	300	257	264	528	190	213	0	322	177	169	113	140	28	0	0
0	0	300	344	300	131	276	189	213	0	402	215	234	112	112	0	0	0
0	110	173	172	344	172	417	184	268	0	299	183	84	142	28	0	0	0
0	115	376	290	133	155	417	261	304	0	392	56	142	56	0	0	0	0
0	150	303	361	193	306	200	217	77	246	238	142	70	0	0	0	0	0
0	340	365	170	163	307	278	186	172	163	98	84	0	0	0	0	0	0
0	150	365	277	436	182	215	34	258	118	98	0	0	0	0	0	0	0
0	0	87	420	242	298	112	190	166	142	56	0	0	0	0	0	0	0
0	0	0	20	186	220	162	404	144	93	0	0	0	0	0	0	0	0
0	0	0	0	0	0	323	404	133	19	0	0	0	0	0	0	0	0
0	0	0	0	0	0	81	121	21	15	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	6	9	0	0	0	0	0	0	0	0

Figure 4 c :



location of existing exchange (OLD)



final boundary of the new exchange, and corresponding location

