Recommendation ITU-R P.2040-3

(08/2023)

P Series: Radiowave propagation

Effects of building materials and structures on radiowave propagation above about 100 MHz

Foreword

The role of the Radiocommunication Sector is to ensure the rational, equitable, efficient and economical use of the radio-frequency spectrum by all radiocommunication services, including satellite services, and carry out studies without limit of frequency range on the basis of which Recommendations are adopted.

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| ***Note***: *This ITU-R Recommendation was approved in English under the procedure detailed in Resolution ITU-R 1.* |

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RECOMMENDATION ITU-R P.2040-3

Effects of building materials and structures on radiowave   
propagation above about 100 MHz

(Question [ITU-R 211/3](https://www.itu.int/pub/R-QUE-SG03.211))

(2013-2015-2021-2023)

Scope

This Recommendation provides guidance on the effects of building materials and structures on radio-wave propagation above 100 MHz.

Keywords

Permittivity, conductivity

The ITU Radiocommunication Assembly,

considering

*a)* that electrical properties of materials and their structures strongly affect radiowave propagation;

*b)* that it is necessary to understand the losses of radiowaves caused by building materials and structures;

*c)* that there is a need to give guidance to engineers to avoid interference from outdoor to indoor and indoor to outdoor systems;

*d)* that there is a need to provide users with a unified source for computing effects of building materials and structures,

noting

*a)* that Recommendation [ITU-R P.526](https://www.itu.int/rec/R-REC-P.526/en) provides guidance on diffraction effects, including those due to building materials and structures;

*b)* that Recommendation [ITU-R P.527](https://www.itu.int/rec/R-REC-P.527/en) provides information on the electrical properties of the surface of the Earth;

*c)* that Recommendation [ITU-R P.679](https://www.itu.int/rec/R-REC-P.679/en) provides guidance on planning broadcasting-satellite systems;

*d)* that Recommendation [ITU-R P.1238](https://www.itu.int/rec/R-REC-P.1238/en) provides guidance on indoor propagation over the frequency range 900 MHz to 100 GHz;

*e)* that Recommendation [ITU-R P.1406](https://www.itu.int/rec/R-REC-P.1406/en) provides information on various aspects of propagation relating to terrestrial land mobile and broadcasting services in the VHF and UHF bands;

*f)* that Recommendation [ITU-R P.1407](https://www.itu.int/rec/R-REC-P.1407/en) provides information on various aspects of multi-path propagation;

*g)* that Recommendation [ITU-R P.1411](https://www.itu.int/rec/R-REC-P.1411/en) provides propagation methods for short paths in outdoor situations, in the frequency range from about 300 MHz to 100 GHz;

*h)* that Recommendation [ITU-R P.1812](https://www.itu.int/rec/R-REC-P.1812/en) provides a propagation prediction method for terrestrial point-to-area services in the frequency range 30 MHz to 6 GHz,

recommends

that the information and methods in Annex 1 should be used as a guide for the assessment of the effects of building material properties and structures on radiowave propagation, and in developing deterministic models of propagation involving the built environment.

Annex 1 describes basic principles, and provides expressions to evaluate reflection from and transmission through building materials and structures. It also includes a model for electrical properties as a function of frequency, and a table of parameters for relevant materials.

Examples of building-entry loss measurements may be found in Report [ITU-R P.2346](https://www.itu.int/pub/R-REP-P.2346).

Annex 1

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# 1 Introduction

This Annex provides guidance on the effects of building material electrical properties and structures on radio-wave propagation.

Section 2 describes fundamental principles concerning the interaction of radio waves with building materials, defines various parameters in use for these purposes, and gives basic expressions for reflection from and transmission through single material interfaces and single and multiple layer slabs, typical of building construction.

Section 3 defines a model for electrical properties, and a table of parameters for various building materials.

# 2 Basic principles and theory

Radio waves that interact with a building will produce losses that depend on the electrical properties of the building materials and material structure. In this section, theoretical effects of material electrical properties and structure on radio-wave propagation will be discussed.

## 2.1 Theory of material electrical properties

### 2.1.1 Introduction

This section describes the development of simple frequency-dependent formulae for the permittivity and conductivity of common building materials. The formulae are based on curve fitting to a number of published measurement results, mainly in the frequency range 1-100 GHz. The aim is to find a simple parameterization for use in indoor-outdoor ray trace modelling.

The characterization of the electrical properties of materials is presented in a number of different ways in the literature. These are described in § 2.1.2 in order that the measured data can be reduced to a common format.

### 2.1.2 Method

#### 2.1.2.1 Definitions of electrical constants

The following treatment deals only with non-ionized, non-magnetic materials, and throughout we therefore set the free charge density, ρ*f*, to zero and the permeability of the material, μ, to the permeability of free space μ0.

The fundamental quantities of interest are the electrical permittivity, ε, and the conductivity, σ. There are many ways of quantifying these parameters in the literature, so we first make explicit these different representations and the relations between them.

#### 2.1.2.2 Derivation

The starting point is the wave equation derived from Maxwell’s equations. Under the above assumptions, the wave equation for the electric field  is:

 (1)

where:

 : (vector) electric field intensity (V/m)

*Jf* : current density of free charges (A/m2)

ε : dielectric permittivity (F/m)

μ0 : permeability of free space (N/A2) = 4π × 10−7 by definition.

In a conductor,  is related to  through Ohm’s Law by:

 (2)

where:

σ : conductivity (S/m).

Combining equations (1) and (2) gives:

 (3)

Writing  in exponential notation:

 (4)

where:

 : value of  for *t* =  = 0 (V/m)

 : (vector) wave number (m−1) magnitude = 2π/λ where λ is the wavelength in m

ω : angular frequency (s−1) = 2π*f* where *f* is the frequency in s−1

: (vector) spatial distance (m).

and substituting in equation (3) gives:

 (5)

where:

*k* : magnitude of .

Equation (5) shows that the electric field intensity propagates as an attenuated sinusoidal wave.

#### 2.1.2.3 Non-conducting dielectric

In a non-conducting dielectric (σ = 0) the field is unattenuated and from equation (5) the velocity of propagation, *v* (= ω/*k*), is:

 (6)

ε is conventionally written in terms of the relative permittivity and the permittivity of free space:

(7)

where:

η: relative dielectric permittivity of the medium concerned

ε0: dielectric permittivity of free space = 8.854 × 10−12 (F/m).

Thus the velocity of propagation in a medium of relative permittivity η can be written:

(8)

where *c* is the velocity of light in free space (= ). In other words,  is the refractive index of the dielectric medium.

#### 2.1.2.4 Conducting dielectric

When σ ≠ 0, the wave attenuates as it propagates. It is convenient in this case to define a complex relative permittivity which may be derived as follows. Equation (5) can be rearranged, with the substitution , to give:

(9a)

Since equation (8) gives , this can be interpreted as a complex relative permittivity given by:

 (9b)

This shows that the relative permittivity defined for a pure dielectric, becomes the real part η' of the more general, complex relative permittivity η defined for a conducting dielectric.

There are no universally accepted symbols for these terms. In this Recommendation, relative permittivity is written in the form:

 (10)

where η' and η'' are the real and imaginary parts. Using equation (9b), the imaginary part is given by:

 (11)

Note that the sign of the imaginary part of η is arbitrary, and reflects the sign convention in equation (4). In practical units, equation (11) gives a conversion from η" to σ:

 (12)

Another formulation of the imaginary part of η is in terms of the *loss tangent*, defined as:

(13)

and so:

(14)

From equation (10) this gives:

(15)

and in practical units:

(16)

Another term sometimes encountered is the *Q* of the medium. This is defined as:

(17)

and is the ratio of the displacement current density  to the conduction current density *Jf*. For non-conductors, *Q* → ∞. From equation (14):

(18)

Yet another term encountered is the complex refractive index *n* which is defined to be . Writing *n* in terms of its real and imaginary parts:

 (19)

η', η" and σ are given from equations (10) and (12) by:

 (20)

#### 2.1.2.5 Attenuation rate

A conducting dielectric will attenuate electromagnetic waves as they propagate. To quantify this, substitute equation (5) in equation (4) and simplify using equation (14):

 (21)

where:

 : (vector) wave number (m−1) in free space.

The imaginary part under the square root sign leads to an exponential decrease of the electric field with distance:

(22)

In a practical calculation using complex variables, the attenuation distance, Δ, at which the field amplitude falls by 1/*e*, can be evaluated as:

 (23a)

where the function “Im” returns the imaginary part of its argument. Analytically it can be shown that:

 (23b)

which can be evaluated by calculating tan δ from  and σ and inverting to obtain cos δ. More direct evaluation is possible in the two limits of σ → 0 (dielectric limit) and σ → ∞ (good conductor limit). By choosing the appropriate approximation of the term under the square root sign in equation (21) these limits are:

 (24)

and:

 (25)

Equations (24) and (25) are accurate to about 3% for tan δ < 0.5 (dielectric) tan δ > 15 (conductor). Δ*conductor* is usually referred to as the “skin depth”.

For practical purposes the attenuation rate is a more useful quantity than the attenuation distance, and is related to it simply by

 (26)

where:

*A*: attenuation rate in dB/m (with Δ in m).

Substituting equations (24) and (25) in equation (26) and converting to practical units gives:

 (27a)

 (27b)

### 2.1.3 Frequency dependence of material properties

In the literature, the real part of the dielectric constant, η', is always given, but often the frequency is not specified. In practice for many materials, the value of η' is constant from DC up to around 5‑10 GHz after which it begins to fall with frequency.

The value of σ is usually a strong function of frequency in the band of interest, increasing with frequency. This may be one reason why the imaginary part of the dielectric constant, or the loss tangent, is often specified in the literature: equations (12) and (16) show that these terms remove a linear frequency dependence compared to the frequency dependence of σ.

For each material a simple regression model for the frequency dependence of σ can be obtained by fitting to measured values of σ at a number of frequencies.

### 2.1.4 Models of material properties frequency dependence

In order to derive the frequency dependence of material properties, the values of the electrical constants of the materials can be characterized in terms of the measurement frequency, real part (η') and imaginary part (η'') of the relative permittivity, loss tangent (tan δ) and conductivity (σ). Expressions in § 2.1.2.4 permit conversions between these quantities.

For the conductivity, there is usually statistically significant evidence for an increase with frequency. In this case the trend has been modelled using:



  (28)

where *c* and *d* are constants characterizing the material. This is a straight line on a log(σ)–log(*f*) graph. The trend line is the best fit to all available data.

For the relative permittivity one can assume similar frequency dependency:



 (29)



where *a* and *b* are constants characterizing the material. However, in almost all cases there is no evidence of a trend of relative permittivity with frequency. In these cases, a constant value can be used at all frequencies. The constant value is the mean of all the values plotted. Some examples are given in Table 3.

## 2.2 Effects of material structure on radiowave propagation

### 2.2.1 Plane wave reflection and transmission at a single planar interface

This section considers a plane wave incident upon a planar interface between two homogeneous and isotropic media of differing electric properties. The media extend sufficiently far from the interface such that the effect of any other interface is negligible. This may not be the case with typical building geometries. For example, propagation losses due to a wall may be influenced by multiple internal reflections. Methods for calculating reflection and transmission coefficients of single-layer and multi-layer slabs are given in § 2.2.2.

A plane wave is useful for analysis purposes, but the concept is largely theoretical. In practice a wave may approximate but not be exactly planar. The point is important here because a truly plane wave does not experience free-space (spreading) loss. The following methods take no account of free-space losses, only the effect of the media interface.

#### 2.2.1.1 Oblique incidence on a plane media interface

Figure 1 illustrates a sinusoidal plane wave incident obliquely to a plane interface separating two uniform non-magnetic dielectric media having relative permittivities η1 and η2. Values for η can be calculated from the real part of the permittivity, η', and conductivity, σ, using equations (10) and (11). Table 3 provides parameters from which these can be calculated as functions of frequency.

There are three important theorems for this case that follow from geometrical considerations.

1) The vector wave numbers of the reflected and transmitted (refracted) waves lie in the plane of incidence, i.e. the plane defined by wave number *ki* of the incident wave and the normal to the interface. This is taken to be the *x-z* plane in Fig. 1.

2) The angles of incidence and reflection are equal (both in Fig. 1).

3) The angle of refraction, is related to the angle of incidence by Snell’s law.



 (30)



where and are the respective wave speeds in the two media, and η1 and η2 represent the complex relative permittivities of the two media.

These theorems ensure that the exponential space-time factors, , for the three waves (, respectively) are identical at all points in the interface.

Figure 1

Reflection and refraction of plane waves at plane interface

Engineering drawing

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Two polarizations of the incident wave are shown in Fig. 1.

a) On the left the incident electric vector *Ei* is perpendicular to the plane of incidence.   
This is known as transverse electric (TE) polarisation. Other terms are perpendicular polarisation, s-polarisation, and σ-polarisation.

b) On the right the incident electric vector *Ei* is parallel to the plane of incidence.   
This is known as transverse magnetic (TM) polarisation. Other terms are parallel polarisation, p-polarization, and π-polarization.

In the following descriptions, polarization will be designated by TE or TM.

An arbitrarily or circularly polarised wave can be resolved into its TE and TM components for calculation purposes, which can then be re-combined.

E-field reflection and transmission coefficients are defined as the ratios of reflected and transmitted (refracted) vectors respectively to the corresponding incident vector as they exist at the interface. In general such coefficients are complex. The following expressions take no account of free-space or other losses prior or subsequent to the interaction of a wave with the interface.

The requirement that electric and magnetic vectors are continuous in the plane of the interface give the following expressions for electric field coefficients. Reflection and transmission coefficients are denoted by *R* and *T* respectively. The subscripts indicate the vectors concerned, and whether the polarization is TE or TM. Each of equations (31a) to (32b) are in two parts, according to whether total internal reflection occurs. Total internal reflection is only possible when a wave is incident upon a medium with lower refractive index.

E-field reflection coefficient for TE polarisation:

 (31a)

E-field reflection coefficient for TM polarisation:

 (31b)

E-field transmission coefficient for TE polarisation:

 (32a)

E-field transmission coefficient for TM polarisation:

 (32b)

where η1 and η2 are the complex relative permittivities of medium 1 and 2 respectively. These can be evaluated using equation (9b) with values of η' and σ obtained from § 3 and Table 3.

The cosθ2 terms in equations (31a) to (32b) can be evaluated in terms of θ1 using equation (30) as:

 (33)

At θ1 = 0 the incidence plane is not uniquely defined. In this case all directions of propagation are normal to the interface, and the coefficient amplitudes from the expression for each polarisation is the same. In the case of reflection there is an apparent sign change. This arises purely from how the polarizations are defined; it is not a physical discontinuity.

#### 2.2.1.2 Calculation examples

Figure 2 gives examples of reflection and transmission coefficient amplitudes for a wave in air incident upon concrete at 1 GHz calculated over a range of incidence angles for both polarizations using equations (31a) to (32b), taking the properties of concrete from Table 3.

FIGURE 2

Reflection and transmission coefficients for air/concrete interface at 1 GHz

Chart, line chart

Description automatically generated

#### 2.2.1.3 Substitutions available in coefficient values

It can be useful to note the following substitutions for E-vector coefficients, where the subscripts denote the medium, 1 or 2, in which the wave is incident on an interface:

a) For either polarisation, , and thus 

b) For either polarisation, , where according to a) *R* can be either *R*1 or *R*2.

#### 2.2.1.4 Coefficients for power flux-densities

Coefficients for power flux densities can be obtained from the E-vector coefficients:

 (34a)

 (34b)

 (35a)

 (35b)

The change in signal level in decibels due to reflection or transmission is thus given by  or  where *RS* and *TS* stand for either reflection or transmission S-vector coefficient in equations (34a) to (35b).

Conservation of energy at the media interface requires that for a given incident wavefront area, the sum of the reflected and transmitted power flux equals the incident power flux. To illustrate this, account must be taken of the change in wavefront width upon refraction. For either polarization:

 (36)

where  adjusts for the change in wavefront width.

#### 2.2.1.5 Simplified expressions for incident wave in air

When medium 1 is air, equations (31a) to (32b) can be simplified to:

 (37a)

 (37b)

 (38a)

 (38b)

where θ is the angle of incidence and η is the relative permittivity of the medium upon which the wave is incident.

Total internal reflection at the interface is not possible in equations (37a) to (38b) since it can be assumed that the wave is incident upon a medium with a higher refractive index than air.

### 2.2.2 Plane wave reflection and transmission for a single- or multi-layer slab

#### 2.2.2.1 General method for a multi-layer slab

Figure 3 illustrates a plane wave incident upon a slab consisting of *N* layers, each with smooth, planar and parallel surfaces, where *N* can be 1 or more. The relative permittivity of layer *n* is η*n*, and its width *dn* metres. It is assumed that the slab is in air, and for calculation purposes this is designated as layers 0 and *N* + 1, with relative permittivity 1 and width 0.

FIGURE 3

Plane wave incident on single- or multi-layer slab

A diagram of mathematical equations

Description automatically generated

The incidence and reflection angles are θ0, and the wave will emerge from layer *N* at θ*N*+1 = θ0.   
The direction of propagation in layer *n* is θ*n*. A complete ray path through the layers is not shown in Fig. 3. For a single incident ray *Si* the departing rays *Sr* and *St* are spatially distributed due to multiple internal reflections in the layers.

Reflection coefficient for the slab can be calculated by applying equation (39) representing the reflection coefficient at the interface separating the layer and the layer for , , , ……, with setting .

(39)

In equation (39), and are the Fresnel reflection coefficient at the interface.

(40a)

(40b)

where:

(41a)

(41b)

(41c)

and λ is the free-space wavelength in metres.

Having evaluated equation (39) for, in order, *n* = *N* to *n* = 0, the reflection coefficient and the transmission coefficient are given by:

(42a)

(42b)

where the subscripts *TE* and *TM* denote transverse-electric and transverse-magnetic incident polarization respectively.

Attachment 1 to this Annex provides an alternative formulation for the multi-layer slab method.

#### 2.2.2.2 Simplified method for a single-layer slab

For a slab consisting of a single layer, that is, for which *N* = 1, and the foregoing method can be simplified to:

         (Reflection coefficient) (43a)

      (Transmission coefficient) (43b)

where:

 (44)

*d* is the thickness of the building material, ƞ is the complex relative permittivity, and  represents *ReTE* or *ReTM*, as given by equations (37a) or (37b) respectively, depending on the polarization of the incident E-field.

#### 2.2.2.3 Calculation examples

Figures 4 to 7 show examples of results from equation (42a) for a single concrete slab at 1 GHz with four incidence angles. The same results may be obtained from equations (43a) and (43b). The electrical properties for concrete are taken from Table 3.

FIGURE 4

Reflection coefficient for a concrete slab at 1 GHz, TE polarisation

Chart, line chart

Description automatically generated

FIGURE 5

Reflection coefficient for a concrete slab at 1 GHz, TM polarisation

Chart, line chart

Description automatically generated

FIGURE 6

Transmission coefficient for a concrete slab at 1 GHz, TE polarisation

Chart, line chart

Description automatically generated

FIGURE 7

Transmission coefficient for a concrete slab at 1 GHz, TM polarisation

Chart, line chart

Description automatically generated

It will be noted in Figs 5 and 7 that the coefficients for TM polarization for 85 degrees incidence have anomalous values compared to the ordering of the other three angles. This is the effect of the minimum in reflection coefficient visible in Fig. 2 for TM polarization, known as the pseudo‑Brewster angle.

### 2.2.3 Waveguide propagation in buildings

#### 2.2.3.1 Theory on frequency characteristics of attenuation constant in waveguide

A waveguide may comprise of a hollow space surrounded by lossy dielectric materials. In the case of a building structure, a corridor, underground mall, or tunnel can be considered as a waveguide. The radiowave power that propagates in a waveguide is attenuated according to the distance. It is well known that a waveguide has frequency characteristics such as the cut-off frequency that varies according to the shape. In this section, a formula is presented to derive the attenuation constant for the frequency characteristics in a waveguide.

The cross-section of a square waveguide structure is shown in Fig. 8. In this case, the intrinsic constants of the lossy dielectric material are different for the sidewalls and for the ceiling and the floor.

Figure 8

Cross-section of waveguide and material constants

A picture containing text, dark, lit

Description automatically generated

In Fig. 8, *a* is the width and *b* is the height of the waveguide (m), *h*1 and *h*2 are the root mean square roughness of the Gaussian distribution of the surface level, and θ is the tilt of the root mean square (rad). The complex permittivity values for materials ε*ri*\* are calculated as follows.

 (45)

where ε*ri* is the relative dielectric constant and σ*i* is the conductivity. The quantity ε*ri*″ is the loss tangent of the materials, ω is the angular frequency and 0 is the permittivity of free space.

The basic attenuation constant is formulated as follows.

 (dB/m) (46)

Kh and Kv are constant values that are dependent on the section shape. The constant values dependent on the section shape are given in Table 1.

TABLE 1

Constant values for various cross-section shapes

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Shape | Circle | Ellipse | Square | Arch-backed |
| Kh | 5.09 | 4.45 | 4.34 | 5.13 |
| Kv | 5.09 | 4.40 | 4.34 | 5.09 |

The formulas mentioned above are valid based on equation (47) representing the condition of constraint.

                (m) (47)

Unique characteristics in square shape case

The attenuation constant due to roughness, which is regarded as local variations in the level of the surface relative to the mean level of the surface of a wall, is given by:

                (dB/m) (48)

The attenuation constant due to the wall tilt is given by:

                (dB/m) (49)

Therefore, the total attenuation constant in a square shape case is the sum of the above losses:

                (dB/m) (50)

#### 2.2.3.2 Applicability of waveguide theory

The waveguide theory shows good agreement with the measured propagation characteristics in the corridor in the frequency range of 200 MHz to 12 GHz in case there is no pedestrian traffic in the corridor.

Effect of pedestrian traffic on waveguide

Figure 9 shows a comparison of the theoretical and measured attenuation constant values during the day (when pedestrian traffic is present), and during the night (when the corridor is empty). Theoretical values are calculated based on the parameters given in Table 2.

TABLE 2

Parameters used in underground calculation

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | Width (m) | Height (m) | Tilt (degrees) | Roughness | | Material constant | | | |
| *h*1 | *h*2 | ε*r*1 | ε*r*2 | σ | σ |
| Underground | 6.4 | 3.0 | 0.35 | 0.4 | 0.2 | 15 | 10 | 0.5 | 0.1 |

Figure 9

Attenuation constant comparison for day and night

Diagram

Description automatically generated

Figure 9 shows that the waveguide theory is applicable to realistic propagation characteristics in the corridor in the frequency range of 200 MHz to 12 GHz at night. However, the waveguide theory is not applicable to realistic propagation characteristics during daytime, because the received power is attenuated by pedestrian traffic.

Therefore, the waveguide theory is applicable to situations where there is no influence from shadowing obstacles.

## 2.3 Theory and results for frequency selective surface materials

### 2.3.1 Frequency selective surfaces

The power of scattering waves varies with roughness of surfaces. In this section, a theory for calculating scattered fields from the surface having round convexity array is described. First, for parameterizing the roughness of the surface, the rough surface is defined by using a round convexity array formed by locating circular cylinders periodically.

Second, the reflection coefficient of the scattered fields is defined by using the lattice sums characterizing a periodic arrangement of scatterers and the T-matrix for a circular cylinder array. Third, a numerical result that shows the frequency-depending characteristic of the reflection from the round convexity’s surface is shown. Finally, a measurement result is shown to explain that the power of scattering waves varies with the frequency of an incident wave when there is a round convexity array on the surface of a building.

### 2.3.2 Theory for wave propagation around the surface of round convexity array

By making periodical round convexity array on a surface of a building, as shown in Fig. 10, reflection/scattering waves can be controlled larger than those from the flat surface. The theory to calculate the scattered waves from the periodic arrays of circular cylinders can be used to define the propagation waves around a convexity array of a surface.

FIGURE 10

The surface of round convexity array

Shape, rectangle

Description automatically generated

FIGURE 11

Geometry of a periodic array of circular cylinders

A picture containing logo

Description automatically generated

When the identical circular cylinders are situated periodically in an *x* axis as shown in Fig. 11, the power reflection coefficient *R* for the **-th propagating mode with *k* > 0 is given as:

(51)

where *k*0 = 20, 0 is the wavelength of the waves indenting in angle ϕ*in*. In equation (51),  and are obtained as follows:

(52)

(53)

where is the unit matrix, , and *h* is the periodic space between each round convex. is a square matrix whose elements are defined in terms of the following lattice sums:

(54)

where is the *m*-th order Hankel function of the first kind. is the T-matrix for the scattered fields and is given by the following diagonal matrix for the incident electric field and the incident magnetic field , respectively.

(55a)

(55b)

where is the relative permittivity of the dielectric cylinder, is the *m*-th orderBessel function, the prime demotes the derivative with respect to the argument, and denotes the Kronecker’s delta. denotes a column vector whose elements represent unknown amplitudes of the incident field.

(56)

### 2.3.3 Calculation results

The calculation result of a power reflection coefficient is shown in Fig. 12. The result is calculated by using equation (51) in the case that the electric field is transmitted in the angle ϕ*in*= 90° to the dielectric round convexities whose diameter and permittivity are *d*= 0.3*h* and ε*r* = 2.0, respectively. In the result, there is the frequency band that the incident wave is reflected almost completely by the surface even if its material is a lossless dielectric substance.

FIGURE 12

Power reflection coefficient *R*0 as functions of the normalized wavelength *h*/λ0  
at normal incidence electric field

A picture containing graphical user interface

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### 2.3.4 Measurement

The measurements of the scattered waves from the building having the round convexity array were carried out. Figure 13 shows the comparison of the scattered waves from the building between the flat surface and the surface with round convexity arrays. The scattered waves from the building were measured in various reflected angles ϕ*r* between 30° to 90°, when the electric field is transmitted in the angle ϕ*in*. The incident angle and reflection angle are defined as shown in Fig. 14.

FIGURE 13

Geometry of a periodic array of circular cylinders

Diagram

Description automatically generated

FIGURE 14

A plane figure of the compositional diagram   
for measurements

A picture containing diagram

Description automatically generated

The measurement results show that the power of the scattered field from the surface having a round convexity array becomes larger than that from the flat surface, and can be controlled by the period between and diameter of each round convexity. Note that the relative permittivity and the conductivity of the building material were estimated as ε*r*= 6.0 and σ = 0.1 S/m, respectively.

# 3 Compilations of electrical properties of materials

Representative data on material electrical properties can be hard to find, as characteristics are expressed using different combination of parameters, and the relative permittivity may be quoted at frequencies that are not close to that of interest. A table of representative material properties has therefore been compiled using the curve-fitting approach described in § 2.1.4.

Data from eight sets of material electrical properties (a total of more than 90 separate characteristics) given in the open literature have been collated, converted to a standard format and grouped into material categories.

For each group, simple expressions for the frequency-dependent values of the real part of the relative permittivity, η', and the conductivity, σ, were derived. These are:

(57)

and:

(58)

where *f* is frequency in GHz and σ is in S/m. (η' is dimensionless.) The values of *a*, *b*, *c* and *d* are given in Table 3. Where the value of *b* or *d* is zero the corresponding value of  or σ is *a* or *c* respectively, and independent of frequency.

If required, the imaginary part of the relative permittivity η" can be obtained from the conductivity and frequency:

 (59)

Parameters for air, metal and three conditions of ground are included in Table 3 for completeness.

TABLE 3

Material properties

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Material class | Real part of relative permittivity | | Conductivity S/m | | Frequency range |
|  | *a* | *b* | *c* | *d* | GHz |
| Vacuum (≈ air) | 1 | 0 | 0 | 0 | 0.001-100 |
| Concrete | 5.24 | 0 | 0.0462 | 0.7822 | 1-100 |
| Brick | 3.91 | 0 | 0.0238 | 0.16 | 1-40 |
| Plasterboard | 2.73 | 0 | 0.0085 | 0.9395 | 1-100 |
| Wood | 1.99 | 0 | 0.0047 | 1.0718 | 0.001-100 |
| Glass | 6.31 | 0 | 0.0036 | 1.3394 | 0.1-100 |
| Glass | 5.79 | 0 | 0.0004 | 1.658 | 220-450 |
| Ceiling board | 1.48 | 0 | 0.0011 | 1.0750 | 1-100 |
| Ceiling board | 1.52 | 0 | 0.0029 | 1.029 | 220-450 |
| Chipboard | 2.58 | 0 | 0.0217 | 0.7800 | 1-100 |
| Plywood | 2.71 | 0 | 0.33 | 0 | 1-40 |
| Marble | 7.074 | 0 | 0.0055 | 0.9262 | 1-60 |
| Floorboard | 3.66 | 0 | 0.0044 | 1.3515 | 50-100 |
| Metal | 1 | 0 | 107 | 0 | 1-100 |
| Very dry ground | 3 | 0 | 0.00015 | 2.52 | 1-10 only |
| Medium dry ground | 15 | −0.1 | 0.035 | 1.63 | 1-10 only |
| Wet ground | 30 | −0.4 | 0.15 | 1.30 | 1-10 only |

The frequency ranges given in Table 3 are not hard limits but are indicative of the measurements used to derive the models. The exceptions are the three ground types where the 1‑10 GHz frequency limits must not be exceeded. Typical values of relative permittivity and conductivity for different types of ground, as function of frequency in the range 0.01 MHz to 100 GHz, are given in Recommendation ITU-R [P.527](https://www.itu.int/rec/R-REC-P.527/en).

The loss tangents of all the dielectric materials in Table 3 are less than 0.5 over the frequency ranges specified. The dielectric limit approximations for the attenuation rate given in equations (24) and (27) can therefore be used to estimate the attenuation of an electromagnetic wave through the materials.

Attachment 1

to Annex 1  
  
Alternative method to obtain reflection and transmission coefficients   
for building materials represented by *N* dielectric slabs   
based on ABCD matrix formulation

An alternative formulation of the method in § 2.2.2.1 is given below to obtain the reflection, *R*, and transmission, *T*, coefficients for a building material represented by *N* dielectric slabs based on the ABCD matrix formulation, as illustrated in Fig. 5. The regions on both sides of the building material are assumed to be free space. This alternative method produces exactly the same results as that given in § 2.2.2.1.

 (60a)

(60b)

where *A*, *B* and *C* are the elements of the ABCD matrix given, using matrix multiplication, by:

 (61a)

where:

(61b)

(61c)

(61d)

(61e)

 (61f)

 (61g)

 (61h)

λ is the free-space wavelength, *k*0 is the free‑space wave number, η*m* and *km* are the complex relative permittivity and wave number in the *m*‑th slab, β*m* is the propagation constant in the direction perpendicular to the slab plane, and *dm* is the width of the *m*‑th slab.

The wave impedances *Z* are given, according to incidence polarization, by:

TE polarisation (62a)

TM polarisation (62b)

where:

(63a)

(63b)

(63c)

The wave impedance in equation (63c) is the free space impedance, and it can be obtained from equations (62a) and (62b) through setting .