

# A MEASUREMENT DATA-BASED INVESTIGATION OF FADING MODELING FOR INDOOR THz WIRELESS SYSTEMS

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**Abstract** – The terahertz (THz) band offers a vast amount of still unallocated bandwidth, which makes it a promising enabler for future sixth generation wireless systems. The high frequencies of the THz band lead to a significantly reduced multipath richness of the propagating THz signals. However, there are still paths that can carry a significant amount of power. As a result, the THz band small-scale fading characterization is of particular interest and the appropriate stochastic distributions that best fit the empirical channels need to be identified. This work investigates the suitability of the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions to adequately model the small-scale fading statistics of the channel gain measurements of various Line-of-Sight (LoS) and Non-Line-of-Sight (NLoS) indoor THz wireless links. The fitting accuracy of the examined analytical distributions is validated by means of the Kolmogorov-Smirnov test, the Kullback-Leibler divergence, the logarithmic Kolmogorov-Smirnov test and the root-mean-square-error. Also, the ergodic capacity based on the channel gain measurements as well as on the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions is presented. Based on the fitting accuracy metrics the Rice and  $\alpha$ - $\mu$  yield the best fit for the LoS and NLoS links, respectively. The Nakagami-m does not fit the empirical distributions for any of the presented links. Furthermore, insights are provided for the ranges of the extracted values of the analytical distributions in LoS and NLoS transmission conditions.

**Keywords** –  $\alpha$ - $\mu$ , experimental results, fitting, Nakagami-m distribution, Rice distribution, small-scale fading, THz wireless communications

## 1. INTRODUCTION

The terahertz (THz) band spans the vast frequency range of 0.1–10 THz. It offers a contiguous bandwidth of more than 20 gigahertz (GHz) [1, 2], which makes it a promising enabler for the sixth Generation (6G) wireless technologies. From the beginning of the previous decade, both the academics and industry have focused their efforts in developing outdoor and especially indoor THz wireless systems [2–5]. Especially for indoor THz wireless communications, major standardization bodies are in the process of publishing spectrum allocation standards and regulations. More specifically, such published standards are the Institute of Electrical and Electronics Engineers (IEEE) Standard (Std.) 802.15.3d-2017 [6], International Telecommunication Union (ITU)-T SM. 2353 report 2015 and 2016 [7], European Telecommunications Standards Institute (ETSI) millimeter Wave Transmission (mWT) [8], Federal Communications Commission (FCC): American spectrum regulations [9] and the European Communications Commission (ECC): Europe spectrum relations [10].

The high frequencies of the THz band lead to severe propagation losses for the transmitted signals. Hence, the wireless THz transmissions heavily depend on the Line-of-Sight (LoS) component of the received signal [11–13]. In this direction, the THz channel is often modeled by taking into consideration only the large scale propagation phenomena, which are the

deterministic path-loss and shadowing [11, 12, 14–20]. In the THz band the deterministic path-loss is given as the product of the free space and molecular absorption loss [11]. The molecular absorption loss is modeled with the aid of spectroscopic databases, which contain the various molecular absorption lines needed [3]. However, this is a tedious procedure and several simplified molecular absorption loss models have been developed spanning different ranges of the THz band. Such models are [11], [15] and [16], which were employed in the ranges of 100–450 GHz, 200–450 GHz and 275–400 GHz, respectively. In these models the THz channel was assumed to consist of a single LoS coefficient, which was expressed as the product of the free space and the molecular absorption loss. In [12] and [14], LoS and Non-Line-of-sight (NLoS) channel measurements for indoor wireless links operating at 28 GHz and 140 GHz were performed. This work made use of the measured received signal power of the multipath components in order to model the millimeter wave (mmWave) and THz channels as the deterministic sum (in dB) of an exponential path-loss and a log-normal shadowing distribution. In more detail, in [12] and [14], the exponential path-loss parameter and the variance of shadowing were extracted by employing the received signal powers of the measured links. In [18] and [20], a single path theoretical THz channel model for nano-scale machine communications within vegetation was developed, where the receiver (RX) was assumed to detect signals only from the LoS direction. The channel was assumed to be

composed of two coefficients, namely the path-loss and the log-normal shadowing.

The THz wireless transmissions heavily rely on the existence of the LoS component of the propagating signal. Despite this fact, there are aerosols in the atmospheric medium, as well as objects laid in the propagation environment that can act as scatterers [12, 14] and [21]. This suggests that there are NLoS THz multipath components with significant power capable of being detected by the RX. The presence of multipath components with different received power levels, angles of arrival and delay times means that the received signal power at the RX can have deep and time varying fast fades [22]. According to [22], these phenomena are parts of the stochastic small-scale fading.

Scanning the technical literature, several pieces of work can be identified that conduct theoretical as well as experimental THz channel modeling by taking into account the small-scale fading phenomena [3, 4, 12, 14, 17, 23–30]. In [3], it was observed that, according to THz channel measurements the small-scale fading can be modeled by means of Rice, Nakagami-m and Rayleigh distributions. This remark was employed in [3] and [27], where the more generic  $\alpha$ - $\mu$  distribution was used to model the small-scale fading and evaluate the performance under different levels of transceivers' antenna misalignment, hardware impairments and various levels of fading severity, for a backhaul THz wireless system. In [30] and [23], a two dimensional geometric channel model for indoor THz communications was developed. The resulting model led to the creation of a parametric multipath Rice fading channel model. In [29], an indoor stochastic THz channel model was presented, where the small-scale fading attenuation factor was expressed as a Rayleigh or Nakagami-m distribution under NLoS conditions and as a Rice or Nakagami-m in LoS. This model was validated by performing experimental measurements in an anechoic chamber.

The authors in [24], exploited the LoS and NLoS links, which were measured in the premises of a shopping mall. The measurements were used to derive a suitable small-scale fading distribution for wireless THz systems operating at 140 GHz. This work concludes that, at least for the used links the distribution that most accurately fits the data is the Weibull in LoS and Nakagami-m in NLoS conditions. The fitting accuracy of the exploited distributions was evaluated in terms of the Kolmogorov-Smirnov (KS) test. In [4], a small-scale fading distribution expressed as the sum of individual Gamma distributions was developed for THz wireless systems operating in the range of 240–300 GHz. The suitability of the proposed distribution was evaluated by fitting it to channel measurements. The used fitting accuracy metrics were the KS, Kullback Leibler (KL) divergence test and the weighted relative mean difference error metric. In [17], a measurement-based

THz channel model for LoS and NLoS links operating in the range of 126–156 GHz was proposed. This model relied on the extended Saleh-Valenzuela channel model.

In [25], a theoretical small-scale fading channel model for a holographic multiple-input-multiple-output system operating in the mmWave or the THz band was developed. The small-scale fading was modeled as a zero-mean spatially stationary and correlated Gaussian scalar random field. In [28], the suitability of the  $\alpha$ - $\mu$  distribution to describe the small-scale fading statistics of indoor LoS and NLoS links operating at 142 GHz was investigated. The fitting accuracy of examined distribution to the channel measurements was evaluated in terms of the KS test. Also, the ergodic capacity was calculated for indicative values of the parameters  $\alpha$  and  $\mu$ . In [26], the fitting accuracy of  $\alpha$ - $\mu$ , Rice, Rayleigh, log-normal and Nakagami-m distributions to indoor THz channel measurements was investigated. In more detail, the employed indoor LoS and NLoS measurements took place in three different locations and time periods. The fitting accuracy of the analytical distributions was evaluated in terms of the KS and the KL divergence tests. By making use of the metrics it was concluded that, the small-scale fading statistics of all the examined links are best described by means of the  $\alpha$ - $\mu$  distribution.

In this work the LoS and NLoS THz links of an indoor measurement environment were exploited. The measurements were conducted in May 2021 within an entrance hall of Aalto university in Finland. For each of the presented links multiple channel gain measurements were recorded. These channel gain measurements are employed in order to investigate the suitability of the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions to adequately describe the small-scale fading statistics of THz wireless links. To study the small-scale fading characteristics of a link, a preprocessing and an increment of channel realizations method must be first applied to the channel gain measurements. By employing the resulting channel gain measurements realizations of each link, the analytical expressions of the Probability Density Function (PDF) and Cumulative Density Function (CDF) of  $\alpha$ - $\mu$ , Rice and Nakagami-m are fitted to the corresponding empirical distributions. The parameters of the analytical distributions are obtained by fitting them to the empirical ones of the channel gain for each of the presented links. To achieve this non-linear regression machine learning is used. Furthermore, the Ergodic Capacity (EC) obtained by means of  $\alpha$ - $\mu$ , Rice and Nakagami-m as well as the EC based on the empirical data of the links are presented. The fitting accuracy metrics and the EC expressions provide useful insights for the purposes of indoor THz small-scale fading statistics. Specifically, from the fitting accuracy metrics it is revealed that in LoS transmission conditions the Rice distribution should be used, whereas in NLoS the  $\alpha$ - $\mu$ . Finally, the metrics provide insights about the values and ranges of the employed analytical distribution parameters in LoS and NLoS transmission scenarios.

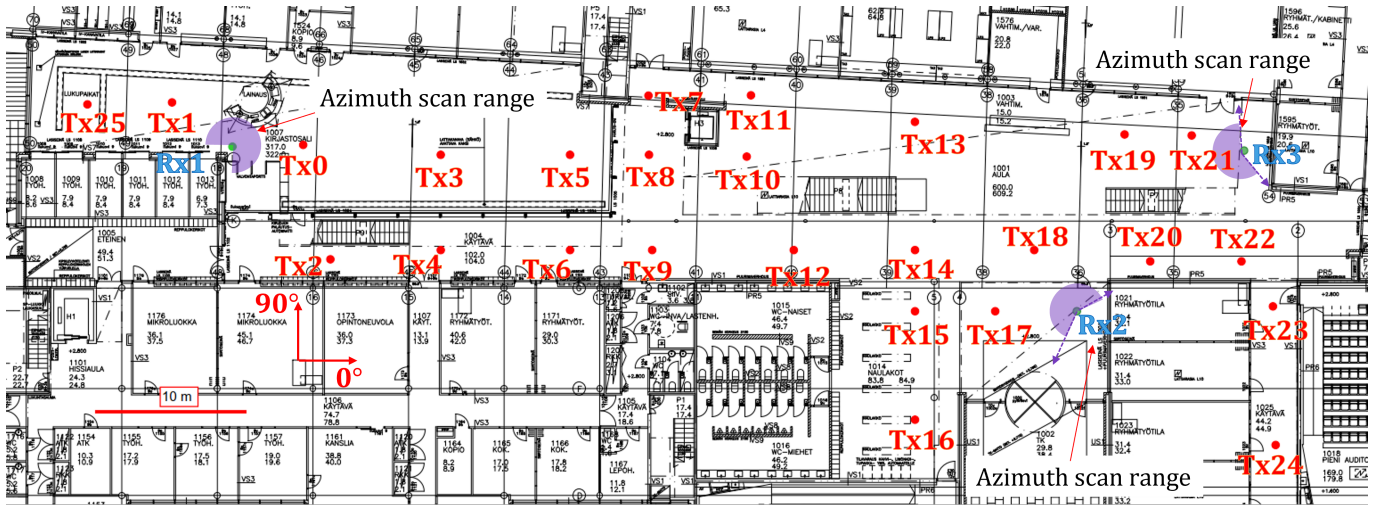


Fig. 1 – Top view of the measurement environment

The remainder of this paper is organized as follows. Section 2 briefly presents the experimental measurements setup. Section 3.1 shows the preprocessing method applied to the channel gain measurements of each link. Section 3.2 presents the method for increasing the channel realizations of a link. Section 3.3 shortly revisits the fundamentals of the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions. Section 3.4 briefly presents the employed fitting accuracy metrics. Section 4 presents the EC expressions calculated by employing the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions. Section 5 presents for each link the calculated parameters of the employed distributions, the results of the fitting accuracy metrics, the achieved EC by the channel measurements as well as the EC obtained by means of the investigated distributions. Finally, Section 6 provides the closing remarks of this work.

## 2. EXPERIMENTAL SETUP

The THz channel measurements that are employed in this work were conducted in an indoor environment within the premises of the Aalto University in Finland. Fig. 1 illustrates a top view of the building, where a transmitter (TX) and a RX pair uniquely identify a measured link. All the measurements were performed in an indoor environment, hence a link could be in LoS conditions or if a link was blocked by obstacles or the transceivers were placed in different rooms, it was in NLoS conditions. During the measurement of each link the TX and the RX were static, while there were not any moving people or objects.

The specifications of the THz channel sounding system utilized in this work can be found in [12, 14, 31, 32]. Finally, it should be noted that, the operational frequency was set equal to 142 GHz and the selected bandwidth was set equal to 4 GHz.

## 3. FADING CHARACTERIZATION

The following sections present the methodology used to obtain the channel gains of the measured paths for each of the links defined by the TXs and RX<sub>2</sub> and RX<sub>3</sub>. It should be noted that the links defined by the TXs and RX<sub>1</sub> are not used in this work. The suitability of the  $\alpha$ - $\mu$  distribution to describe the small-scale fading channel amplitude of those links was investigated in [31]. Meanwhile, Section 3.1 presents the preprocessing method applied to obtain the channel gain of the measured paths of each link. In Section 3.2, the technique to increase the channel realizations of a link by introducing a random uniform phase to the measured amplitudes will be shown. Then, Section 3.3, briefly revisits the PDF, CDF and the corresponding parameters definitions of the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions. Finally, Section 3.4, provides the definitions of the employed fitting accuracy metrics, which namely are the KS, lgKS, KL and RMSE.

### 3.1 Preprocessing

The channel of a Radio Frequency (RF) wireless link is composed of the product of two coefficients, one deterministic and one stochastic. The deterministic part of the channel encapsulates the large-scale fading effects of the propagation, i.e. the path-loss. In more detail, the large-scale fading describes the time-invariant phenomena of the signal propagation. The stochastic channel coefficient expresses the small-scale fading characteristics of the channel, which are time and frequency dependent. Furthermore, the small-scale fading can lead to deep unpredicted fades to the received signal power. Hence, in order to perform small-scale fading characterization of the channel the deterministic coefficient must be eliminated.

The channel sounding performed in the building shown in Fig. 1, provides Power Angular Delay Profiles (PADPs) for each of the measured TX-RX<sub>2</sub> and TX-RX<sub>3</sub> links. The

PADPs for each link are expressed as a set of propagation paths

$$\text{PADP}(\phi, t) = \sum_{i=1}^I G P_i \delta(\phi - \phi_i) \delta(t - t_i), \quad (1)$$

where  $\phi_i$ ,  $P_i$  and  $t_i$  stand for the azimuth angle at the RX, the propagation delay gain and time of the  $i$ -th propagation path, respectively. The parameter  $G$  known as the broadside angle, denotes the combined gains of the TX and RX antennas, while  $I$  and  $\delta(\cdot)$  are the total number of multipath components of a link and the Dirac delta function, respectively. Then, in order to eliminate the deterministic phenomenon of path-loss, the link path gain measurements are normalized to unity as

$$\zeta_i^2 = \frac{P_i}{\bar{p}}, \quad (2)$$

where

$$\bar{p} = \frac{\sum_{i=1}^I P_i}{I}. \quad (3)$$

### 3.2 Incrementing link channel realizations

The THz band experiences much higher propagation losses in comparison with the mmWave and Ultra-High-Frequency (UHF) bands [11, 12, 33]. In more detail, the THz free space attenuation losses even at a communication distance of one meter and an operational frequency of 140 GHz can be in the excess of 75 dB [5, 11, 14]. Also, the atmospheric water vapor causes severe attenuation to the propagating THz signal [5, 11]. Furthermore, the wavelength of the transmitted THz electromagnetic wave is much smaller compared to the size of obstacles laid within the propagation path [13]. Hence, the reflection and refraction losses of the THz band are significantly stronger in comparison with the lower frequency bands [33–36]. This leads in the reduction of the number of dominant rays, since the THz signal power becomes drastically weaker when it is reflected or scattered two or more times [13, 34]. Accordingly, the ability of the THz electromagnetic wave to propagate through blockages is nearly lost due to the severe penetration loss. As a result, the capability of the THz signals to diffract around obstacles is significantly reduced. For example, in [36] 45.6 dB of attenuation were observed at 310 GHz when the transmission was obstructed by a human hand. Based on the aforementioned remarks, it is clear that the THz band yields non-rich multipath environments, when compared to lower frequency bands such as the mmWave. Despite this fact, there are surfaces that can act as scatterers in the THz band [12, 14, 17, 23, 33]. This leads to the existence of reflected NLoS multipath components carrying a significant amount of power capable of being detected by the RX. Nevertheless, the number of measured multi-path components, utilized in our analysis, is still not sufficient to perform small-scale fading statistics analysis for a THz channel.

To overcome this limitation, different realizations of the transfer function can be realized by changing the phases of the multipath components [37, 38]. The phases are assumed to be stochastic and given by a uniform distribution in the interval  $(0, 2\pi)$ . Then, the channel coefficient of a Single-Input-Single-Output (SISO) system can be obtained as [31, 37, 38]

$$h = \sum_{i=1} \zeta_i \exp(-j2\pi f t_i) \exp(j\psi_i), \quad (4)$$

where  $\psi_i \sim U(0, 2\pi)$  represents the random phase of the  $i$ -th multipath component and  $f$  stands for the frequency. Moreover, by assuming that the amplitude of the channel coefficients does not change dramatically among the progressing  $t_i$ , i.e. the channel can be considered as flat-fading then,  $t_i = 0$  [37]. Also, the term  $U(\cdot, \cdot)$  is the uniform distribution operator [22].

### 3.3 Fading distributions

According to (5) and (6) the  $\alpha$ - $\mu$  distribution offers mathematical tractability. Also, by setting the parameters  $\alpha$  and  $\mu$  to appropriate values many important distributions of the statistical analysis can be obtained, such as the Nakagami-m, Gamma, Rayleigh, Weibull, exponential and one-sided Gaussian [39, 40]. Moreover, it has been extensively employed in studies considering the small-scale fading statistics of RF wireless channels [3, 38, 40]. The PDF and CDF of  $\alpha$ - $\mu$  are expressed as [39]

$$f(x) = \frac{\alpha \mu^\mu x^{\alpha\mu-1} \exp(-\mu x^\alpha)}{\Gamma(\mu)}, \quad (5)$$

$$F(x) = 1 - \frac{\Gamma(\mu, x^\alpha \mu)}{\Gamma(\mu)}, \quad (6)$$

where  $\mu$  is obtained as [39]

$$\mu = \frac{\mathbb{E}^2(X^\alpha)}{\mathbb{V}(X^\alpha)} \quad (7)$$

and  $X$  is a random variable (r.v.) following the  $\alpha$ - $\mu$  distribution. Additionally,  $\Gamma(\cdot)$  and  $\Gamma(\cdot, \cdot)$  stand for the gamma function and the upper incomplete gamma function, respectively [41, eq. (8.310.1)], [41, eq. (8.350.2)].  $\mathbb{E}(\cdot)$  and  $\mathbb{V}(\cdot)$  represent the expected value and variance, respectively. The parameters  $\alpha > 0$  and  $\mu > 0$  stand for the non-linearity of the received signal envelope due to the propagation environment and the number of the multipath components of the received signal [39], respectively. The non-integer values of  $\mu$  could indicate non-zero correlation among the in-phase and quadrature parts of the multipath component, non-zero correlation between different clusters of multipath components, or non-Gaussianity of the in-phase and quadrature components of the fading signal [39].

The Rice and Nakagami-m distributions are widely used in modeling the fading statistics of RF wireless channels



[24, 31, 38]. The PDF and CDF of the Nakagami-m distribution are obtained as [22, eq. (3.38)]

$$f_m(x) = \frac{2\exp(-mx^2)m^m x^{-1+2m}}{\Gamma(m)}, \quad (8)$$

$$F_m(x) = 1 - \frac{\Gamma(m, mx^2)}{\Gamma(m)}, \quad (9)$$

where the parameter  $m$  is the fading parameter. The PDF and CDF of the Rice distribution is expressed as [22, eq. (3.37)]

$$f_R(x) = 2x(K+1)\exp(-K - (K+1)x^2) \times I_0(2x\sqrt{K(K+1)}), \quad (10)$$

$$F_R(x) = Q_1(\sqrt{2K}, 0) - Q_1\left(\sqrt{2K}, \frac{x}{\frac{\sqrt{2}}{2}\sqrt{\frac{1}{K+1}}}\right), \quad (11)$$

where  $Q_1(\cdot, \cdot)$  is the first order Marcum-Q function [42]. The parameter  $K$  denotes the ratio of power of the LoS signal component to the other NLoS signal components, while  $I_0(\cdot)$  is the zero order modified Bessel function of the first kind [43, eq. (9.6.3)].

### 3.4 Analytical distributions fitting accuracy evaluation metrics

The fitting of the examined analytical distributions to the empirical channel gain distribution of each link is evaluated by means of the KS test, the KL divergence, the lgKS test and the RMSE.

The KS goodness of the fit test is defined as [44, eq. (8.320)]

$$\max(|F_{emp}(x) - F(x)|) \leq \sqrt{-\frac{1}{2N} \ln\left(\frac{A}{2}\right)}, \quad (12)$$

where  $F_{emp}(\cdot)$ ,  $N$  and  $\ln(\cdot)$  stand for the empirical values of the channel gain CDF of the examined link, the number of discrete samples of  $F_{emp}(\cdot)$  and the natural logarithm respectively. The parameter  $F(\cdot)$  stands for the analytical CDF, while  $A = 5\%$  is the selected significance level and  $x \in [1, N]$ . According to the KS the analytical distribution is said to fit the empirical one when the inequality of (12) holds true.

The KL divergence is defined as the distance between the empirical PDF  $f_{emp}(\cdot)$  and the analytical PDF  $f(\cdot)$  of the examined distribution [45]

$$KL = -\sum_x f_{emp}(x) \ln\left(\frac{f(x)}{f_{emp}(x)}\right), \quad (13)$$

where  $x \in [1, N]$ . The closer the value of (13) to 0 the better is the fit of the analytical to the empirical distribution.

In some cases the fitting of the tail of the analytical distribution to the empirical one is of particular interest. For

example, such a scenario is the case of severe fading [46, 47]. The statistical test that can yield an appropriate metric regarding the tail fitting is the modified KS test, which from now on will be referred to as the logarithmic scale KS test (lgKS). The lgKS test is expressed as [47, 48]

$$q = \max_x |\log_{10}(F_{emp}(x)) - \log_{10}(F(x))|, \quad (14)$$

where  $x \in [1, N]$  and  $\log_{10}(\cdot)$  stands for the logarithm of base 10. It should be noted, that a value of  $q = 1$  expresses that there is a difference of one order of magnitude between the analytical and the empirical CDF.

The RMSE is a common fitting accuracy metric. It is applied in many different fields, where the deviation of a function from another one is needed and it is expressed as

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_x (f_{emp}(x) - f(x))^2}, \quad (15)$$

where  $x \in [1, N]$ . The mean square error expresses the mean distance of the analytical distribution to the empirical one. The closer the value of (15) to 0, the better the fit achieved by the analytical distribution. The RMSE is commonly used as a fitting evaluation metric in wireless channel modeling [48, 49]. Also, it should be noted that the RMSE is often presented in dB scale [48]. The RMSE values representation in dB scale is also applied in this work as can be seen in Tables 3 and 4.

## 4. COMMUNICATION PERFORMANCE ASSESSMENT METRICS

An important aspect in evaluating the performance of a wireless system is the EC. In this direction, the EC must be evaluated, when the wireless channel is assumed to be described by each of the examined analytical distributions. Also, the achieved aforementioned EC must be compared to the one based on the measurements of each link.

In THz wireless communications the channel gain of SISO link is expressed as [3]

$$|h| = |h_d| |h_f|, \quad (16)$$

where  $h_d$  and  $h_f$  stand for the deterministic and stochastic channel gain, respectively. Based on (16) the instantaneous SNR is expressed as

$$\text{SNR} = \kappa |h_f|^2, \quad (17)$$

where

$$\kappa = \frac{P_t G_t G_r |h_d|^2}{N_o}. \quad (18)$$

The parameters  $P_t$  and  $N_o$  stand for the transmitted power spectral density and the noise power spectral density at the RX, respectively. Meanwhile, the parameters  $G_t$  and  $G_r$  denote the TX and RX antenna gains, respectively.

For a THz wireless system where  $h_f$  is expressed by the  $\alpha$ - $\mu$  distribution, the PDF and CDF of the instantaneous SNR after some algebraic manipulations and by using [44, eq. 5.4] and [44, eq. 5.3] can be obtained as

$$f_{SNR_{\alpha-\mu}}(x) = \frac{\alpha \exp\left(-\mu\left(\frac{x}{\kappa}\right)^{\frac{\alpha}{2}}\right) \left(\mu\left(\frac{x}{\kappa}\right)^{\frac{\alpha}{2}}\right)^{\mu}}{2x\Gamma(m)}, \quad (19)$$

$$F_{SNR_{\alpha-\mu}}(x) = 1 - \frac{\Gamma\left(\mu, \mu\left(\frac{x}{\kappa}\right)^{\frac{\alpha}{2}}\right)}{\Gamma(\mu)}. \quad (20)$$

The EC by employing (19) can be obtained as [42]

$$EC_{\alpha-\mu} = \int_0^{\infty} \log_2(1+x) f_{SNR_{\alpha-\mu}}(x) dx. \quad (21)$$

For a THz wireless system where  $h_f$  follows the Nakagami-m distribution, the PDF and CDF of the instantaneous SNR after some algebraic manipulations and by using [44, eq. 5.4] and [44, eq. 5.3] can be obtained as

$$f_{SNR_N}(x) = \frac{\exp\left(-\frac{mx}{\kappa}\right) m^m \left(\frac{x}{\kappa}\right)^{m-1}}{x\Gamma(m)}, \quad (22)$$

$$F_{SNR_N}(x) = 1 - \frac{\Gamma\left(m, \frac{mx}{\kappa}\right)}{\Gamma(m)} \quad (23)$$

The ergodic capacity by employing (19) can be obtained as

$$EC_N = \int_0^{\infty} \log_2(1+x) f_{SNR_N}(x) dx. \quad (24)$$

For a THz wireless system where  $h_f$  follows the Rice distribution, the PDF and CDF of the instantaneous SNR after some algebraic manipulations and by using [44, eq. 5.4] and [44, eq. 5.3] can be obtained as

$$f_{SNR_R}(x) = 2x(K+1) \exp(-K - (K+1)x^2) \times I_0\left(2x\sqrt{K(K+1)}\right), \quad (25)$$

$$F_{SNR_R}(x) = Q_1\left(\sqrt{2K}, 0\right) - Q_1\left(\sqrt{2K}, \sqrt{\frac{2x(K+1)}{\kappa}}\right). \quad (26)$$

The ergodic capacity by employing (19) can be obtained as

$$EC_R = \int_0^{\infty} \log_2(1+x) f_{SNR_R}(x) dx. \quad (27)$$

## 5. NUMERICAL RESULTS

In this section, the fitting accuracy of the  $\alpha$ - $\mu$ , Rice, and Nakagami-m distributions to the empirical channel gain distributions of the links defined by the TXs and RX<sub>2</sub> and

RX<sub>3</sub>, is presented. Also, the applicability of the presented framework in the evaluation of the EC of the corresponding wireless links is examined. Furthermore, the range of the calculated distribution parameters provides useful insights regarding the small-scale fading channel modeling of LoS and NLoS THz wireless links. Additionally, the values of the fitting accuracy metrics aid in locating the most suitable distribution to model the small-scale fading of a THz wireless link.

Tables 1 and 2 respectively present the extracted parameters of the examined distributions for the links defined by a TX and RX<sub>2</sub> and RX<sub>3</sub>. The TX column in these tables contains the index of the particular TX-RX link. The  $d$  column stands for the TX-RX separation distance. The LoS column in these tables indicates whether the considered link is in LoS or NLoS. According to Table 1, the ranges of the examined distribution parameters of the LoS links defined by RX<sub>2</sub> are  $\alpha \in [3- 3.3]$ ,  $\mu \in [0.75- 2.11]$ ,  $m \in [1.6- 4.4]$  and  $K \in [1.9- 7.5]$ . For the NLoS links defined by RX<sub>2</sub> it is observed that the extracted distribution parameters presented in Table 1 are within the ranges  $\alpha \in [2.07- 3.17]$ ,  $\mu \in [0.65- 0.95]$ ,  $m \in [1- 1.55]$  and  $K \in [0.14- 1.7]$ . Meanwhile, from Table 2, the parameters of the LoS links defined by RX<sub>3</sub> are within the ranges  $\alpha \in [2.8- 3.12]$ ,  $\mu \in [0.61- 1.2]$ ,  $m \in [1.07- 2.6]$ , and  $K \in [0.63- 3.87]$ . For the NLoS links defined by RX<sub>3</sub> the distribution parameters of Table 2 are within the ranges  $\alpha \in [2.04- 5.27]$ ,  $\mu \in [0.35- 1.45]$ ,  $m \in [1.006- 3.09]$ , and  $K \in [0.18- 4.85]$ .

**Table 1** – Distribution parameters for RX<sub>2</sub> links

TX	LoS	$d$ (m)	$\alpha$	$\mu$	$m$	$K$ (dB)
2	✗	47.22	2.078	0.952	1.009	0.198
3	✗	39.57	2.282	0.863	1.054	0.474
4	✗	38.67	2.067	0.954	1.003	0.149
5	✗	32.08	2.46	0.775	1.057	0.516
6	✗	30.95	2.449	0.785	1.064	0.539
7	✗	28.71	2.25	0.872	1.041	0.419
8	✗	27.13	3.054	0.756	1.476	1.605
9	✗	25.93	2.245	0.886	1.057	0.473
10	✗	20.46	2.136	0.925	1.022	0.301
11	✗	22.56	2.233	0.878	1.038	0.4
12	✗	17.16	3.171	0.748	1.557	1.776
13	✓	15.29	3.217	0.756	1.619	1.904
14	✓	10.64	3.019	1.488	3.094	4.85
15	✓	10.19	3.283	0.989	2.289	3.253
16	✗	10.79	3.069	0.656	1.259	1.123
17	✓	5.02	3.278	1.126	2.642	3.959
18	✓	4.05	2.998	2.11	4.438	7.554
19	✗	10.12	3.073	0.694	1.35	1.332
20	✗	4.65	2.518	0.796	1.13	0.749
21	✗	11.77	2.149	0.927	1.033	0.357
22	✗	9.44	2.173	0.907	1.029	0.344
23	✗	10.72	2.2	0.895	1.035	0.378

**Table 2** – Distribution parameters for RX<sub>3</sub> links

TX	LoS	$d$ (m)	$\alpha$	$\mu$	$m$	$K$ (dB)
2	✗	58.09	2.195	0.875	1.007	0.247
3	✗	49.02	2.344	0.828	1.052	0.482
4	✗	49.62	2.042	0.978	1.009	0.18
6	✗	41.82	2.293	0.866	1.066	0.52
7	✗	36.2	2.726	0.737	1.18	0.906
8	✗	36.13	2.527	0.773	1.1	0.666
9	✗	36.87	2.161	0.904	1.016	0.285
10	✗	28.93	2.786	0.7	1.154	0.845
11	✗	29.08	2.494	0.799	1.118	0.714
12	✗	28.03	3.127	0.781	1.599	1.858
13	✗	19.19	5.275	0.353	1.434	1.58
14	✗	20.69	2.787	0.66	1.077	0.626
15	✗	21.89	2.351	0.84	1.072	0.548
16	✗	25.48	2.318	0.838	1.047	0.456
17	✗	17.31	3.421	0.664	1.542	1.752
18	✗	13.27	2.727	0.704	1.121	0.747
19	✓	9.07	2.819	0.649	1.076	0.631
20	✗	7.12	3.058	1.457	3.094	4.858
21	✓	3.07	3.123	0.613	1.195	0.971
22	✗	5.55	2.699	0.71	1.112	0.721
23	✓	9.97	3.12	1.205	2.605	3.88
24	✗	17.09	2.926	0.705	1.263	1.128

Tables 3 and 4 evaluate the fitting accuracy of the examined analytical distributions to the empirical PDFs and CDFs of the measured links. These tables encapsulate the PDF fitting accuracy metrics KL and RMSE and the CDF accuracy metric of lgKS. The CDF accuracy KS metric is not shown in Tables 3 and 4, because for all the investigated links, all the examined analytical distributions yield a value below the selected significance level of 5%.

Fig. 2(a) shows the fitting of examined analytical distributions to the empirical channel gain PDFs of the links TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>. The blue circles stand for the empirical channel gain PDFs of the presented links, while the red, orange and green lines stand for the corresponding analytical expressions of  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions, respectively. The KL and RMSE values of Table 3 show that Rice yields the best fit to the empirical distributions for both of the links. Meanwhile, Nakagami-m does not fit the empirical PDFs of the links. Also, for both TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>,  $\alpha$ - $\mu$  yields a good fit, except a slight divergence on the left of the empirical distributions.

In Fig. 2(b), the fitting of the examined analytical CDFs to the empirical ones of the links TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> is presented. The blue circles and stars stand for the empirical CDFs of TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>, respectively. The continuous and dashed red, orange and green lines represent the analytical CDF expressions of  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions for TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> respectively. The minimum empirical probability of TX<sub>17</sub>-RX<sub>2</sub> is  $F(x) = 0.0014$ , which is obtained for  $x = -9.6$  dB. The minimum empirical probability of TX<sub>14</sub>-RX<sub>2</sub> is  $F(x) = 0.0013$ , which corresponds to  $x = -8.86$  dB. Also, for any given  $x$ ,

the empirical probability of TX<sub>14</sub>-RX<sub>2</sub> is lower compared to that of TX<sub>17</sub>-RX<sub>2</sub>. For example, for  $x = -7$  dB the empirical probability of TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> is  $F(x) = 0.003$  and  $F(x) = 0.005$ , respectively. The previous observations indicate that, the channel propagation conditions of TX<sub>14</sub>-RX<sub>2</sub> are better compared to those of TX<sub>17</sub>-RX<sub>2</sub>. These findings on the empirical CDFs correspond to the parameter values of the analytical distributions of Table 1. The values of  $\mu$ ,  $m$  and  $K$  of TX<sub>14</sub>-RX<sub>2</sub> are greater than those of TX<sub>17</sub>-RX<sub>2</sub>. The parameter  $\alpha$  of TX<sub>14</sub>-RX<sub>2</sub> is lower compared to the one of TX<sub>17</sub>-RX<sub>2</sub>. In more detail, the physical meaning of those parameters verify that stronger multipath components are detected by the RX in the case of TX<sub>14</sub>-RX<sub>2</sub>. Furthermore, the lgKS metric shown in Table 3 and the curves of Fig. 2 demonstrate that the Rice distribution in both of the presented links yields an almost perfect fit to the empirical data.

Fig. 2(c) shows the EC of the links TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> as a function of  $\kappa$ . The circles and stars stand for the EC achieved by employing the empirical distributions of TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>, respectively. The continuous and dashed red, orange and green lines represent the EC obtained by making use of the analytical expressions of  $\alpha$ - $\mu$ , Rice and Nakagami-m for the TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> links, respectively. The empirical curves show that for any given value of  $\kappa$ , the EC of TX<sub>14</sub>-RX<sub>2</sub> is always greater compared to the one of TX<sub>17</sub>-RX<sub>2</sub>. This remark is in accordance with the observation made on Fig. 2(b), which states that TX<sub>14</sub>-RX<sub>2</sub> has better channel conditions compared to TX<sub>17</sub>-RX<sub>2</sub>. As an example, for  $\kappa = 16$  dB the empirical EC of TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub> is 5.1 (bps/Hz) and 5.06 (bps/Hz), respectively. As Fig. 2(c) illustrates the EC curves obtained by employing the Rice distribution closely follow the empirical ones, whereas the  $\alpha$ - $\mu$  EC curves slightly diverge. For example, for TX<sub>14</sub>-RX<sub>2</sub> and  $\kappa = 24$  dB the empirical, Rice and  $\alpha$ - $\mu$  obtained EC is 7.71, 7.72, and 7.73 bps/Hz, respectively. The Nakagami-m EC curves show the greatest divergence from the empirical ones. For both TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>, the EC obtained by means of Nakagami-m can be considered as an upper bound. For example, for TX<sub>14</sub>-RX<sub>2</sub> and  $\kappa = 30$  dB the empirical and Nakagami-m EC is 9.69 and 9.78 bps/Hz, respectively. Also, for TX<sub>17</sub>-RX<sub>2</sub> and  $\kappa = 30$  dB the empirical and Nakagami-m EC is 9.65 and 9.75 bps/Hz, respectively.

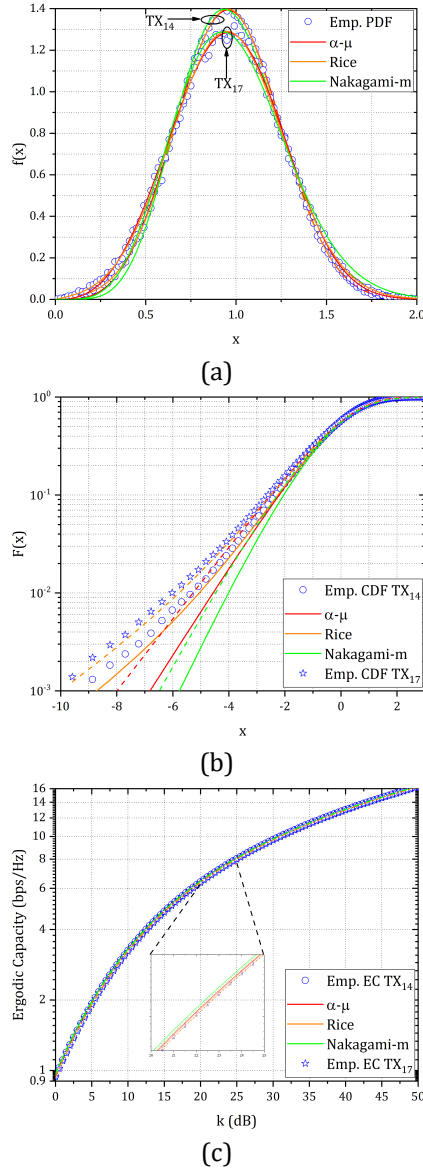
Fig. 3(a) shows the fitting achieved by  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions to the empirical PDFs of links TX<sub>5</sub>-RX<sub>2</sub> and TX<sub>16</sub>-RX<sub>2</sub>. The blue circles and the red, orange and green lines stand for the empirical PDFs, the  $\alpha$ - $\mu$ , Rice and Nakagami-m analytical PDFs, respectively. The KL and RMSE metrics of Table 3 for the presented links state that the  $\alpha$ - $\mu$  performs a better fit to the empirical data compared to that achieved by Rice and Nakagami-m. From this figure, it is observed that for both TX<sub>5</sub>-RX<sub>2</sub> and TX<sub>16</sub>-RX<sub>2</sub> Nakagami-m does not fit the empirical curves. The curve of Rice diverges from

**Table 3** – Fitting evaluation metrics for  $RX_2$  links.

TX	$KL_{\alpha-\mu}$	$KL_R$	$KL_N$	$lgKS_{\alpha-\mu}$	$lgKS_R$	$lgKS_N$	$RMSE_{\alpha-\mu}$ (dB)	$RMSE_R$ (dB)	$RMSE_N$ (dB)
2	0.019	0.019	0.023	0.124	0.138	0.151	−19.94	−19.92	−19.82
3	0.021	0.023	0.083	0.154	0.17	0.254	−20.15	−20.14	−18.84
4	0.017	0.018	0.021	0.13	0.149	0.153	−20.33	−20.3	−20.23
5	0.046	0.076	0.199	0.097	0.166	0.25	−19.27	−18.93	−17.31
6	0.03	0.048	0.159	0.107	0.162	0.258	−19.5	−19.27	−17.52
7	0.015	0.016	0.057	0.134	0.158	0.221	−20.15	−20.18	−19.09
8	0.025	0.019	0.419	0.312	0.124	0.822	−19.19	−19.63	−14.96
9	0.016	0.015	0.066	0.166	0.167	0.255	−20.21	−20.21	−19.16
10	0.016	0.016	0.031	0.152	0.165	0.2	−20.2	−20.23	−19.81
11	0.025	0.026	0.073	0.127	0.151	0.208	−19.41	−19.45	−18.68
12	0.035	0.03	0.539	0.341	0.125	0.94	−18.95	−19.57	−14.6
13	0.048	0.032	0.571	0.431	0.18	1.08	−18.5	−19.13	−14.46
14	0.211	0.031	0.928	0.901	0.149	1.749	−17.58	−18.6	−14.89
15	0.109	0.05	1.013	0.692	0.076	1.663	−18.87	−18.53	−14.3
16	0.017	0.072	0.449	0.192	0.204	0.591	−18.74	−17.99	−14.83
17	0.13	0.049	1.006	0.658	0.089	1.571	−17.61	−17.8	−14.15
18	0.067	0.035	0.45	0.376	0.034	0.983	−17.74	−17.73	−15.11
19	0.016	0.038	0.441	0.228	0.158	0.679	−19.97	−19.58	−15.06
20	0.013	0.019	0.158	0.15	0.144	0.342	−20.14	−20.02	−17.42
21	0.017	0.016	0.035	0.153	0.154	0.206	−19.89	−19.89	−19.5
22	0.016	0.016	0.039	0.129	0.145	0.189	−21.32	−21.34	−20.46
23	0.019	0.02	0.052	0.168	0.185	0.238	−19.76	−19.76	−19.14

**Table 4** – Fitting evaluation metrics for  $RX_3$  links.

TX	$KL_{\alpha-\mu}$	$KL_R$	$KL_N$	$lgKS_{\alpha-\mu}$	$lgKS_R$	$lgKS_N$	$RMSE_{\alpha-\mu}$ (dB)	$RMSE_R$ (dB)	$RMSE_N$ (dB)
2	0.016	0.018	0.033	0.117	0.175	0.182	−20.04	−19.73	−19.36
3	0.019	0.024	0.087	0.154	0.194	0.272	−20.21	−20.09	−18.63
4	0.021	0.02	0.024	0.186	0.186	0.201	−19.39	−19.39	−19.36
6	0.016	0.016	0.068	0.162	0.166	0.268	−19.79	−19.77	−18.64
7	0.015	0.027	0.233	0.161	0.159	0.429	−19.86	−19.6	−16.34
8	0.015	0.022	0.141	0.114	0.147	0.297	−19.85	−19.71	−17.19
9	0.02	0.022	0.043	0.22	0.262	0.293	−19.9	−19.9	−19.46
10	0.017	0.044	0.267	0.116	0.159	0.39	−19.58	−18.95	−15.92
11	0.016	0.015	0.115	0.148	0.149	0.327	−20.15	−20.16	−17.57
12	0.034	0.031	0.547	0.409	0.143	1.016	−18.88	−19.25	−14.65
13	0.057	0.651	1.509	0.045	0.198	0.832	−16.81	−12.6	−11.05
14	0.057	0.159	0.378	0.048	0.178	0.289	−18.4	−17.27	−15.55
15	0.019	0.021	0.092	0.175	0.189	0.299	−19.22	−19.21	−18.03
16	0.021	0.026	0.09	0.125	0.163	0.234	−19.57	−19.53	−18.3
17	0.021	0.081	0.685	0.304	0.171	0.966	−19.6	−17.96	−14.03
18	0.024	0.066	0.273	0.112	0.176	0.357	−18.92	−18.33	−15.98
19	0.047	0.133	0.351	0.079	0.218	0.326	−18.93	−17.44	−15.56
20	0.142	0.028	0.813	0.786	0.071	1.654	−18.03	−18.51	−14.89
21	0.063	0.216	0.62	0.128	0.215	0.505	−19.03	−17.23	−14.44
22	0.032	0.079	0.285	0.114	0.181	0.349	−19.11	−18.47	−16.03
23	0.144	0.032	0.917	0.815	0.07	1.738	−17.76	−18.25	−14.65
24	0.014	0.025	0.318	0.186	0.155	0.548	−19.7	−19.51	−15.41



**Fig. 2** – Fitting of the analytical to the empirical distributions for the links TX<sub>14</sub>-RX<sub>2</sub> and TX<sub>17</sub>-RX<sub>2</sub>

the right tail of the empirical PDF of TX<sub>16</sub>-RX<sub>2</sub>. Also, the curve of Rice slightly diverges from the left tail of the empirical PDF of TX<sub>5</sub>-RX<sub>2</sub>.

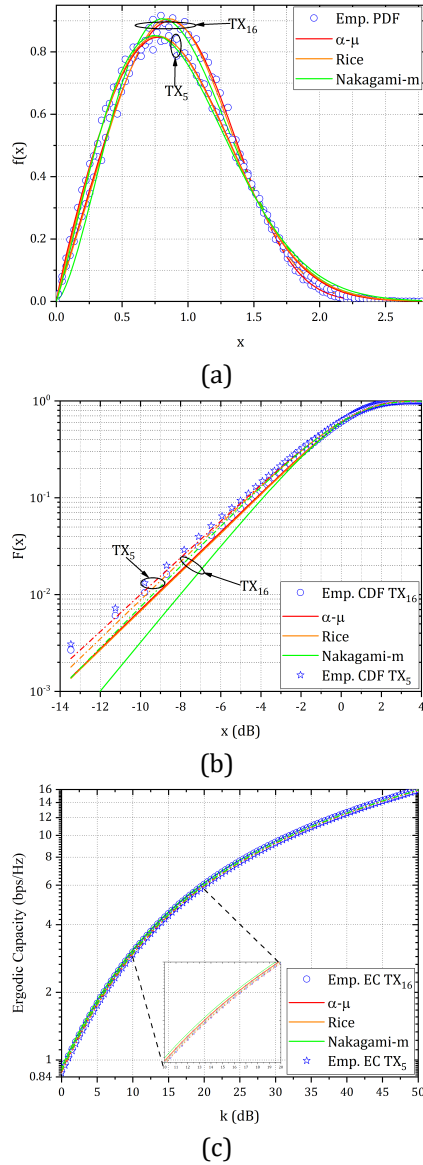
In Fig. 3(b), the fitting of the investigated analytical CDFs to the empirical ones of the links TX<sub>5</sub>-RX<sub>2</sub> and TX<sub>16</sub>-RX<sub>2</sub> is presented. The blue circles and stars stand for the empirical CDFs of TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub>, respectively. The continuous and dashed red, orange and green lines indicate the analytical CDF expressions of TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub>, respectively. The minimum empirical probability for TX<sub>16</sub>-RX<sub>2</sub> is  $F(x) = 0.0026$  for  $x = -13.46$  dB. Meanwhile, the minimum empirical probability for TX<sub>5</sub>-RX<sub>2</sub> is  $F(x) = 0.0031$  for  $x = -13.46$  dB. For any given low value of  $x$  the empirical probability of TX<sub>16</sub>-RX<sub>2</sub> is lower compared to that of TX<sub>5</sub>-RX<sub>2</sub>. As an example, for  $x = -9.08$  dB the empirical probability of TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub> is  $F(x) = 0.0105$

and  $F(x) = 0.0132$ , respectively. The aforementioned results indicate that the channel propagation conditions of TX<sub>16</sub>-RX<sub>2</sub> are better than those of TX<sub>5</sub>-RX<sub>2</sub>. The previous observations on the empirical distributions of the links TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub>, have also to be interpreted in terms of the extracted distribution parameters shown in Table 1. In terms of the  $\alpha$ - $\mu$ , the parameter  $\alpha$  of TX<sub>16</sub>-RX<sub>2</sub> is greater compared to the one of TX<sub>5</sub>-RX<sub>2</sub>. Meanwhile, the parameter  $\mu$  of TX<sub>16</sub>-RX<sub>2</sub> is less than the one of TX<sub>5</sub>-RX<sub>2</sub>. This remark states that in NLoS conditions, when comparing the channel propagation conditions of two links; the one with the greatest value of  $\alpha$  and the lower value of  $\mu$  has the lowest probability at a greater value of  $x$ . In the meantime, the parameters  $K$  and  $m$  of TX<sub>16</sub>-RX<sub>2</sub> are greater than those of TX<sub>5</sub>-RX<sub>2</sub>. This remark states that when comparing two NLoS links the one with the greatest value of  $K$  or  $m$  has the lowest probability at a greater value of  $x$ . This is in accordance with the definition of the Rice and Nakagami-m distribution parameters. Meanwhile, the lgKS values of Table 3 reveal that  $\alpha$ - $\mu$  performs a better fit to the empirical CDFs compared to Rice and Nakagami-m. Fig. 2(b), illustrates that Nakagami-m for both of the presented links as  $x$  decreases significantly deviates from the empirical curves. Moreover, Rice has almost the same fitting performance as  $\alpha$ - $\mu$  for the link TX<sub>16</sub>-RX<sub>2</sub>, whereas it diverges as  $x$  decreases for TX<sub>5</sub>-RX<sub>2</sub>.

Fig. 3(c) shows the EC of the links TX<sub>5</sub>-RX<sub>2</sub> and TX<sub>16</sub>-RX<sub>2</sub> as a function of  $\kappa$ . The circles and stars stand for the achieved empirical EC of TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub>, respectively. The continuous and dashed red, orange and green lines represent the EC expressions obtained by employing the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions for the links TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub>, respectively. From the empirical EC curves it is observed that the achieved EC by TX<sub>16</sub>-RX<sub>2</sub> is greater compared to that of TX<sub>5</sub>-RX<sub>2</sub> for any given  $\kappa$ . This observation is in accordance with that of Fig. 3(b), which states that TX<sub>16</sub>-RX<sub>2</sub> has better channel conditions compared to TX<sub>5</sub>-RX<sub>2</sub>. For example, for  $\kappa = 15$  dB the achieved empirical EC of TX<sub>16</sub>-RX<sub>2</sub> and TX<sub>5</sub>-RX<sub>2</sub> is 4.48 (bps/Hz) and 4.38 (bps/Hz), respectively. Fig. 3(c), illustrates that for both of the examined links the EC curves obtained by means of the  $\alpha$ - $\mu$  closely follow the empirical ones. Meanwhile, for both of the presented links the Rice EC curves slightly diverge from the empirical ones. For example, for TX<sub>16</sub>-RX<sub>2</sub> and  $\kappa = 17$  dB the empirical and  $\alpha$ - $\mu$  EC is 5.1 bps/Hz, while for  $\kappa = 17$  dB Rice yields an EC equal to 5.12 bps/Hz. For both of the examined links, the EC curves obtained by means of the Nakagami-m display an upper bound behavior to the empirical ones. As an example, for the link TX<sub>16</sub>-RX<sub>2</sub> and  $\kappa = 25$  dB the empirical EC and the corresponding Nakagami-m one yield 7.67 and 7.78 bps/Hz, respectively.

Fig. 4(a) illustrates the fitting of the analytical PDFs to the empirical ones of the links TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>.





**Fig. 3** – Fitting of the analytical to the empirical distributions and their EC performance for the links TX<sub>5</sub>-RX<sub>2</sub> and TX<sub>16</sub>-RX<sub>3</sub>.

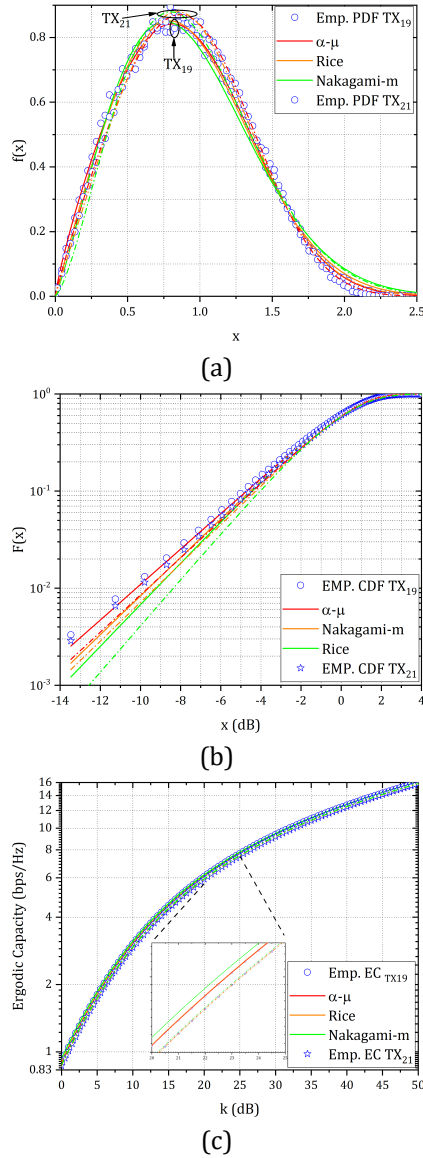
The blue circles indicate the empirical PDFs of TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>. The red, orange and green continuous and dashed lines stand for the analytical expressions of  $\alpha$ - $\mu$ , Rice and Nakagami-m for TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. Based on the fitting accuracy KL and RMSE metrics of Table 4,  $\alpha$ - $\mu$  yields the best fit to both of the empirical channel gain distributions. Meanwhile, for both of the presented links, the curve of Rice diverges from the right tail of the empirical PDFs. Furthermore, the curve of Nakagami-m does not fit the empirical distributions of TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>.

In Fig. 4(b), the fitting of the examined analytical distributions to the empirical CDFs of the links TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub> is presented. The blue circles and stars stand for the empirical CDFs of the links TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. The continuous and dashed red, orange and green lines represent the analytical expressions of  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions of

TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. The minimum empirical probability of TX<sub>21</sub>-RX<sub>3</sub> and TX<sub>19</sub>-RX<sub>3</sub> is obtained for  $x = -13.47$  dB and is  $F(x) = 0.0029$  and  $F(x) = 0.0033$ , respectively. For any given value of  $x$ , especially for the lower ones the empirical probability of TX<sub>21</sub>-RX<sub>3</sub> is always lower compared to that of TX<sub>19</sub>-RX<sub>3</sub>. As an example, a value of  $x = -11.25$  dB yields  $F(x) = 0.0077$  and  $F(x) = 0.0066$  for TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. The previous observations indicate that the channel conditions of TX<sub>21</sub>-RX<sub>3</sub> are better than those of TX<sub>19</sub>-RX<sub>3</sub>. By considering this, the equivalent connection to the extracted distribution parameters of Table 2 must be performed. In more detail, in terms of the  $\alpha$ - $\mu$  distribution it is noted that the parameter  $\alpha$  of TX<sub>21</sub>-RX<sub>3</sub> is greater than the one of TX<sub>19</sub>-RX<sub>3</sub>. The parameter  $\mu$  of TX<sub>21</sub>-RX<sub>3</sub> is lower than the one of TX<sub>19</sub>-RX<sub>3</sub>. The parameters  $K$  and  $m$  of TX<sub>21</sub>-RX<sub>3</sub> are greater compared to those of TX<sub>19</sub>-RX<sub>3</sub>. This is in accordance with the definitions of the Rice and Nakagami-m distribution parameters. In more detail, the greater the value of  $K$  or  $m$ , the stronger the multipath components of the channel. Furthermore, the lgKS metric of Table 4 and Fig. 4(b), show that as  $x$  is reduced for both TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>,  $\alpha$ - $\mu$  achieves the best fit to the empirical CDFs. Meanwhile, the analytical expressions of Rice and Nakagami-m diverge from the empirical curves of TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>. The Nakagami-m curves perform the worst fit to the empirical distributions of both links.

Fig. 4(c) illustrates the EC of the links TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub> as a function of  $\kappa$ . The circles and stars stand for the achieved EC by the data of TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. The continuous and dashed red, orange and green lines represent the EC expressions obtained by means of the  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions for TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>, respectively. The empirical EC curves state that the EC achieved by TX<sub>19</sub>-RX<sub>3</sub> link is greater compared to that of TX<sub>21</sub>-RX<sub>3</sub> for every value of  $\kappa$ . This observation is in accordance with that of fig. 4(b), which states that TX<sub>19</sub>-RX<sub>3</sub> has better channel conditions compared to TX<sub>21</sub>-RX<sub>3</sub>. As an example, for  $\kappa = 30$  dB the empirical EC of TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub> is 9.36 bps/Hz and 9.18 bps/Hz, respectively. As Fig. 4(c), illustrates for both of the examined links, the EC curves obtained by means of  $\alpha$ - $\mu$  and Rice closely follow the empirical curves. For example, for TX<sub>19</sub>-RX<sub>3</sub> and  $\kappa = 20$  dB the empirical and  $\alpha$ - $\mu$  EC is 6.08 bps/Hz, while for  $\kappa = 20$  dB Rice yields an EC equal to 6.1 bps/Hz. Meanwhile, the Nakagami-m EC curves for both of the links do not diverge significantly from the empirical ones. However, they display an upper bound behavior to the empirical ones.

Fig. 5(a) presents the fitting accomplished by  $\alpha$ - $\mu$ , Rice and Nakagami-m analytical PDFs to the empirical ones of the links TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>. The blue circles stand for the empirical PDFs of TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>. The red, orange and green lines represent



**Fig. 4** – Fitting of the analytical to the empirical distributions for the links TX<sub>19</sub>-RX<sub>3</sub> and TX<sub>21</sub>-RX<sub>3</sub>.

the analytical PDFs of  $\alpha$ - $\mu$ , Rice and Nakagami-m, respectively. The KL and RMSE metrics of Table 4 reveal that the Rice distribution accomplishes a good fit to the empirical distributions. Meanwhile, on both TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>,  $\alpha$ - $\mu$  diverges from the left tail of the empirical PDFs of the links at all.

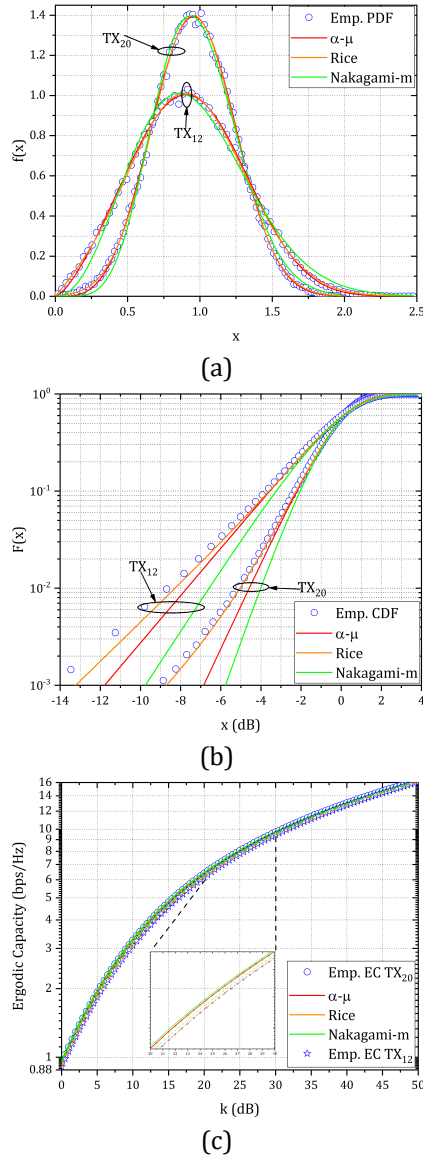
In Fig. 5(b), the fitting achieved by the analytical CDFs to the empirical ones of the links TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub> is illustrated. The blue circles stand for the empirical CDFs of TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>. The red, orange and green lines represent the analytically obtained CDFs of  $\alpha$ - $\mu$ , Rice and Nakagami-m, respectively. The minimum empirical probability for TX<sub>12</sub>-RX<sub>3</sub> is  $F(x) = 0.0015$  for  $x = -13.47$  dB. For TX<sub>20</sub>-RX<sub>3</sub> the minimum empirical probability is  $F(x) = 0.0011$  for  $x = -8.86$  dB. Furthermore, for a given low value of  $x$  the empirical probability of TX<sub>20</sub>-RX<sub>3</sub> is significantly

to lower compared that of TX<sub>12</sub>-RX<sub>3</sub>. As an example, a value of  $x = -6$  dB yields  $F(x) = 0.0345$  and  $F(x) = 0.0056$  for TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>, respectively. The aforementioned observations indicate that the channel conditions of TX<sub>20</sub>-RX<sub>3</sub> are better compared to those of TX<sub>13</sub>-RX<sub>3</sub>. This interpretation of the empirical distributions additionally corresponds to the extracted parameters of the examined analytical distributions, which can be found in Table 2. In more detail, the parameters  $\mu$ ,  $m$  and  $K$  of TX<sub>20</sub>-RX<sub>3</sub> are significantly greater compared to those of TX<sub>12</sub>-RX<sub>3</sub>. By taking into account the definition of those parameters, this can be interpreted as the TX<sub>20</sub>-RX<sub>3</sub> having significantly stronger multipath components detected by the RX, when compared to TX<sub>20</sub>-RX<sub>3</sub>. Furthermore, by observing the curves of the analytical CDFs of this figure and based on the lgKS metric of Table 4, the Rice distribution achieves almost a perfect fit to the empirical data, even as  $x$  decreases.

Fig. 5(c) illustrates the EC of the links TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub> as a function of  $\kappa$ . The circles and stars stand for the achieved EC by the data of TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>, respectively. The continuous and dashed red, orange and green lines represent the EC expressions obtained by means of  $\alpha$ - $\mu$ , Rice and Nakagami-m for TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub>, respectively. The empirical EC curves state that the EC achieved by TX<sub>20</sub>-RX<sub>3</sub> is greater compared to that of TX<sub>12</sub>-RX<sub>3</sub> for every value of  $\kappa$ . This observation is in accordance with that of Fig. 5(b), which states that TX<sub>20</sub>-RX<sub>3</sub> has better channel conditions than TX<sub>12</sub>-RX<sub>3</sub>. As an example for  $\kappa = 25$  dB the empirical EC of TX<sub>20</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub> is 8.05 bps/Hz and 7.78 bps/Hz, respectively. As Fig. 5(c), illustrates for both of the examined links, the EC curves obtained by means of  $\alpha$ - $\mu$  and Rice distributions closely follow the empirical ones. For example, for TX<sub>20</sub>-RX<sub>3</sub> and  $\kappa = 30$  dB the empirical and Rice EC is 9.7 bps/Hz, while for  $\kappa = 30$  dB  $\alpha$ - $\mu$  yields an EC equal to 9.72 bps/Hz. Meanwhile, the EC curves obtained by means of Nakagami-m for both TX<sub>12</sub>-RX<sub>3</sub> and TX<sub>20</sub>-RX<sub>3</sub> do not diverge significantly from the empirical ones. However, it is observed that for both of the examined links the EC curves of Nakagami-m display an upper bound behavior to the empirical ones.

Tables 1 and 2, in combination with the observations made on the LoS links presented in figures 2(a)(b) and 4(a)(b) provide insights about the values of the examined distribution parameters. More specifically, when comparing the channel conditions of two LoS links, the one with the better channel conditions, yields greater values for the parameters  $\mu$ ,  $m$  and  $K$ , while the parameter  $\alpha$  obtains a lower value.

By taking into account Tables 1 and 2 combined with the observations made on the NLoS links presented in figures 3(a)(b) and 5(a)(b), insights can be provided regarding the parameter values of the examined distributions. In more detail, when comparing two NLoS links, the one



**Fig. 5** – Fitting of the analytical to the empirical distributions for the links TX<sub>12</sub>–RX<sub>3</sub> and TX<sub>20</sub>–RX<sub>3</sub>

with the better channel conditions yields greater values for the parameters  $\alpha$ ,  $m$  and  $K$  and a lower value for the parameter  $\mu$ .

The observations made on the figures 2(a)(b)–5(a)(b) and the fitting accuracy metrics presented in Tables 3 and 4, provide useful insights about the suitability of the examined distributions in terms of small-scale fading statistics of the THz wireless channels. For the LoS transmissions it is deduced that the Rice distribution describes more accurately the fading statistics of the measured channels. However, there are cases where the fitting metrics suggest that the  $\alpha$ - $\mu$  should be employed instead. Despite this fact, in such scenarios, by observing the metrics of Tables 3 and 4, the difference between the corresponding ones of  $\alpha$ - $\mu$  and Rice are minor. Furthermore, for the NLoS transmissions it is observed that, the  $\alpha$ - $\mu$  distribution yields the most accurate fit to the measured channel gains of the investigated links. Meanwhile,

there are cases where according to the fitting accuracy metrics the Rice distribution achieves the most accurate fit to the empirical distributions. Despite this fact, in such scenarios the fitting accuracy metrics of Tables 3 and 4 suggest that the difference between the corresponding ones of  $\alpha$ - $\mu$  and Rice is insignificant. Meanwhile, for all of the presented links according to the KL, RMSE and lgKS metrics it is concluded that the Nakagami-m does not fit the empirical channel gain measurements.

The observations made on the EC performance results presented in figures 2(c)– 5(c) are in accordance with the fitting evaluation of the examined analytical distributions. In more detail, the analytical expression that performs the best fit, also yields the most accurate EC expression, which is almost exact to the empirical one. Furthermore, the EC expressions obtained by means of  $\alpha$ - $\mu$ , Rice and Nakagami-m yield values quite similar to the empirical ones for every value of  $\kappa$ . However, it is observed that the EC expression of Nakagami-m has the greatest divergence from the empirical values and can be stated that it presents an upper bound behavior to the EC results. Meanwhile, an increase of  $\kappa$  improves the achieved EC. This corresponds to an improvement of the deterministic channel gain, which mitigates the impact of the small-scale fluctuations in the total channel gain of a THz wireless link.

## 6. CONCLUSION

In this work, the suitability of  $\alpha$ - $\mu$ , Rice and Nakagami-m distributions was investigated in order to describe the small-scale fading statistics of indoor THz wireless channels. Also, the empirical EC of the measured links was presented and compared to the one achieved by means of the employed analytical distributions. Moreover, useful observations about the ranges and the values of the extracted distributions parameters were made for the LoS and NLoS indoor THz wireless transmission scenarios. The fitting accuracy of the examined distributions was performed by means of the KS, KL, lgKS and RMSE metrics. These metrics revealed that, in LoS transmission conditions the Rice distribution should be employed to model the small-scale fading statistics of the THz channel, whereas in NLoS scenarios  $\alpha$ - $\mu$  is the most accurate. The fitting accuracy metrics revealed that the Nakagami-m cannot be employed to describe the small-scale fading statistics of the investigated links. Meanwhile, the comparison of two LoS links showed that the one with the better channel conditions has greater values for the parameters  $\mu$ ,  $m$  and  $K$  and a lower value of  $\alpha$ . The comparison of two NLoS links showed that, the one with the better channel conditions yields greater values for the parameters  $\alpha$ ,  $m$  and  $K$  and a lower value for  $\mu$ . By comparing two LoS or NLoS links in terms of the achieved empirical EC it is revealed that, the one having better channel conditions achieves higher EC. Meanwhile, the analytical distribution that leads to the most accurate fit to the empirical

channel gain PDFs and CDFs yields also EC values closer to the empirical ones.

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