Multi-dimensional signal mapping technique for satellite communications
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Multi-dimensional signal mapping technique for satellite communications
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(2014)

1 Introduction

This Report proposes two techniques to increase the spectrum efficiency of satellite communications. These techniques differ from the conventional orthogonal polarization multiplexing (OPM) scheme such as the one shown in Report ITU-R M.2175 [1], by multiplexing/modulating more than two data streams onto the vertical (V) and horizontal (H) polarizations.

The Report shows that the total transmit power can be reduced by up to about 2.3 dB at BER $10^{-4}$ and maintain the same spectral efficiency as OPM. The proposed schemes are flexible in that they can be applied to many different modulation formats and spectrum configurations. The particular scheme can be selected based on the required spectral efficiency and operating SNR region. The concepts of the two schemes are first described, then, the spectrum usage and the results of a computer simulation, indoor laboratory and actual satellite measurements are revealed.

2 Concept of multi-dimensional signal mapping

Two types of multi-dimensional signal mapping are described. The first technique is termed poly-polarization multiplexing (PPM) and the second scheme is termed polarization domain modulation (PDM).

2.1 Poly-Polarization Multiplexing (PPM)

Figure 1 shows the basic concept of the proposed PPM scheme [2-4]. Input data is split into $M$ data streams and each data stream is allocated to a certain polarization plane whose angle is different from all others. In the case of three data streams (termed ʻ3PMʼ), the 3rd data stream is at a polarization angle half-way between that of the V and H axis. The projection of its vertical (V) and horizontal (H) component signals is then made onto the two physical V and H channels respectively. When superposed signals of projected components are transmitted from V and H polarization antennas, the virtual additional polarization planes can be recovered. The transmitted signals, $S_H(t)$ and $S_V(t)$ on H and V polarization antennas shown in Fig. 1 are expressed by (1).

$$\begin{bmatrix} S_H(t) \\ S_V(t) \end{bmatrix} = \sum_{m=1}^{M} \begin{bmatrix} \cos \varphi_m \\ \sin \varphi_m \end{bmatrix} P_m(t)$$

(1)

where:

- $M$: number of polarizations multiplexed
- $m$: polarization index
- $A_m$, $\varphi_m$ and $P_m$: amplitude, polarization angle and modulated signal of $m$-th virtual polarization plane, respectively.

Note that equation (1) is a case that all virtual polarization signals are projected onto V and H polarizations in-phase.
Meanwhile, when each virtual polarization signal is projected onto an arbitrary phase, equation (1) can be rewritten as equation (2).

\[
\begin{bmatrix}
S_H(t) \\
S_V(t)
\end{bmatrix} = \sum_{m=1}^{M} \left( \begin{bmatrix} \alpha_m \\ \beta_m \end{bmatrix} P_m(t) \right)
\]

(2)

where \(\alpha_m\) and \(\beta_m\) are complex coefficients. Equation (2) gives a general formula of the proposed PPM transmitter as shown in Fig. 2(a).

The estimated symbol \(P_m(t)\) at the receiver is calculated from \(R_H(t)\), \(R_V(t)\) using maximum likelihood detection (MLD) (see Fig. 2(b)) as per equation (3).

\[
\tilde{P}_m(t) = \arg\min_{1 \leq n \leq 2^N} \left\| R_H(t) - \tilde{R}_H(n) \right\|^2 + \left\| R_V(t) - \tilde{R}_V(n) \right\|^2
\]

(3)

\[
\begin{bmatrix}
\tilde{R}_H(n) \\
\tilde{R}_V(n)
\end{bmatrix} = \sum_{m=1}^{M} \left( \begin{bmatrix} \alpha_m \\ \beta_m \end{bmatrix} X_m(n) \right)
\]

(4)

where:

- \(n\): candidate symbol index on the H and V planes
- \(N\): number of bits per symbol
- \(X_m(n)\): \(n\)-th candidate symbol and the received signal is given by equation (4).
An optimum coefficient set, $\alpha_m$ and $\beta_m$, was searched by using the generalized reduced gradient (GRG) algorithm. The search range was $[-1 \leq \alpha \leq 1]$ and $[-1 \leq \beta \leq 1]$ and proceeded in steps of 0.00001. The optimized set had a minimum Euclidean distance ($D_{\text{min}}$) of 0.7071 and compares with 0.5412 for OPM-8PSK (see Table 1). This increase in $D_{\text{min}}$ is the reason for the improved BER performance. The I-Q constellation points for the proposed scheme are shown in Fig. 3.

**TABLE 1**

<table>
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<th>Signal set</th>
<th>Streams</th>
<th>Minimum Euclidean distance ($D_{\text{min}}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>OPM (8PSKx2)</td>
<td>2 (H/V)</td>
<td>0.5412</td>
</tr>
<tr>
<td>PPM</td>
<td>3</td>
<td>0.7071</td>
</tr>
</tbody>
</table>

**FIGURE 3**
Composite constellations diagram (a) Vi-Vq-Hi, (b) Hi-Hq-Vq

### 2.2 Polarization Domain Modulation (PDM)

The PDM transmitter converts the input data into parallel streams and maps a component of each signal onto orthogonal streams. An extra information stream is transmitted by controlling the polarization phase and a general constellation is shown in Fig. 4(a). The modulation scheme is referred to as $SP$-$BQAM$ where $S$ indicates the number of polarization states and $B$ is the modulation level. A simple case of 2P-4QAM ($S = 2$ and $B = 4$) is used to explain the concept as shown in Fig. 4(b). The polarization angle in 2P-4QAM is ±45 degrees and candidate signal points for different polarization angles are also shown. The combination of the I-Q data points and the polarization phase conveys the information.
The polarization angle is the angle relative to the H plane. At any one instance in time only one symbol is transmitted and in the case of 2P-4QAM, eight candidate I-Q points convey three data bits (i.e. \( \log_2(S) + \log_2(B) \)) (see Fig. 4(b)). The PDM transmitter is shown in Fig. 5. The serial input data is converted into parallel streams and mapped onto the H and V planes according to equations (5a) and (5b).

\[
\begin{align*}
S_H(t) &= I_b(t) \cos(\theta_s(t)) + jQ_b(t) \cos(\theta_s(t)) \\
S_V(t) &= I_b(t) \sin(\theta_s(t)) + jQ_b(t) \sin(\theta_s(t))
\end{align*}
\]

(5a) (5b)

where:

\( \theta_s(t) \): polarization angle relative to the H plane

\( I_b(t) + jQ_b(t) \): modulator output at time \( t \).
3 Spectrum usage

Figure 6 shows an overview of the spectrum usage of the proposed multiplexing scheme. Figure 6(a) shows the concept where the signals are mapped onto both V and H polarizations in the same spectrum band. Figure 6(b) shows the configuration where the V and H planes are staggered and Fig. 6(c) shows an alternative format where the two signal components are transmitted on the same polarization but different centre frequencies. In all cases the spectrum shape and bandwidths are the same. Clearly, it is not possible to form virtual polarization planes with configurations (b) and (c), however, the pairs of signals can be used to convey the transmitted information as in (a). This means the scheme is compatible with a range of other frequency division multiple access (FDMA) based schemes.

4 Performance evaluation

A software simulation was conducted to compare the performance of the proposed schemes with that of a comparable conventional OPM system achieving the same spectral efficiency (see Table 2). The results were also compared with those from actual hardware measurements in an indoor trials campaign. The system parameters are shown in Table 3. The hardware measurement results naturally include an arbitrary timing offset due to the random start-up state.

For PPM, the performance is compared to an OPM one with two streams of 8PSK, which achieves a total of 6 bit/s/Hz efficiency. In the case of PDM, it is compared with an OPM scheme consisting of QPSK on V and BPSK on H achieving 3 bit/s/Hz efficiency. In each case, the total transmission power was set at the same value.

The BER results show that the proposed PPM scheme reduces the required SNR by about 1.6 dB at the BER of $10^{-4}$ compared to the conventional OPM scheme. The results are independent of frequency offsets (see Fig. 7(a)) or phase offsets (see Fig. 7(b)). The small difference between the simulation and hardware results is attributed to the initial timing synchronization algorithm. Similarly, the proposed PDM scheme provides an SNR gain of 2.3 dB at the BER of $10^{-4}$ (see Fig. 8).

Actual satellite field experiments were additionally conducted in the 14/12 GHz band. The results of the software simulation (subscript ‘Sim’), laboratory (subscript ‘Labo’) and satellite (subscript ‘Sat’) are compared in Fig. 9 for both PPM (6-bit) and PDM (3-bit). It can be seen that the satellite results closely follow those of the indoor laboratory results showing that the technique works in a practical satellite channel.
TABLE 2
Modulation overview

<table>
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<tr>
<th>Polarization Scheme</th>
<th>OPM (8PSKx2)</th>
<th>PPM 3PM</th>
<th>OPM (QPSK+BPSK)</th>
<th>PDM 2P-4QAM</th>
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<tr>
<td>Number of streams</td>
<td>2</td>
<td>3</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>Stream modulation</td>
<td>8PSK (3-bit)</td>
<td>QPSK (2-bit)</td>
<td>QPSK (2-bit) BPSK (1-bit)</td>
<td>2P-4QAM</td>
</tr>
<tr>
<td>Spectral efficiency (bit/s/Hz)</td>
<td>6 (3-bit by 2 streams)</td>
<td>6 (2-bit by 3 streams)</td>
<td>3</td>
<td>3</td>
</tr>
</tbody>
</table>

TABLE 3
System parameters

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<th>Value</th>
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<tr>
<td>Symbol rate</td>
<td>1.6 MBaud</td>
</tr>
<tr>
<td>Data length</td>
<td>2 304 symbol/frame</td>
</tr>
<tr>
<td>UW length</td>
<td>256 symbol/frame</td>
</tr>
<tr>
<td>Roll-off factor</td>
<td>0.2</td>
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<tr>
<td>Detection</td>
<td>MLD</td>
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</tbody>
</table>

FIGURE 7
BER performances – 3PM (a) Frequency offsets, (b) Phase offsets
FIGURE 8
BER performances – PDM (a) Frequency offsets, (b) Phase offsets

FIGURE 9
Comparison of simulation, laboratory and satellite experiments for both PPM (6-bit) and PDM (3-bit)
5 Conclusion

This Report proposes the PPM and PDM schemes that reduce the required transmit power by about 1.6-2.3 dB, respectively, compared to the OPM scheme for the same spectral efficiency. The proposed techniques were tested and verified in both the laboratory and over a real satellite channel. The choice of scheme depends on the required operating SNR region.

References


