## **RECOMMENDATION ITU-R S.1713-1**

## Methodology to calculate the minimum separation angle at the Earth's surface between a non-geostationary HEO-type FSS satellite in its "active" arc and a geostationary satellite

(Question ITU-R 241/4)

(2005-2007)

#### Scope

This Recommendation provides methodologies to calculate the minimum separation angle anywhere on the Earth's surface between a high Earth orbit (HEO) satellite in its "active" arc and:

- a) all visible locations in the GSO arc;
- b) a *specific* GSO satellite.

The first methodology (see Annex 3) is useful for determining if a HEO system complies with the equivalent power flux density (epfd) limits in frequency bands where Radio Regulations Article 22 epfd limits apply. The second (see Annex 5) is useful for interference assessment between a *specific* GSO network and a HEO-type FSS satellite.

The ITU Radiocommunication Assembly,

#### considering

a) that in the great majority of HEO satellite system designs, the apogee for each satellite occurs at the highest latitude point in its orbit, and each satellite transmits only while it is within an "active" arc around the apogee;

b) that the key parameter to determine the worst case of interference between a HEO system and a GSO system is the minimum separation angle at which an active HEO satellite is seen by any earth station operating with a GSO satellite;

c) that the angle subtended at the Earth's surface between a HEO satellite and a point in the GSO varies with the latitude and longitude of the point on the Earth's surface. Thus the separation angle at an earth station in a GSO network between the satellite to which it is operating and a HEO satellite varies with the latitude and longitude of that earth station;

d) that the determination of the minimum separation angle between a HEO system and a GSO network would facilitate rapid preliminary assessments of the potential for a HEO system to share a band with GSO systems;

e) that in frequency bands where Radio Regulations (RR) Article 22 epfd limits apply, non-GSO systems, including HEO systems, are obliged to meet the epfd↓ limits everywhere on the Earth's surface taking into account downlinks from every visible location in the GSO arc (whether or not a GSO satellite currently exists at the worst-case longitude);

f) that for HEO systems described in *considering* a) operating in frequency bands where RR Article 22 epfd limits apply, the maximum epfd corresponds to the minimum separation angle at the Earth's surface between a HEO satellite in its active arc and the worst-case GSO longitude and

occurs when a HEO satellite is at the beginning or end of its active arc (i.e. lowest latitude point in the active arc);

g) that in frequency bands where RR Article 22 epfd limits do not apply, frequency sharing between a HEO system and a specific GSO network generally requires calculation of the minimum separation angle at the Earth's surface between a HEO satellite in its active arc and the location of the specific GSO satellite;

h) that for HEO systems described in *considering* a), the calculation indicated in *considering* g) results in a minimum separation angle at the Earth's surface between a HEO satellite in its "active" arc and the specific GSO satellite that does not necessarily occur when the HEO satellite is at the beginning or end of its "active" arc,

#### recommends

1 that the methodology described in Annex 1 may be used to compute the separation angle at which a given HEO satellite in its active arc is "seen" from a given earth station operating with a given GSO satellite, and then to compute the minimum separation angle at the Earth's surface taking into account all possible earth station locations and all possible GSO satellite longitudes;

2 that Annex 2 may be used to determine the increase in noise temperature of the GSO link due to interference from the HEO satellite;

**3** that the methodology described in Annex 5 may be used to compute the minimum separation angle at which a given HEO satellite in its "active" arc is "seen" from a given earth station operating to a specific GSO satellite.

NOTE 1 – Annex 3 applies iteratively the methodologies contained in Annexes 1 and 2 to determine the minimum separation angle at which an active satellite in a given HEO system can be seen by any earth station operating to any GSO satellite, and thus calculates the worst case of increase in noise temperature of the GSO link.

NOTE 2 – Annex 4 gives examples of the application of Annexes 1 to 3.

NOTE 3 – Annex 6 gives examples of the application of Annex 5.

## Annex 1

## Method for calculating the minimum angle, subtended at the Earth's surface, between a HEO satellite within its active arc and the visible portion of the geostationary orbit

Figure 1 is a two-dimensional illustration of the path taken by a satellite orbiting the Earth. In general this will be an elliptical orbit, where one of the two focal points is coincident with the Earth's centre of gravity, O, and the orbit plane is inclined with respect to the Earth's Equatorial plane. (The GSO is a special case, in which the ellipse becomes a circle in the Equatorial plane.)

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#### FIGURE 1

Plane geometry of an elliptical orbit



In most HEO systems a satellite in such an orbit will transmit (and receive) only while it is within a limited arc containing the apogee, A, and hence will cause (or suffer) interference only while it is within that arc, which is commonly termed the active arc. The great majority of HEO systems are designed so that the apogee is the highest latitude point within the orbit, and in such cases the maximum interference levels potentially occur when a satellite is at the beginning or the end of its active arc. The length of the active arc varies from system to system. In Fig. 1 the start of the active arc is shown as s, and the end as e. The orbit dynamics are such that the satellite travels rapidly in the region of the perigee, P, and relatively slowly in the region of the apogee. (In fact the area swept out by radius vector, r, per unit of time, i.e.  $(r^2/2)(\delta\theta/\delta t)$ , is constant throughout the orbit.)

Step 1: The first step here is to determine the length Os from the basic orbit characteristics.

Information normally provided to ITU-R concerning a HEO system includes the following: apogee height (AB (km)); perigee height (PL (km)); eccentricity,*e*; inclination; *i* degrees; true anomaly of start (and end) of active arc (angle POs in Fig. 1, i.e.  $180^\circ - \theta^\circ$ ).

As an alternative to the true anomalies of s and e, the time periods for the satellite to travel from s to apogee and from apogee to e are often given, e.g.  $\pm 4$  h. In such cases the value of  $\theta$  may be deduced, either by setting up a time-step simulation to determine it, or by integration based on the fact that  $(r^2/2)(\delta\theta/\delta t)$  is constant, but both options are relatively complex. For ITU-R studies it is usually more convenient for either the true anomaly of s (or e), or angle  $\theta$ , to be given explicitly, and this is assumed here; however, the electronic version of the EXCEL spreadsheet appended to this Recommendation contains a visual basic routine to determine  $\theta$  from the time before apogee at which the satellite reaches s (or the time after apogee at which the satellite reaches e).

It may be noted that the information required by RR Appendix 4 to be supplied when any filing for a non-GSO satellite system is submitted to the Radiocommunication Bureau includes the apogee and perigee heights and the eccentricity, but currently the active arc limits, which are relevant only for non-GSO systems of the HEO class, are not listed in the data to be supplied. However, for non-GSO systems (implicitly including HEOs) planned to use bands in which RR Article 22 epfd limits apply, one of the parameters required by RR Appendix 4 is the minimum height above the Earth's surface at which any satellite in the system transmits. For a HEO satellite this is sC in Fig. 1.

From Fig. 1, using the equation of an ellipse and plane trigonometry, a quadratic equation for x in terms of AB, PL, e and  $\theta$  may be formed, and solved for x, and length Os may then be found from triangle Oms.

#### FIGURE 2

#### Plane triangle extracts



Step 2: The next step is to find the latitude of s and its longitude relative to the simultaneous apogee longitude, which may be done using Fig. 3. This is a three-dimensional representation of the orbit, using the same symbols as in Fig. 1 – so Os is as calculated in Step 1. By applying the spherical Cosine Rule to spherical triangles OBCD and CODF in Fig. 3, and then applying the spherical Sine Rule to spherical triangle ONBC, it may be deduced that the longitude of s relative to A ( $\alpha_c$ ) and its latitude ( $\lambda_c$ ) are given by:

$$\alpha_C = -\angle FOD = -\tan^{-1}(\tan(\theta)/\cos(i))$$
 and  $\lambda_C = \angle FOC = \cos^{-1}(\sin(\theta)/\sin(\alpha_c))$ 





Step 3: Having found the latitude and instantaneous relative longitude of s, the corresponding interference separation angle ( $\varphi$ ) at any earth station, E, operating to any geostationary satellite, G, may be calculated using Fig. 4, in which points C, O, F, N and s are identical to those in Fig. 3. Thus in Fig. 4 the latitude of E is  $\lambda_E$  and its longitude relative to the longitude of A is  $\alpha_E$ , and the longitude of G relative to the longitude of A is  $\alpha_G$ . Then, since  $\alpha_C$ ,  $\alpha_E$ ,  $\lambda_C$ ,  $\lambda_E$ ,  $\alpha_G$ , OE (Earth's radius), OG (GSO radius) and Os are known or have been calculated,

- by applying the spherical Cosine Rule to spherical triangle ONCE, and then applying the plane Cosine Rule to plane triangle OsE, the length sE may be calculated;
- by applying the spherical Cosine Rule to spherical triangle OCFJ, and then applying the plane Cosine Rule to plane triangle OsG, the length sG may be calculated; and
- by applying the spherical Cosine Rule to spherical triangle OEJK, and then applying the plane Cosine Rule to plane triangle OEG, the length EG may be calculated.

And finally in plane triangle EsG, since the three sides sE, sG and EG have now been calculated, the angle  $\phi$  may be found by using the plane Cosine Rule.

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#### FIGURE 4





Thus, by employing this procedure, the interference separation angle,  $\varphi$ , may be calculated for any GSO downlink (i.e. for an earth station in any geographical location receiving from a GSO satellite on any longitude), if the HEO inclination angle, apogee height, perigee height, eccentricity, and either the true anomaly or the time relative to apogee of the start (or end) of the active arc are known.

To find the minimum value of  $\varphi$  a simple computer program may be written to cycle through a range of combinations of  $\alpha_E$ ,  $\lambda_E$  and  $\alpha_G$ , employing the above procedure to calculate  $\varphi$  for each combination, and then select the lowest value. Since interference can occur only for combinations of  $\alpha_E$ ,  $\lambda_E$  and  $\alpha_G$  for which E is visible to both G and s (see Fig. 4), but all such combinations must be investigated, it is convenient to arrange for the simple program to include wide ranges of the three variables and then to exclude from the reckoning any combinations where E is obscured by the Earth from either G or s or both G and s. This is illustrated in the plane triangle extracts from Fig. 4 shown in Fig. 2.

#### Annex 2

# Calculation of increase in GSO link noise due to interference from a HEO satellite at the start of its active arc

From Fig. 4 it can be seen that interference from a HEO satellite at s to the link between a geostationary satellite at G and an earth station at E will enter that earth station's receiver via a side lobe of its antenna pattern. The corresponding increase in noise temperature of the GSO link is given by:

$$10\log((\Delta T/T)/100) = E_1 - 20\log(4\pi d/\lambda) + G(\varphi) - 10\log(kT)$$
 dB

where:

 $\Delta T/T$ : link noise increase expressed as a percentage

- $E_1$ : e.i.r.p. density of carrier transmitted by HEO satellite (dB(W/Hz))
  - *d*: length of interference path sE (m)
  - $\lambda$ : wavelength (m) = (0.3)/f where f is the HEO carrier frequency (GHz)
- $G(\varphi)$ : receive gain of earth station antenna at frequency f and at off-axis angle  $\varphi$  (dBi)
  - *T*: noise temperature of GSO link (K)
  - *k*: Boltzmann's constant, i.e.  $10\log(k) = -228.6 \text{ dB}(W/\text{Hz/K})$ .

T may be either the noise temperature of the GSO downlink alone, or the GSO system noise temperature referred to the earth station receiver input, depending on how it is preferred to express  $\Delta T/T$ .

For the calculation of  $G(\varphi)$ , since the methodology in this Annex relates to interference between non-GSO and GSO systems it is appropriate to employ the gain patterns prescribed in Recommendation ITU-R S.1428, where  $G(\varphi)$  is expressed in terms of  $D/\lambda$  and D is the antenna diameter (m).

#### Annex 3

#### **Iterative implementation of the methodology in Annex 1**

In the attachment ("MinseparationHEOangle") to this Annex the procedure developed in Annex 1 is implemented in an EXCEL spreadsheet, which contains Visual Basic routines to cycle through all combinations of earth station latitude and longitude and GSO satellite longitude for which both the GSO satellite and the start of a HEO system active arc are simultaneously visible, and thus identify the minimum separation angle at any earth station for which mutual interference could occur. For the convenience of the user the simple steps described in Annex 2 are incorporated into the spreadsheet to provide an output giving the maximum value of  $\Delta T/T$  due to that interference if required. As is evident from the examples in Annex 4, the spreadsheet covers all types of orbit in which a limited active arc is employed, provided that the arc does not intersect any line between the GSO and the Earth's surface at latitude ±81.3°.

The only input data required are the following parameters of the HEO system:

- height of apogee (km);
- height of perigee (km);

- eccentricity (as a decimal fraction);
- orbit inclination angle (degrees);
- one (or more) of three parameters to define the start s (or end "e") of the active arc, i.e.:
  - either geocentric angle between s and apogee (degrees),
  - or time taken for a satellite to move between s and apogee  $(h)^1$ ,
  - or height of s (km).

If the user wishes the corresponding value of  $\Delta T/T$  to be calculated the following additional input parameters are needed:

maximum HEO satellite e.i.r.p. density (dB(W/Hz));

and the following parameters of the GSO link:

- diameter (m) of the antenna in the earth station of the GSO link;
- receive gain pattern of the antenna in the earth station of the GSO link (dBi vs. angle off-axis);
- noise temperature of GSO link (K);
- frequency (GHz).



## Annex 4

## **Examples of application of the methodology of Annex 1**

In its 2nd to 8th rows, Table 1 below lists the orbital characteristics of 12 different designs of HEO systems compiled from information contributed to ITU-R. To illustrate such systems their types of Earth tracks are compared in Figs. 5 to 7. The 11th row of Table 1 gives the apogee longitudes used in preparing Figs. 5 to 7; these apogee longitudes have been selected solely for convenience of illustration and no other significance is intended here.

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<sup>&</sup>lt;sup>1</sup> The attachment includes an additional Visual Basic routine in order to make use of this item of data, if it is entered. In that case, not only is the minimum separation angle calculated, but the absolute locations of earth station and GSO satellite for which that angle obtains are also calculated, provided that the longitude of the HEO apogee is entered as an additional input. See associated EXCEL file labelled "MinseparationHEOangle".

											1		
1.	HEO system	1	2	3	4	5	6	7	8	9	10	11	12
2.	Apogee height (km)	35 970	44 640.5	39 000	35 800	52 700	40 000	50 400	27 288.3	20 180	47 669	39 300	27 470
3.	Perigee height (km)	4 500	26 931.5	500	35 800	18 900	31 600	21 200	517.4	20 180	9 312.9	1 075	310
4.	Orbit eccentricity	0.59	0.21	0.74	0	0.4	0.1	0.347	0.66	0	0.55	0.72	0.67
5.	Orbit inclination (degrees)	50	42.5	63.43	63.4	60	40	63.4	63.435	63.4	45	63.4	45
6.	Angle of s with respect to the apogee (degrees)	35	31	(29.5)	60	(30)	37	(24)	40	(30)	(36)	25	(28)
7.	Time of s with respect to the apogee (h)	(-3.13)	(-3)	-3.5	(-4)	-4	(-2.95)	-3	(-2.55)	-1	(-4.5)	(-3.06)	-2
8.	Height of s (km)	(27 200)	(42 800)	(26 900)	N/A	(48 000)	(39 000)	(47 900)	(16 500)	N/A	(37 800)	(30 700)	(21 400)
9.	Minimum separation angle (degrees)	39.84	35.84	52.58	26.94	49.35	31.34	55.49	40.66	51.84	35.47	55.55	37.73
10.	Check using simulation (degrees)	(39.78)	(35.78)	(52.50)	(26.86)	(49.25)	(31.40)	(55.47)	(40.91)	(51.86)	(35.51)	(55.49)	(37.26)
11.	Apogee longitude (degrees E)	-150	-108	-62	-43	-130	-38	-110	-83	-30	-18	27	57
12.	Earth station longitude (degrees E)	-117.63	-110.81	14.89	17.33	-43.32	38.65	-34.89	-75.38	-35.33	79.63	101.86	82.72
13.	Earth station latitude (degrees N)	73.63	-46.70	3.72	-7.73	-3.15	-5.44	-2.01	73.63	73.63	-5.44	2.58	73.63
14.	GSO satellite longitude (degrees E)	-150.29	-102.22	-61.32	-58.88	-119.52	-37.55	-111.09	-108.04	-67.99	3.42	25.66	50.06
15.	Example $\Delta T/T$ (%) <sup>(1)</sup>	0.204	0.072	0.150	0.200	0.058	0.108	0.058	0.572	0.386	0.043	0.122	0.312

TABLE 1

<sup>(1)</sup> Values calculated via Annex 2 for  $E_1 = -21$  dB(W/Hz), D = 3 m, T = 100 K, f = 11 GHz and  $G(\varphi)$  from Recommendation ITU-R S.1428-1. N/A: not available.

The 6th, 7th and 8th rows are different ways of stating the start (or end) of the active arc. In these three rows the unbracketed values are those contributed to ITU-R; the bracketed values were obtained from computer simulation of each of the systems, pausing each run at the unbracketed value and noting the two corresponding bracketed values. The results in the 9th row were determined from Annex 3 using the unbracketed values to determine the start of the active arc. (When the bracketed values were used in Annex 3 the results were marginally different, but the differences were within the accuracy of the computations performed). A check on each result was performed via computer simulation, yielding the minimum separation angles shown in italics in the 10th row; as can be seen, these are in close accord with the values in the 9th row and thus confirm the validity of Annex 3.

Additionally, based on the apogee longitudes in the 11th row, the combination of earth station and GSO satellite locations for which the minimum off-axis angle would occur in each case was obtained using Annex 3, and these are given in the 12th, 13th and 14th rows of Table 1.



#### FIGURE 5

Parts of Earth tracks of HEO systems 1 to 4, showing active arcs (i.e. above --)

#### FIGURE 6









Finally, the availability of Annex 3 provides a means to verify the truth of *considering* c) in example cases. This was done for systems 1, 4 and 8 with the aim of broadly spanning the system types, by finding the minimum off-axis (or separation) angle for progressively reduced values of the geocentric angle,  $\theta$ , between a HEO satellite and apogee. The results are shown graphically in Fig. 8.



FIGURE 8 Variation of minimum off-axis angle with HEO satellite distance from apogee

Figure 8 clearly demonstrates that, for typical HEO systems, the further a satellite is from the apogee of its orbit the smaller is the minimum off-axis angle at which it is seen by earth stations

theoretically operating to a geostationary satellite located at the worst-case longitude in the GSO arc for that particular HEO satellite's orbit.

### Annex 5

## Method for calculating the minimum angle, subtended at the Earth's surface within the footprint of a beam of a geostationary satellite at a given longitude, between that satellite and a HEO satellite within its active arc

#### **1** Plane geometry of an elliptical orbit

Figure 9 shows a two-dimensional illustration of the path taken by a HEO satellite orbiting the Earth. The parameters often used to define the instantaneous location of such a satellite within its orbit, i.e. the mean anomaly, M, the eccentric anomaly, E, and the true anomaly, f, are given by the following expressions<sup>2</sup>, where the symbols are as defined below:

 $M = 2\pi t/T \text{ rad}$   $M = E - e \sin(E) \text{ rad} \quad \text{(Kepler's equation)}$  $f = 2 \tan^{-1}(\{(1 + e)/(1 - e)\}^{0.5} \tan(E/2)) \text{ rad}$ 

Also, it may be deduced that the length L between an "active" HEO satellite and the Earth's centre of gravity is given by:

 $L = a \left( 1 - e \cos(E) \right) \quad \text{km}$ 

<sup>&</sup>lt;sup>2</sup> See Annex 1 of Recommendation ITU-R S.1529.



#### 2 Calculation of geographical coordinates of an "active" HEO satellite

By applying the method in Step 2 of Annex 1, the latitude,  $\lambda_C$  and relative longitude,  $\alpha_C$ , of an "active" HEO satellite may be calculated. Also, its absolute longitude,  $\alpha$ , is given by:

 $\alpha = \alpha_c + \alpha_{apogee} - \omega_E(t - t_{apogee}) \qquad \text{rad}$ 

t<sub>apogee</sub>: time at apogee (s)

 $\alpha_{apogee}$ : longitude of apogee (rad).



FIGURE 10 Geographical coordinates of HEO satellite

#### **3** Calculation of minimum separation angle

By employing the method in Step 3 of Annex 1, the separation angle,  $\varphi$ , between an "active" HEO satellite and a specific GSO satellite may be calculated for an earth station in any geographical location receiving from the GSO satellite, if HEO inclination angle, apogee height, perigee height, eccentricity, longitude of apogee, and GSO longitude are known.





Note that in Annex 1,  $\alpha_E$  and  $\alpha_G$  are relative to  $\alpha_C$  whereas in Annex 5 they indicate the absolute longitudes of E and G, respectively.

To find the minimum value of  $\varphi$ , a computer program may be written to cycle through a range of combinations of  $\alpha_E$ ,  $\lambda_E$  and *t*, employing the procedure of Step 3 of Annex 1 to calculate  $\varphi$  for each combination, and then select the lowest value.

Because interference can occur only for combinations of  $\alpha_E$ ,  $\lambda_E$  and *t* for which the earth station is visible to both the HEO satellite and the GSO satellite, but all such combinations must be investigated, it is convenient to arrange for the program to include wide ranges of the three variables and then exclude from the reckoning any combinations where the earth station is obscured by the Earth from either the GSO satellite or the HEO satellite or from both satellites. This is illustrated in Fig. 2.

For cases where the GSO satellite does not use a global coverage beam, the combinations for which the GSO earth station would be outside of the usable beamwidth of the GSO satellite should also be excluded.



FIGURE 12 Minimum separation angle between HEO and GSO satellites for non-global beam case

Also,  $\Delta T/T$  may be calculated by employing the methodology of Annex 2.

## Annex 6

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## **Examples of applying of the methodology of Annex 5**

Table 2 shows the results determined from Annex 5 for the 12 different designs of HEO systems listed in Table 1.

		-	0				-			0		
1. HEO system	1	2	3	4	5	6	7	8	9	10	11	12
2. Apogee height (km)	35 970	44 640.5	39 000	35 800	52 700	40 000	50 400	27 288.3	20 180	47 669	39 300	27 470
3. Perigee height (km)	4 500	26 931.5	500	35 800	18 900	31 600	21 200	517.4	20 180	9 312.9	1 075	310
4. Orbit eccentricity	0.59	0.21	0.74	0	0.4	0.1	0.347	0.66	0	0.55	0.72	0.67
5. Orbit inclination (degrees)	50	42.5	63.43	63.4	60	40	63.4	63.435	63.4	45	63.4	45
6. Apogee longitude (° E)	-150	-108	-62	-43	-130	-38	-110	-83	-30	-18	27	57
7. Period of active-arc (h)	6.26 <sup>(1)</sup>	6 <sup>(1)</sup>	7 <sup>(1)</sup>	8(1)	8(1)	5.9 <sup>(1)</sup>	6 <sup>(1)</sup>	5.1 <sup>(1)</sup>	2 <sup>(1)</sup>	9 <sup>(1)</sup>	6.12 <sup>(1)</sup>	4 <sup>(1)</sup>
8. GSO satellite longitude (° E)	135	135	135	135	135	135	135	135	135	135	135	135
9. Minimum separation angle (degrees)	80.5	109.6	118.6	120.2	87.4	145.4	102.5	112.6	118.2	126.7	100.2	78.5
10. Earth station longitude (° E)	-153	76	60	-150	66	60	62	-149	59	-165	-152	-162
11. Earth station latitude (° N)	-40	62	24	18	45	22	34	-7	-6	61	35	58
12. HEO satellitelongitu de (° E)	-150.3	-114.1	-62	-43	-141.3	-38.1	-112.0	-96.8	3.7	2.6	27.3	63.4
13. HEO satellite latitude (° N)	38.9	35.4	63.4	63.4	48.8	40.0	62.4	59.5	54.1	36.6	63.2	38.8

#### TABLE 2

Minimum separation angles in the case of an example GSO with a global beam

<sup>(1)</sup> These values were obtained by doubling the values in the 7th row of Table 1.

Also, Figs. 13, 14 and 15 show the results of finding the minimum separation angle for each true anomaly for example HEO systems 1, 4 and 8, respectively. These results show that the minimum separation angle between an "active" HEO satellite and a specific GSO satellite varies with the GSO satellite's longitude. Furthermore, these results demonstrate the truth of *considering* h). In this regard it may be noted that apogee occurs at a true anomaly of 180°, and that the curves in each Figure extend from the true anomaly at the start of the active arc to the true anomaly at the end of the active arc.

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#### FIGURE 14

Minimum separation angle versus true anomaly of "active" satellite of HEO system 4





Table 3 shows an example of the elliptical beam footprint of the GSO satellite at 135° E. Table 4 shows the results of finding the minimum separation angle between example HEO system 4 and the GSO satellite at 135° E that has the beam footprint shown in Table 3. Also, Fig. 16 shows the minimum separation angle for each true anomaly in this case.

#### TABLE 3

Longitude (° E)	Latitude (° N)	Longitude (° E)	Latitude (° N)	Longitude (° E)	Latitude (° N)
75.7	39.9	74.3	6.3	103.0	29.5
73.3	37.4	77.7	4.8	104.0	32.5
71.1	34.8	81.8	4.4	104.6	35.5
69.1	32.2	85.7	5.4	104.8	38.6
67.8	29.2	88.7	7.5	104.0	41.6
67.2	26.1	91.3	9.9	101.7	44.1
66.9	23.1	93.7	12.4	98.1	45.6
66.7	20.1	95.7	15.1	94.0	46.1
67.0	17.0	97.3	17.9	89.9	45.8
67.7	13.9	98.8	20.8	86.0	44.9
69.1	11.1	100.3	23.7	82.1	43.7
71.4	8.5	101.7	26.5	78.7	42.1

#### Data defining an example elliptical beam footprint of the example GSO satellite at 135° E

#### TABLE 4

## Minimum separation angle in the case of an example GSO with a non-global beam

1. HEO system	4
2. Apogee height (km)	35 800
3. Perigee height (km)	35 800
4. Orbit eccentricity	0
5. Orbit inclination (degrees)	63.4
6. Apogee longitude (° E)	-43
7. Period of active-arc (h)	8
8. GSO satellite longitude (° E)	135
9. Minimum separation angle (degrees)	122.0
10. Earth station longitude (° E)	67
11. Earth station latitude (° N)	18
12. HEO satellite longitude (° E)	-39.93
13. HEO satellite latitude (° N)	63.29

#### FIGURE 16

Minimum separation angle versus true anomaly of an "active" satellite of HEO system 4 (GSO satellite location: 135° E)



The following embedded Excel file "MinSepAnnex5" includes an additional Visual Basic routine for the methodology of Annex 5. This tool will correctly compute the minimum separation angle in both cases: a GSO with a global beam and a GSO with a non-global beam. Note that this tool will correctly compute the minimum separation angle within the footprint of a shaped beam provided the footprint does not contain concavities. In the case of a footprint containing concavities, the input data should include artificial points bridging each concavity and, in the event that a minimum

separation angle is computed to occur at a geographical location within one of the concavities, the user should assume that it occurs on the footprint contour at the point nearest to the computed point.

