# ITU-R <br> Radiocommunication Sector of ITU 

Recommendation ITU-R P.452-17
(09/2021)

## Prediction procedure for the evaluation of interference between stations on the surface of the Earth at frequencies above about $0.1 \mathbf{G H z}$

P Series
Radiowave propagation

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## RECOMMENDATION ITU-R P.452-17*

# Prediction procedure for the evaluation of interference between stations on the surface of the Earth at frequencies above about 0.1 GHz 

(Question ITU-R 208/3)

(1970-1974-1978-1982-1986-1992-1994-1995-1997-1999-2001-2003-2005-2007-2009-2013-2015-2021)

## Scope

This Recommendation contains a prediction method for the evaluation of interference between stations on the surface of the Earth at frequencies from about 0.1 GHz to 50 GHz , accounting for both clear-air and hydrometeor scattering interference mechanisms.

## Keywords

Interference, Ducting, Tropospheric scatter, Diffraction, Hydrometeor Scattering, Digital Data Products

The ITU Radiocommunication Assembly, considering
a) that due to congestion of the radio spectrum, frequency bands must be shared between different terrestrial services, between systems in the same service and between systems in the terrestrial and Earth-space services;
b) that for the satisfactory coexistence of systems sharing the same frequency bands, interference prediction procedures are needed that are accurate and reliable in operation and acceptable to all parties concerned;
c) that propagation predictions are applied in interference prediction procedures which are often required to meet "worst-month" performance and availability objectives;
d) that prediction methods are required for application to all types of path in all areas of the world,

## recommends

that the interference prediction procedure given in Annex 1 be used for the evaluation of the available propagation loss over unwanted signal paths between stations on the surface of the Earth for frequencies above about 0.1 GHz .

[^0]
## Annex 1

## 1 Introduction

Congestion of the radio-frequency spectrum has made necessary the sharing of many frequency bands between different radio services, and between the different operators of similar radio services. In order to ensure the satisfactory coexistence of the terrestrial and Earth-space systems involved, it is important to be able to predict with reasonable accuracy the interference potential between them, using propagation predictions and models which are acceptable to all parties concerned, and which have demonstrated accuracy and reliability.

Many types and combinations of interference path may exist between stations on the surface of the Earth, and between these stations and stations in space, and prediction methods are required for each situation. This Annex addresses one of the more important sets of interference problems, i.e. those situations where there is a potential for interference between radio stations located on the surface of the Earth.

The models contained within Recommendation ITU-R P. 452 work from the assumption that the interfering transmitter and the interfered-with receiver both operate within the surface layer of atmosphere. Use of exceptionally large antenna heights to model operations such as aeronautical systems is not appropriate for these models. The prediction procedure has been tested for radio stations operating in the frequency range of about 0.1 GHz to 50 GHz .
The models within Recommendation ITU-R P. 452 are designed to calculate propagation losses not exceeded for time percentages over the range $0.001 \leq p \leq 50 \%$. This assumption does not imply the maximum loss will be at $p=50 \%$.

The method includes a complementary set of propagation models which ensure that the predictions embrace all the significant interference propagation mechanisms that can arise. Methods for analysing the radio-meteorological and topographical features of the path are provided so that predictions can be prepared for any practical interference path falling within the scope of the procedure up to a distance limit of 10000 km .

## 2 Interference propagation mechanisms

Interference may arise through a range of propagation mechanisms whose individual dominance depends on climate, radio frequency, time percentage of interest, distance and path topography. At any one time a single mechanism or more than one may be present. The principal interference propagation mechanisms are as follows:

- Line-of-sight (Fig. 1): The most straightforward interference propagation situation is when a line-of-sight transmission path exists under normal (i.e. well-mixed) atmospheric conditions. However, an additional complexity can come into play when subpath diffraction causes a slight increase in signal level above that normally expected. Also, on all but the shortest paths (i.e. paths longer than about 5 km ) signal levels can often be significantly enhanced for short periods of time by multipath and focusing effects resulting from atmospheric stratification (see Fig. 2).
- Diffraction (Fig. 1): Beyond line-of-sight (LoS) and under normal conditions, diffraction effects generally dominate wherever significant signal levels are to be found. For services where anomalous short-term problems are not important, the accuracy to which diffraction can be modelled generally determines the density of systems that can be achieved. The diffraction prediction capability must have sufficient utility to cover smooth-earth, discrete obstacle and irregular (unstructured) terrain situations.

Tropospheric scatter (Fig. 1): This mechanism defines the "background" interference level for longer paths (e.g. more than $100-150 \mathrm{~km}$ ) where the diffraction field becomes very weak. However, except for a few special cases involving sensitive receivers or very high power interferers (e.g. radar systems), interference via troposcatter will be at too low a level to be significant.

FIGURE 1
Long-term interference propagation mechanisms


Surface ducting (Fig. 2): This is the most important short-term propagation mechanism that can cause interference over water and in flat coastal land areas, and can give rise to high signal levels over long distances (more than 500 km over the sea). Such signals can exceed the equivalent "free-space" level under certain conditions.

FIGURE 2
Anomalous (short-term) interference propagation mechanisms


- Elevated layer reflection and refraction (Fig. 2): The treatment of reflection and/or refraction from layers at heights up to a few hundred metres is of major importance as these mechanisms enable signals to overcome the diffraction loss of the terrain very effectively under favourable path geometry situations. Again the impact can be significant over quite long distances (up to $250-300 \mathrm{~km}$ ).
- Hydrometeor scatter (Fig. 2): Hydrometeor scatter can be a potential source of interference between terrestrial link transmitters and earth stations because it may act virtually omnidirectionally, and can therefore have an impact off the great-circle interference path. However, the interfering signal levels are quite low and do not usually represent a significant problem.

A basic problem in interference prediction (which is indeed common to all tropospheric prediction procedures) is the difficulty of providing a unified consistent set of practical methods covering a wide range of distances and time percentages; i.e. for the real atmosphere in which the statistics of dominance by one mechanism merge gradually into another as meteorological and/or path conditions change. Especially in these transitional regions, a given level of signal may occur for a total time percentage which is the sum of those in different mechanisms. The approach in this procedure has been to define completely separate methods for clear-air and hydrometeor-scatter interference prediction, as described in §§ 4 and 5 respectively.

The clear-air method consists of separate models for diffraction, ducting/layer-reflection, and troposcatter. All three are applied for every case, irrespective of whether a path is LoS or transhorizon. The results are then combined into an overall prediction using a blending technique that ensures for any given path distance and time percentage that the signal enhancement in the equivalent notional line-of-sight model is the highest attainable.

## 3 Clear-air interference prediction

### 3.1 General comments

Although the clear-air method is implemented by three separate models, the results of which are then blended, the procedure takes account of five basic types of propagation mechanism:

- line-of-sight (including signal enhancements due to multipath and focusing effects);
- $\quad$ diffraction (embracing smooth-earth, irregular terrain and sub-path cases);
- tropospheric scatter;
- anomalous propagation (ducting and layer reflection/refraction);
- height-gain variation in clutter (where relevant).


### 3.2 Deriving a prediction

### 3.2.1 Outline of the procedure

The steps required to achieve a prediction are as follows:

## Step 1: Input data

The basic input data required for the procedure is given in Table 1. All other information required is derived from these basic data during the execution of the procedure.

TABLE 1
Basic input data

| Parameter | Preferred resolution | Description |
| :---: | :---: | :--- |
| $f$ | 0.01 | Frequency (GHz) |
| $p$ | 0.001 | Required time percentage(s) for which the calculated basic <br> transmission loss is not exceeded |
| $\varphi_{t}, \varphi_{r}$ | 0.001 | Latitude of station (degrees) |
| $\psi_{t}, \psi_{r}$ | 0.001 | Longitude of station (degrees) |
| $h_{t g}, h_{r g}$ | 1 | Antenna centre height above ground level (m) |
| $h_{t s}, h_{r s}$ | 1 | Antenna centre height above mean sea level (m) |
| $G_{t}, G_{r}$ | 0.1 | Antenna gain in the direction of the horizon along the great- <br> circle interference path (dBi) |
| $P o l$ | N/A | Signal, e.g. vertical or horizontal |

NOTE 1 - For the interfering and interfered-with stations:
$t$ : interferer
$r$ : interfered-with station.
Polarization in Table 1 is not a parameter with a numerical value. The information is used in § 4.2.2.1 in connection with equations (30a), (30b) and (31).

Step 2: Selecting average year or worst-month prediction
The choice of annual or "worst-month" predictions is generally dictated by the quality (i.e. performance and availability) objectives of the interfered-with radio system at the receiving end of the interference path. As interference is often a bidirectional problem, two such sets of quality objectives may need to be evaluated in order to determine the worst-case direction upon which the
minimum permissible basic transmission loss needs to be based. In the majority of cases the quality objectives will be couched in terms of a percentage "of any month", and hence worst-month data will be needed.
The propagation prediction models predict the annual distribution of basic transmission loss. For average year predictions the percentages of time $p$, for which particular values of basic transmission loss are not exceeded, are used directly in the prediction procedure. If average worst-month predictions are required, the annual equivalent time percentage, $p$, of the worst-month time percentage, $p_{w}$, must be calculated for the path centre latitude $\varphi$ using:

$$
\begin{equation*}
p=10^{\left(\frac{\log \left(p_{w}\right)+\log \left(G_{L}\right)-0.186 \omega-0.444}{0.816+0.078 \omega}\right)} \quad \% \tag{1}
\end{equation*}
$$

where:
$\omega$ : fraction of the path over water (see Table 3).

$$
G_{L}= \begin{cases}\sqrt{1.1+|\cos 2 \varphi|^{0.7}} & \text { for }|\varphi| \leq 45^{\circ}  \tag{1a}\\ \sqrt{1.1-|\cos 2 \varphi|^{0.7}} & \text { for }|\varphi|>45^{\circ}\end{cases}
$$

If necessary the value of $p$ must be limited such that $12 p \geq p_{w}$.
Note that the latitude $\varphi$ (degrees) is deemed to be positive in the Northern Hemisphere.
The calculated result will then represent the basic transmission loss for the required worst-month time percentage, $p_{w} \%$.

## Step 3: Radiometeorological data

The prediction procedure employs three radio-meteorological parameters to describe the variability of background and anomalous propagation conditions at the different locations around the world.

- $\quad \Delta N(\mathrm{~N}$-units $/ \mathrm{km})$, the average radio-refractivity lapse-rate through the lowest 1 km of the atmosphere, provides the data upon which the appropriate effective Earth radius can be calculated for path profile and diffraction obstacle analysis. Note that $\Delta N$ is a positive quantity in this procedure.
- $\quad \beta_{0}(\%)$, the time percentage for which refractivity lapse-rates exceeding 100 N -units/km can be expected in the first 100 m of the lower atmosphere, is used to estimate the relative incidence of fully developed anomalous propagation at the latitude under consideration. The value of $\beta_{0}$ to be used is that appropriate to the path centre latitude.
- $\quad N_{0}$ (N-units), the sea-level surface refractivity, is used only by the troposcatter model as a measure of location variability of the troposcatter scatter mechanism. As the scatter path calculation is based on a path geometry determined by annual or worst-month values of $\Delta N$, there is no additional need for worst-month values of $N_{0}$. The correct values of $\Delta N$ and $N_{0}$ are given by the path-centre values as derived from the appropriate maps.
Point incidence of anomalous propagation, $\beta_{0}(\%)$, for the path centre location is determined using:

$$
\beta_{0}=\left\{\begin{array}{lll}
10^{-0.015|\varphi|+1.67} \mu_{1} \mu_{4} & \% & \text { for }|\varphi| \leq 70^{\circ}  \tag{2}\\
4.17 \mu_{1} \mu_{4} & \% & \text { for }|\varphi|>70^{\circ}
\end{array}\right.
$$

where:
$\varphi: \quad$ path centre latitude (degrees).

The parameter $\mu_{1}$ depends on the degree to which the path is over land (inland and/or coastal) and water, and is given by:

$$
\begin{equation*}
\mu_{1}=\left[10^{\frac{-d_{t m}}{16-6.6 \tau}}+\left[10^{-(0.496+0.354 \tau)}\right]^{5}\right]^{0.2} \tag{3}
\end{equation*}
$$

where the value of $\mu_{1}$ shall be limited to $\mu_{1} \leq 1$,
with:

$$
\begin{equation*}
\tau=\left[1-\mathrm{e}^{-\left(4.12 \times 10^{-4} \times d_{l m}^{2.41}\right)}\right] \tag{3a}
\end{equation*}
$$

where:
$d_{t m}$ : longest continuous land (inland + coastal) section of the great-circle path (km)
$d_{l m}$ : longest continuous inland section of the great-circle path (km).
The radioclimatic zones to be used for the derivation of $d_{t m}$ and $d_{l m}$ are defined in Table 2.

$$
\mu_{4}= \begin{cases}10^{(-0.935+0.0176|\varphi|) \log \mu_{1}} & \text { for }|\varphi| \leq 70^{\circ}  \tag{4}\\ 10^{0.3 \log \mu_{1}} & \text { for }|\varphi|>70^{\circ}\end{cases}
$$

TABLE 2
Radio-climatic zones

| Zone type | Code | Definition |
| :--- | :--- | :--- |
| Coastal land | A1 | Coastal land and shore areas, i.e. land adjacent to the sea up to an altitude <br> of 100 m relative to mean sea or water level, but limited to a distance of <br> 50 km from the nearest sea area. Where precise 100 m data are not <br> available an approximate value, i.e. 300 ft , may be used |
| Inland | A2 | All land, other than coastal and shore areas defined as "coastal land" <br> above |
| Sea | B | Seas, oceans and other large bodies of water (i.e. covering a circle of at <br> least 100 km in diameter) |

## Large bodies of inland water

A "large" body of inland water, to be considered as lying in Zone B, is defined as one having an area of at least $7800 \mathrm{~km}^{2}$, but excluding the area of rivers. Islands within such bodies of water are to be included as water within the calculation of this area if they have elevations lower than 100 m above the mean water level for more than $90 \%$ of their area. Islands that do not meet these criteria should be classified as land for the purposes of the water area calculation.

## Large inland lake or wet-land areas

Large inland areas of greater than $7800 \mathrm{~km}^{2}$ which contain many small lakes or a river network should be declared as "coastal" Zone A1 by administrations if the area comprises more than $50 \%$ water, and more than $90 \%$ of the land is less than 100 m above the mean water level.
Climatic regions pertaining to Zone A1, large inland bodies of water and large inland lake and wetland regions, are difficult to determine unambiguously. Therefore administrations are invited to register
with the ITU Radiocommunication Bureau (BR) those regions within their territorial boundaries that they wish identified as belonging to one of these categories. In the absence of registered information to the contrary, all land areas will be considered too pertain to climate Zone A2.

For maximum consistency of results between administrations the calculations of this procedure should be based on the ITU Digitized World Map (IDWM) which is available from the BR. If all points on the path are at least 50 km from the sea or other large bodies of water, then only the inland category applies.
If the zone information is stored in successive points along the radio path, it should be assumed that changes occur midway between points having different zone codes.

## Effective Earth radius

The median effective Earth radius factor $k_{50}$ for the path is determined using:

$$
\begin{equation*}
k_{50}=\frac{157}{157-\Delta N} \tag{5}
\end{equation*}
$$

Assuming the average physical Earth radius of $\alpha=6371 \mathrm{~km}$, the median value of effective Earth radius $a_{e}$ can be determined from:

$$
\begin{equation*}
a_{e}=k_{50} a \quad \mathrm{~km} \tag{6a}
\end{equation*}
$$

The effective Earth radius exceeded for $\beta_{0} \%$ time, $a_{\beta}$, is given by:

$$
\begin{equation*}
a_{\beta}=k_{\beta} a \quad \mathrm{~km} \tag{6b}
\end{equation*}
$$

where $k_{\beta}=3.0$ is an estimate of the effective Earth radius factor exceeded for $\beta_{0} \%$ time.
A general effective earth radius, $a_{p}$, will be set to $a_{e}$ for $50 \%$ time and to $a_{\beta}$ for $\beta_{0} \%$ time in $\S \S 4.2 .1$ and 4.2.2.

## Step 4: Path profile analysis

Values for a number of path-related parameters necessary for the calculations, as indicated in Table 3, must be derived via an initial analysis of the path profile based on the value of $a_{e}$ given by equation (6a). Information on the derivation, construction and analysis of the path profile is given in Attachment 2 to Annex 1.

TABLE 3
Parameter values to be derived from the path profile analysis

| Parameter | Description |
| :---: | :--- |
| $d$ | Great-circle path distance (km) |
| $d_{t t}, d_{l r}$ | Distance from the transmit and receive antennas to their respective horizons (km). |
| $\theta_{t}, \theta_{r}$ | For a transhorizon path, transmit and receive horizon elevation angles respectively <br> (mrad). For a LoS path, each is set to the elevation angle to the other terminal |
| $\theta$ | Path angular distance (mrad) |
| $h_{t s}, h_{r s}$ | Antenna centre height above mean sea level (m) |
| $h_{t e}, h_{r e}$ | Effective heights of antennas above the terrain (m) for the ducting/layer-reflection <br> model (see Attachment 2 to Annex 1 for definitions). <br> Note that the same parameter names are used for effective heights in the diffraction <br> model, but $h_{t e}$ and $h_{r e}$ have different definitions in the diffraction model. See equations <br> (39a) and (39b) |

TABLE 3 (end)

| Parameter | Description |
| :---: | :--- |
| $d_{b}$ | Aggregate length of the path sections over water (km) |
| $\omega$ | Fraction of the total path over water: <br> $\omega=d_{b} / d$ <br> where $d$ is the great-circle distance (km) calculated using equation (148). <br> For totally overland paths: $\omega=0$ |
| $d_{c, t, c r}$ | Distance over land from the transmit and receive antennas to the coast along the great- <br> circle interference path (km). Set to zero for a terminal on a ship or sea platform |

## 4 Clear-air propagation models

Basic transmission loss, $L_{b}(\mathrm{~dB})$, not exceeded for the required annual percentage time, $p$, is evaluated as described in the following sub-sections.

### 4.1 Line-of-sight propagation (including short-term effects)

The following should be evaluated for both LoS and transhorizon paths.
Basic transmission loss due to free-space propagation and attenuation by atmospheric gases:

$$
\begin{equation*}
L_{b f s g}=92.4+20 \log f+20 \log d_{f s}+A_{g}\left(d_{f s}\right) \quad \mathrm{dB} \tag{8}
\end{equation*}
$$

where:

## $f$ : frequency ( GHz )

$d_{f s}$ : distance between the transmit and receive antennas ( km ):

$$
\begin{equation*}
d_{f s}=\sqrt{d^{2}+\left(\frac{h_{t s}-h_{r s}}{1000}\right)^{2}} \tag{8a}
\end{equation*}
$$

$d: \quad$ great-circle path distance (km)
$h_{t s}$ : transmit antenna height above sea level (masl)
$h_{r s}$ : receive antenna height above sea level (masl)
$A_{g}: \quad$ total gaseous absorption (dB):

$$
\begin{equation*}
A_{g}\left(d_{f s}\right)=\left[\gamma_{0}+\gamma_{w}(\rho)\right] \cdot d_{f s} \quad \mathrm{~dB} \tag{9}
\end{equation*}
$$

where:
$\gamma_{o}, \gamma_{w}(\rho)$ : specific attenuation due to dry air and water vapour, respectively, and are found from the equations in Recommendation ITU-R P. 676
$\rho$ : water vapour density:

$$
\begin{equation*}
\rho=7.5+2.5 \omega \quad \mathrm{~g} / \mathrm{m}^{3} \tag{9a}
\end{equation*}
$$

$\omega$ : fraction of the total path over water.
Corrections for multipath and focusing effects at $p$ and $\beta_{0}$ percentage times:

$$
\begin{array}{rlc}
E_{s p} & =2.6\left[1-\exp \left(-0.1\left\{d_{l t}+d_{l r}\right\}\right)\right] \log (p / 50) & \mathrm{dB} \\
E_{s \beta} & =2.6\left[1-\exp \left(-0.1\left\{d_{l t}+d_{l r}\right\}\right)\right] \log \left(\beta_{0} / 50\right) & \mathrm{dB} \tag{10b}
\end{array}
$$

Basic transmission loss not exceeded for time percentage, $p \%$, due to LoS propagation:

$$
\begin{equation*}
L_{b 0 p}=L_{b f s g}+E_{s p} \quad \mathrm{~dB} \tag{11}
\end{equation*}
$$

Basic transmission loss not exceeded for time percentage, $\beta_{0} \%$, due to LoS propagation (regardless of whether or not the path is actually LoS):

$$
\begin{equation*}
L_{b 0 \beta}=L_{b f s g}+E_{s \beta} \quad \mathrm{~dB} \tag{12}
\end{equation*}
$$

### 4.2 Diffraction

The time variability of the excess loss due to the diffraction mechanism is assumed to be the result of changes in bulk atmospheric radio refractivity lapse rate, i.e. as the time percentage $p$ reduces, the effective Earth radius factor $k(p)$ is assumed to increase. This process is considered valid for $\beta_{0} \leq p \leq 50 \%$. For time percentages less than $\beta_{0}$ signal levels are dominated by anomalous propagation mechanisms rather than by the bulk refractivity characteristics of the atmosphere. Thus diffraction loss not exceeded for $p<\beta_{0} \%$ is assumed to be the same as for $p=\beta_{0} \%$ time.
Taking this into account, in the general case where $p<50 \%$, the diffraction calculation must be performed twice, first for the median effective Earth-radius factor $k_{50}$ (equation (5)) and second for the limiting effective Earth-radius factor $k_{\beta}$ equal to 3 . This second calculation gives an estimate of diffraction loss not exceeded for $\beta_{0} \%$ time, where $\beta_{0}$ is given by equation (2).
The diffraction loss $L_{d p}$ not exceeded for $p \%$ time, for $0.001 \% \leq p \leq 50 \%$, is then calculated using a limiting or interpolation procedure described in § 4.2.4.
The diffraction model calculates the following quantities required in § 4.6:

$$
L_{d p}: \quad \text { diffraction loss not exceeded for } p \% \text { time }
$$

Lbd50: median basic transmission loss associated with diffraction
$L_{b d}$ : basic transmission loss associated with diffraction not exceeded for $p \%$ time.
The diffraction loss is calculated by the combination of a method based on the Bullington construction and spherical-Earth diffraction. The Bullington part of the method is an expansion of the basic Bullington construction to control the transition between free-space and obstructed conditions. This part of the method is used twice: for the actual path profile, and for a zero-height smooth profile with modified antenna heights referred to as effective antenna heights. The same effective antenna heights are also used to calculate the spherical-Earth diffraction loss. The final result is obtained as a combination of three losses calculated as above. For a perfectly smooth path, the final diffraction loss will be the output of the spherical-Earth model.
This method provides an estimate of diffraction loss for all types of paths, including over-sea or overinland or coastal land, and irrespective of whether the land is smooth or rough, and whether LoS or transhorizon.
This method also makes extensive use of an approximation to the single knife-edge diffraction loss as a function of the dimensionless parameter, $v$, given by:

$$
\begin{equation*}
J(v)=6.9+20 \log \left(\sqrt{(v-0.1)^{2}+1}+v-0.1\right) \tag{13}
\end{equation*}
$$

Note that $J(-0.78) \approx 0$, and this defines the lower limit at which this approximation should be used. $J(v)$ is set to zero for $v<-0.78$.
The overall diffraction calculation is described in the subsections as follows:

Section 4.2.1 describes the Bullington part of the diffraction method. For each diffraction calculation for a given effective Earth radius this is used twice. On the second occasion, the antenna heights are modified and all profile heights are zero.
Section 4.2.2 describes the spherical-Earth part of the diffraction model. This is used with the same antenna heights as for the second use of the Bullington part in § 4.2.1.
Section 4.2.3 describes how the methods in $\S \S 4.2 .1$ and 4.2.2 are used in combination to perform the complete diffraction calculation for a given effective Earth radius. Due to the manner in which the Bullington and spherical-Earth parts are used, the complete calculation has come to be known as the "delta-Bullington" model.
Section 4.2.4 describes the complete calculation for diffraction loss not exceeded for a given percentage time $p \%$.

### 4.2.1 The Bullington part of the diffraction calculation

In the following equations, slopes are calculated in $\mathrm{m} / \mathrm{km}$ relative to the baseline joining sea level at the transmitter to sea level at the receiver. The distance and height of the $i$-th profile point are $d_{i}$ kilometres and $h_{i}$ metres above mean sea level respectively, $i$ takes values from 0 to $n$ where $n+1$ is the number of profile points, and the complete path length is $d$ kilometres. For convenience the terminals at the start and end of the profile are referred to as transmitter and receiver, with heights in m above sea level, $h_{t s}$ and $h_{r s}$, respectively. Effective Earth curvature $C_{e} \mathrm{~km}^{-1}$ is given by $1 / a_{p}$ where $a_{p}$ is effective earth radius in kilometres. Wavelength in metres is represented by $\lambda$. Values to be used for $a_{p}$ are given in § 4.2.4.
Find the intermediate profile point with the highest slope of the line from the transmitter to the point.

$$
\begin{equation*}
S_{\text {tim }}=\max \left\lfloor\frac{h_{i}+500 C_{e} d_{i}\left(d-d_{i}\right)-h_{t s}}{d_{i}}\right\rfloor \quad \mathrm{m} / \mathrm{km} \tag{14}
\end{equation*}
$$

where the profile index $i$ takes values from 1 to $n-1$.
Calculate the slope of the line from transmitter to receiver assuming a LoS path:

$$
\begin{equation*}
S_{t r}=\frac{h_{t s}-h_{t s}}{d} \quad \mathrm{~m} / \mathrm{km} \tag{15}
\end{equation*}
$$

Two cases must now be considered.

## Case 1. Path is LoS

If $S_{t i m}<S_{t r}$ the path is LoS.
Find the intermediate profile point with the highest diffraction parameter $v$ :

$$
\begin{equation*}
\left.v_{\max }=\max \left\{\left\lvert\, h_{i}+500 C_{e} d_{i}\left(d-d_{i}\right)-\frac{h_{s s}\left(d-d_{i}\right)+h_{r s} d_{i}}{d}\right.\right] \sqrt{\frac{0.002 d}{\lambda d_{i}\left(d-d_{i}\right)}}\right\} \tag{16}
\end{equation*}
$$

where the profile index $i$ takes values from 1 to $n-1$.
In this case, the knife-edge loss for the Bullington point is given by:

$$
\begin{equation*}
L_{u c}=J\left(v_{\max }\right) \quad \mathrm{dB} \tag{17}
\end{equation*}
$$

where the function $J$ is given by equation (13) for $v_{b}$ greater than -0.78 , and is zero otherwise.

## Case 2. Path is transhorizon

If $S_{t i m} \geq S_{t r}$ the path is transhorizon.
Find the intermediate profile point with the highest slope of the line from the receiver to the point.

$$
\begin{equation*}
S_{\text {rim }}=\max \left\lfloor\frac{h_{i}+500 C_{e} d_{i}\left(d-d_{i}\right)-h_{r s}}{d-d_{i}}\right\rfloor \quad \mathrm{m} / \mathrm{km} \tag{18}
\end{equation*}
$$

where the profile index $i$ takes values from 1 to $n-1$.
Calculate the distance of the Bullington point from the transmitter:

$$
\begin{equation*}
d_{b p}=\frac{h_{r s}-h_{t s}+S_{\text {rim }} d}{S_{\text {tim }}+S_{\text {rim }}} \mathrm{km} \tag{19}
\end{equation*}
$$

Calculate the diffraction parameter, $v_{b}$, for the Bullington point

$$
\begin{equation*}
v_{b}=\left[h_{t s}+S_{t i m} d_{b p}-\frac{h_{t s}\left(d-d_{b p}\right)+h_{t s} d_{b p}}{d}\right] \sqrt{\frac{0.002 d}{\lambda d_{b p}\left(d-d_{b p}\right)}} \tag{20}
\end{equation*}
$$

In this case, the knife-edge loss for the Bullington point is given by:

$$
\begin{equation*}
L_{u c}=J\left(v_{b}\right) \quad \mathrm{dB} \tag{21}
\end{equation*}
$$

For $L_{u c}$ calculated using either equation (17) or (21), Bullington diffraction loss for the path is now given by:

$$
\begin{equation*}
L_{b u l l}=L_{u c}+\left[1-\exp \left(-L_{u c} / 6\right)\right](10+0.02 d) \quad \mathrm{dB} \tag{22}
\end{equation*}
$$

### 4.2.2 Spherical-Earth diffraction loss

The spherical-Earth diffraction loss for antenna heights $h_{t e}$ and $h_{r e}(\mathrm{~m}), L d s p h$, is calculated as follows. Calculate the marginal LoS distance for a smooth path:

$$
\begin{equation*}
d_{l o s}=\sqrt{2 a_{p}} \cdot\left(\sqrt{0.001 h_{t e}}+\sqrt{0.001 h_{r e}}\right) \quad \mathrm{km} \tag{23}
\end{equation*}
$$

Values to be used for $a_{p}$ are given in $\S$ 4.2.4. Effective antenna heights $h_{t e}$ and $h_{r e}$ are defined in equations (39a) and (39b).
If $d \geq d_{\text {los }}$ calculate diffraction loss using the method in $\S 4.2 .2$. below for $a_{d f t}=a_{p}$ to give $L_{d f t}$, and set $L_{d s p h}$ equal to $L_{d f f}$. No further spherical-Earth diffraction calculation is necessary.
Otherwise continue as follows:
Calculate the smallest clearance height between the curved-Earth path and the ray between the antennas, $h_{s e}$, given by:

$$
\begin{equation*}
h_{s e}=\frac{\left(h_{t e}-500 \frac{d_{s e 1}^{2}}{a_{p}}\right) d_{s e 2}+\left(h_{r e}-500 \frac{d_{s e 2}^{2}}{a_{p}}\right) d_{s e 1}}{d} \mathrm{~m} \tag{24}
\end{equation*}
$$

where:

$$
\begin{gather*}
d_{\text {se1 }}=\frac{d}{2}(1+b) \quad \mathrm{km}  \tag{25a}\\
d_{\text {se2 }}=d-d_{\text {se1 }} \mathrm{km}  \tag{25b}\\
b=2 \sqrt{\frac{m+1}{3 m}} \cos \left\{\frac{\pi}{3}+\frac{1}{3} \arccos \left(\frac{3 c}{2} \sqrt{\frac{3 m}{(m+1)^{3}}}\right)\right\} \tag{25c}
\end{gather*}
$$

where the arccos function returns an angle in radians.

$$
\begin{align*}
c & =\frac{h_{t e}-h_{r e}}{h_{t e}+h_{r e}}  \tag{25~d}\\
m & =\frac{250 d^{2}}{a_{p}\left(h_{t e}+h_{r e}\right)} \tag{25e}
\end{align*}
$$

Calculate the required clearance for zero diffraction loss, $h_{\text {req }}$, given by:

$$
\begin{equation*}
h_{\text {req }}=17.456 \sqrt{\frac{d_{s e 1} \cdot d_{s e 2} \cdot \lambda}{d}} \quad \mathrm{~m} \tag{26}
\end{equation*}
$$

If $h_{s e}>h_{\text {req }}$ the spherical-Earth diffraction loss $L_{d s p h}$ is zero. No further spherical-Earth diffraction calculation is necessary.
Otherwise continue as follows:
Calculate the modified effective earth radius, $a_{e m}$, which gives marginal LoS at distance $d$ given by:

$$
\begin{equation*}
a_{e m}=500\left(\frac{d}{\sqrt{h_{t e}}+\sqrt{h_{r e}}}\right)^{2} \quad \mathrm{~km} \tag{27}
\end{equation*}
$$

Use the method in § 4.2.2.1 for $a_{d f t}=a_{e m}$ to give $L_{d f f}$.
If $L_{d f t}$ is negative, the spherical-Earth diffraction loss, $L_{d s p h}$, is zero, and no further spherical-Earth diffraction calculation is necessary.
Otherwise continue as follows:
Calculate the spherical-Earth diffraction loss by interpolation:

$$
\begin{equation*}
L_{d s p h}=\left[1-h_{s e} / h_{r e q}\right] L_{d f t} \quad \mathrm{~dB} \tag{28}
\end{equation*}
$$

### 4.2.2.1 First-term part of spherical-Earth diffraction loss

This sub-section gives the method for calculating spherical-Earth diffraction using only the first term of the residue series. It forms part of the overall diffraction method described in § 4.2.2 above to give the first-term diffraction loss, $L_{d f f}$, for a given value of effective Earth radius $a_{d f t}$. The value of $a_{d f t}$ to use is given in § 4.2.2.
Set terrain electrical properties typical for land, with relative permittivity $\varepsilon_{r}=22.0$ and conductivity $\sigma=0.003 \mathrm{~S} / \mathrm{m}$ and calculate $L_{d f t}$ using equations (30) to (37) and call the result $L_{d f f l a n d .}$
Set terrain electrical properties typical for sea, with relative permittivity $\varepsilon_{r}=80.0$ and conductivity $\sigma=5.0 \mathrm{~S} / \mathrm{m}$ and calculate $L_{d f t}$ using equations (30) to (37) and call the result $L_{d f f s e a .}$
First-term spherical diffraction loss is now given by:

$$
\begin{equation*}
L_{d f t}=\omega L_{d f \text { sea }}+(1-\omega) L_{d f t l a n d} \quad \mathrm{~dB} \tag{29}
\end{equation*}
$$

where $\omega$ is the fraction of the path over sea.
Start of calculation to be performed twice, as described above:
Normalized factor for surface admittance for horizontal and vertical polarization.

$$
\begin{equation*}
K_{H}=0.036\left(a_{d f f} f\right)^{-1 / 3}\left[\left(\varepsilon_{r}-1\right)^{2}+(18 \sigma / f)^{2}\right]^{-1 / 4} \quad \text { (horizontal) } \tag{30a}
\end{equation*}
$$

and:

$$
\begin{equation*}
K_{V}=K_{H}\left[\varepsilon_{r}^{2}+(18 \sigma / f)^{2}\right]^{1 / 2} \quad(\text { vertical }) \tag{30b}
\end{equation*}
$$

If the polarization vector contains both horizontal and vertical components, e.g. circular or slant, decompose it into horizontal and vertical components, calculate each separately starting from equations (30a) and (30b) and combine the results by a vector sum of the field amplitude. In practice this decomposition will generally be unnecessary because above 300 MHz a value of 1 can be used for $\beta_{d f t}$ in equation (31).
Calculate the Earth ground/polarization parameter:

$$
\begin{equation*}
\beta_{d f t}=\frac{1+1.6 K^{2}+0.67 K^{4}}{1+4.5 K^{2}+1.53 K^{4}} \tag{31}
\end{equation*}
$$

where $K$ is $K_{H}$ or $K_{V}$ according to polarization.
Normalized distance:

$$
\begin{equation*}
X=21.88 \beta_{d f t}\left(\frac{f}{a_{d f t}^{2}}\right)^{1 / 3} d \tag{32}
\end{equation*}
$$

Normalized transmitter and receiver heights:

$$
\begin{align*}
& Y_{t}=0.9575 \beta_{d f t}\left(\frac{f^{2}}{a_{d f t}}\right)^{1 / 3} h_{t e}  \tag{33a}\\
& Y_{r}=0.9575 \beta_{d f t}\left(\frac{f^{2}}{a_{d f t}}\right)^{1 / 3} h_{r e} \tag{33b}
\end{align*}
$$

Calculate the distance term given by:

$$
F_{X}= \begin{cases}11+10 \log (X)-17.6 X & \text { for } X \geq 1.6  \tag{34}\\ -20 \log (X)-5.6488 X^{1.425} & \text { for } X<1.6\end{cases}
$$

Define a function of normalized height given by:

$$
G\left(Y_{t / r}\right)= \begin{cases}17.6\left(B_{t / r}-1.1\right)^{0.5}-5 \log \left(B_{t / r}-1.1\right)-8 & \text { for } B_{t / r}>2  \tag{35}\\ 20 \log \left(B_{t / r}+0.1 B_{t / r}{ }^{3}\right) & \text { otherwise }\end{cases}
$$

where:

$$
\begin{align*}
B_{t} & =\beta_{d f t} Y_{t}  \tag{36a}\\
B_{r} & =\beta_{d f t} Y_{r} \tag{36b}
\end{align*}
$$

If $G(Y)$ is less than $2+20 \log K$, then limit $G(Y)$ such that $G(Y)=2+20 \log K$.
The first-term spherical-Earth diffraction loss is now given by:

$$
\begin{equation*}
L_{d f t}=-F_{X}-G\left(Y_{t}\right)-G\left(Y_{r}\right) \quad \mathrm{dB} \tag{37}
\end{equation*}
$$

### 4.2.3 Complete 'delta-Bullington' diffraction loss model

Use the method in § 4.2.1 for the actual terrain profile and antenna heights. Set the resulting Bullington diffraction loss for the actual path, $L_{b u l l a}=L_{b u l l}$ as given by equation (22).
Use the method in $\S 4.2 .1$ for a second time, with all profile heights, $h_{i}$, set to zero, and modified antenna heights given by:

$$
\begin{array}{ll}
h_{t s}^{\prime}=h_{t s}-h_{s t d} & \text { masl } \\
h_{r s}^{\prime}=h_{r s}-h_{s r d} & \text { masl } \tag{38b}
\end{array}
$$

where the smooth-Earth heights at transmitter and receiver, $h_{s t d}$ and $h_{s r d}$, are given in § 5.1.6.3 of Attachment 2. Set the resulting Bullington diffraction loss for this smooth path, Lbulls $=$ Lbull as given by equation (22).
Use the method in § 4.2.2 to calculate the spherical-Earth diffraction loss $L_{d s p h}$ for the actual path length $d(\mathrm{~km})$ and with:

$$
\begin{array}{ll}
h_{t e}=h_{t s}^{\prime} & \mathrm{m} \\
h_{r e}=h_{r s}^{\prime} & \mathrm{m} \tag{39b}
\end{array}
$$

Diffraction loss for the general path is now given by:

$$
\begin{equation*}
L_{d}=L_{\text {bulla }}+\max \left\{L_{d s p h}-L_{\text {bulls }}, 0\right\} \quad \mathrm{dB} \tag{40}
\end{equation*}
$$

### 4.2.4 The diffraction loss not exceeded for $\boldsymbol{p} \%$ of the time

Use the method in $\S 4.2 .3$ to calculate diffraction loss $L_{d}$ for effective Earth radius $a_{p}=a_{e}$ as given by equation (6a). Set median diffraction loss $L_{d 50}=L_{d}$.
If $p=50 \%$ the diffraction loss not exceeded for $p \%$ time, $L_{d p}$, is given by $L_{d 50}$, and this completes the diffraction calculation.

If $p<50 \%$ continue as follows.
Use the method in § 4.2.3 to calculate diffraction loss $L_{d}$ for effective Earth radius $a_{p}=a_{\beta}$ as given in equation (6b). Set diffraction loss not exceeded for $\beta_{0} \%$ time $L_{d \beta}=L_{d}$.

The application of the two possible values of effective Earth radius factor is controlled by an interpolation factor, $F_{i}$, based on the normal distribution of diffraction loss over the range $\beta_{0} \% \leq p<50 \%$ given by:

$$
\begin{array}{rlr}
F_{i} & =\frac{I\left(\frac{p}{100}\right)}{I\left(\frac{\beta_{0}}{100}\right)} & \text { for } 50 \%>p>\beta_{0} \% \\
& =1 & \text { for } \beta_{0} \% \geq p \tag{41b}
\end{array}
$$

where $I(x)$ is the inverse complementary cumulative normal function. An approximation for $I(x)$ which may be used with confidence for $x<0.5$ is given in Attachment 3 to Annex 1.
The diffraction loss, $L_{d p}$, not exceeded for $p \%$ time, is now given by:

$$
\begin{equation*}
L_{d p}=L_{d 50}+F_{i}\left(L_{d \beta}-L_{d 50}\right) \quad \mathrm{dB} \tag{42}
\end{equation*}
$$

where $L_{d 50}$ and $L_{d \beta}$ are defined above, and $F_{i}$ is defined by equations (41a) and (41b), depending on the values of $p$ and $\beta_{0}$.

The median basic transmission loss associated with diffraction, $L_{b d 50}$, is given by:

$$
\begin{equation*}
L_{b d 50}=L_{b f s g}+L_{d 50} \quad \mathrm{~dB} \tag{43}
\end{equation*}
$$

where $L_{b f s g}$ is given by equation (8).
The basic transmission loss associated with diffraction not exceeded for $p \%$ time is given by:

$$
\begin{equation*}
L_{b d}=L_{b 0 p}+L_{d p} \quad \mathrm{~dB} \tag{44}
\end{equation*}
$$

where $L_{b 0 p}$ is given by equation (11).

### 4.3 Tropospheric scatter (Notes 1 and 2)

NOTE 1 - At time percentages much below $50 \%$, it is difficult to separate the true tropospheric scatter mode from other secondary propagation phenomena which give rise to similar propagation effects. The "tropospheric scatter" model adopted in this Recommendation is therefore an empirical generalization of the concept of tropospheric scatter which also embraces these secondary propagation effects. This allows a continuous consistent prediction of basic transmission loss over the range of time percentages $p$ from $0.001 \%$ to $50 \%$, thus linking the ducting and layer reflection model at the small time percentages with the true "scatter mode" appropriate to the weak residual field exceeded for the largest time percentage.
NOTE 2 - This troposcatter prediction model has been derived for interference prediction purposes and is not appropriate for the calculation of propagation conditions above $50 \%$ of time affecting the performance aspects of trans-horizon radio-relay systems.

The basic transmission loss due to troposcatter, $L_{b s}(\mathrm{~dB})$ not exceeded for any time percentage, $p$, below $50 \%$, is given by:
$L_{b s}=190+L_{f}+20 \log d+0.573 \theta-0.15 N_{0}+L_{c}+A_{g}-10.1[-\log (p / 50)]^{0.7} \mathrm{~dB}$
where:
$L_{f}$ : frequency dependent loss:

$$
\begin{equation*}
L_{f}=25 \log f-2.5[\log (f / 2)]^{2} \quad \mathrm{~dB} \tag{45a}
\end{equation*}
$$

$L_{c}$ : aperture to medium coupling loss (dB):

$$
\begin{equation*}
L_{c}=0.051 \cdot \mathrm{e}^{0.055\left(G_{t}+G_{r}\right)} \quad \mathrm{dB} \tag{45b}
\end{equation*}
$$

$N_{0}$ : path centre sea-level surface refractivity from the maps in Attachment 1 to Annex 1
$A_{g}$ : gaseous absorption derived from equation (9) using $\rho=3 \mathrm{~g} / \mathrm{m}^{3}$ for the whole path length.

### 4.4 Ducting/layer reflection

The prediction of the basic transmission loss, $L_{b a}(\mathrm{~dB})$ occurring during periods of anomalous propagation (ducting and layer reflection) is based on the following function:

$$
\begin{equation*}
L_{b a}=A_{f}+A_{d}(p)+A_{g} \quad \mathrm{~dB} \tag{46}
\end{equation*}
$$

where:
$A_{f}$ : total of fixed coupling losses (except for local clutter losses) between the antennas and the anomalous propagation structure within the atmosphere:
$A_{f}=102.45+20 \log f+20 \log \left(d_{l t}+d_{l r}\right)+A_{l f}+A_{s t}+A_{s r}+A_{c t}+A_{c r} \quad \mathrm{~dB}$
$A_{l f:} \quad$ empirical correction to account for the increasing attenuation with wavelength inducted propagation:

$$
\begin{equation*}
A_{t}(f)=45.375-137.0 \cdot f+92.5 \cdot f^{2} \mathrm{~dB} \quad \text { if } f<0.5 \mathrm{GHz} \tag{47a}
\end{equation*}
$$

$A_{l f}(f)=0.0 \mathrm{~dB} \quad$ otherwise
$A_{s t}, A_{s r}$ : site-shielding diffraction losses for the interfering and interfered-with stations respectively:

$$
A_{s t, s r}=\left\{\begin{array}{llll}
20 \log \left[1+0.361 \theta_{t, r}^{\prime \prime}\left(f \cdot d_{t, t r}\right)^{1 / 2}\right]+0.264 \theta_{t, r}^{\prime \prime} f^{1 / 3} & \mathrm{~dB} & \text { for } \theta_{t, r}^{\prime \prime}>0 & \mathrm{mrad}  \tag{48}\\
0 & \mathrm{~dB} & \text { for } \theta_{t, r}^{\prime \prime} \leq 0 & \mathrm{mrad}
\end{array}\right.
$$

where:

$$
\begin{equation*}
\theta_{t, r}^{\prime \prime}=\theta_{t, r}-0.1 d_{l t, t r} \quad \mathrm{mrad} \tag{48a}
\end{equation*}
$$

$A_{c t}, A_{c r}$ : over-sea surface duct coupling corrections for the interfering and interfered-with stations respectively:

$$
\begin{gather*}
A_{c t, c r}=-3 \mathrm{e}^{-0.25 d_{c t, c r}^{2}\left[1+\tanh \left(0.07\left(50-h_{t s, r s}\right)\right)\right.} \begin{array}{c}
\quad \mathrm{dB} \quad \text { for } \omega \geq 0.75 \\
d_{c t, c r} \\
d_{c t, c r} \\
\leq d_{l t, l r} \\
A_{c t, c r}=0 \quad \\
\mathrm{~dB} \\
\mathrm{~km} \\
\text { for all other conditions }
\end{array}
\end{gather*}
$$

It is useful to note the limited set of conditions under which equation (49) is needed.
$A_{d}(p)$ : time percentage and angular-distance dependent losses within the anomalous propagation mechanism:

$$
\begin{equation*}
A_{d}(p)=\gamma_{d} \cdot \theta^{\prime}+A(p) \quad \mathrm{dB} \tag{50}
\end{equation*}
$$

where:
$\gamma_{d}$ : specific attenuation:

$$
\begin{equation*}
\gamma_{d}=5 \times 10^{-5} a_{e} f^{1 / 3} \quad \mathrm{~dB} / \mathrm{mrad} \tag{51}
\end{equation*}
$$

$\theta^{\prime}$ : angular distance (corrected where appropriate (via equation (52a)) to allow for the application of the site shielding model in equation (48)):

$$
\begin{gather*}
\theta^{\prime}=\frac{10^{3} d}{a_{e}}+\theta_{t}^{\prime}+\theta_{r}^{\prime} \quad \operatorname{mrad}  \tag{52}\\
\theta_{t, r}^{\prime}=\left\{\begin{array}{ll}
\theta_{t, r} & \text { for } \theta_{t, r} \leq 0.1 d_{l t, l r} \\
0.1 d_{l t, l r} & \text { for } \theta_{t, r}>0.1 d_{l t, l r}
\end{array} \quad \mathrm{mrad}\right.  \tag{52a}\\
\mathrm{mrad}
\end{gather*} ~ . ~ \$
$$

$A(p)$ : time percentage variability (cumulative distribution):

$$
\begin{gather*}
A(p)=-12+\left(1.2+3.7 \times 10^{-3} d\right) \log \left(\frac{p}{\beta}\right)+12\left(\frac{p}{\beta}\right)^{\Gamma} \quad \mathrm{dB}  \tag{53}\\
\Gamma=\frac{1.076}{(2.0058-\log \beta)^{1.012}} \times \mathrm{e}^{-\left(9.51-4.8 \log \beta+0.198(\log \beta)^{2}\right) \times 10^{-6} \cdot d^{1.13}}  \tag{53a}\\
\beta=\beta_{0} \cdot \mu_{2} \cdot \mu_{3} \quad \% \tag{54}
\end{gather*}
$$

$\mu_{2}$ : correction for path geometry:

$$
\begin{equation*}
\mu_{2}=\left[\frac{500}{a_{e}} \frac{d^{2}}{\left(\sqrt{h_{t e}}+\sqrt{h_{r e}}\right)^{2}}\right]^{\alpha} \tag{55}
\end{equation*}
$$

The value of $\mu_{2}$ shall not exceed 1 .
Effective antenna heights $h_{t e}$ and $h_{r e}$ are defined in equation (170).

$$
\begin{equation*}
\alpha=-0.6-\varepsilon \cdot 10^{-9} \cdot d^{3.1} \cdot \tau \tag{55a}
\end{equation*}
$$

where:

$$
\begin{aligned}
& \varepsilon=3.5 \\
& \tau \text { : is defined in equation (3a) } \\
& \text { and the value of } \alpha \text { shall not be allowed to reduce below }-3.4 \text {. } \\
& \mu_{3} \text { : correction for terrain roughness: } \\
& \mu_{3}=\left\{\begin{array}{lr}
1 & \text { for } h_{m} \leq 10 \mathrm{~m} \\
\exp \left[-4.6 \times 10^{-5}\left(h_{m}-10\right)\left(43+6 d_{I}\right)\right] & \text { for } h_{m}>10 \mathrm{~m} \\
d_{I}=\min \left(d-d_{l t}-d_{l r}, 40\right) & \mathrm{km}
\end{array}\right.
\end{aligned}
$$

$A_{g}: \quad$ total gaseous absorption determined from equations (9) and (9a).
The remaining terms have been defined in Tables 1 and 2 and Attachment 2.

### 4.5 Additional clutter losses

### 4.5.1 General

Considerable benefit, in terms of protection from interference, can be derived from the additional diffraction losses available to antennas which are imbedded in local ground clutter (buildings, vegetation, etc.). This procedure allows for the addition of such clutter losses at either or both ends of the path in situations where the clutter scenario is known. It predicts a maximum additional loss at either end of the path, applied via an S-shaped interpolation function intended to avoid an overestimate of the shielding loss. The maximum additional loss is 20 dB above 0.9 GHz , and progressively less at lower frequencies, down to 5 dB at 0.1 GHz . Where there are doubts as to the certainty of the clutter environment this additional loss should not be included. Where the correction is used, care should be taken not to expect high clutter losses in a high-rise urban area consisting of isolated tall buildings separated by open spaces. Lower clutter losses are often observed in such areas compared to more traditional city centres comprising lower but more connected blocks of buildings.
The clutter losses are designated as $A_{h t}(\mathrm{~dB})$ and $A_{h r}(\mathrm{~dB})$ for the interferer and interfered-with stations respectively. The additional protection available is height dependent, and is therefore modelled by a height-gain function normalized to the nominal height of the clutter. Appropriate nominal heights are available for a range of clutter types.
The correction applies to all clear-air predictions in this Recommendation, i.e. for all propagation modes and time percentages.

### 4.5.2 Clutter categories

Table 4 indicates the clutter (or ground cover) categories as defined in Recommendation ITU-R P. 1058 for which the height-gain correction can be applied. The nominal clutter height, $h_{a}(\mathrm{~m})$ and distance from the antenna, $d_{k}(\mathrm{~km})$ are deemed to be "average" values most representative of the clutter type. However, the correction model has been made conservative in recognition of the uncertainties over the actual height that are appropriate in individual situations. Where the clutter parameters are more accurately known they can be directly substituted for the values taken from Table 4.
The nominal heights and distances given in Table 4 approximate to the characteristic height $H_{c}$ and gap-width $G_{c}$ defined in Recommendation ITU-R P.1058. However the model used here to estimate the additional losses due to shielding by clutter (ground cover) is intended to be conservative.

### 4.5.3 The height-gain model

The additional loss due to protection from local clutter is given by the expression:

$$
\begin{equation*}
A_{h}=10.25 F_{f c} \cdot \mathrm{e}^{-d_{k}}\left(1-\tanh \left[6\left(\frac{h}{h_{a}}-0.625\right)\right]\right)-0.33 \quad \mathrm{~dB} \tag{57}
\end{equation*}
$$

where:

$$
\begin{equation*}
F_{f c}=0.25+0.375\{1+\tanh [7.5(f-0.5)]\} \tag{57a}
\end{equation*}
$$

and:
$d_{k}$ : distance (km) from nominal clutter point to the antenna (see Fig. 3)
$h$ : antenna height ( m ) above local ground level
$h_{a}$ : nominal clutter height (m) above local ground level.

TABLE 4
Nominal clutter heights and distances

| Clutter (ground-cover) category | Nominal height, $\boldsymbol{h}_{\boldsymbol{a}}$ <br> $(\mathbf{m})$ | Nominal distance, $\boldsymbol{d}_{\boldsymbol{k}}$ <br> $(\mathbf{k m})$ |
| :--- | :---: | :---: |
| High crop fields <br> Park land <br> Irregularly spaced sparse trees <br> Orchard (regularly spaced) <br> Sparse houses <br> Village centre | 0.1 |  |
| Deciduous trees (irregularly spaced) <br> Deciduous trees (regularly spaced) <br> Mixed tree forest | 5 | 0.07 |
| Coniferous trees (irregularly spaced) <br> Coniferous trees (regularly spaced) | 15 | 0.05 |
| Tropical rain forest | 20 | 0.05 |
| Suburban | 20 | 0.03 |
| Dense suburban | 9 | 0.025 |
| Urban | 12 | 0.02 |

TABLE 4 (end)

| Clutter (ground-cover) category | Nominal height, $\boldsymbol{h}_{\boldsymbol{a}}$ <br> $(\mathbf{m})$ | Nominal distance, $\boldsymbol{d}_{\boldsymbol{k}}$ <br> $(\mathbf{k m})$ |
| :--- | :---: | :---: |
| Dense urban | 25 | 0.02 |
| High-rise urban | 35 | 0.02 |
| Industrial zone | 20 | 0.05 |

Additional losses due to shielding by clutter (ground cover) should not be claimed for categories not appearing in Table 4.

FIGURE 3
Method of applying height-gain correction, $A_{h t}$ or $A_{h r}$

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### 4.5.4 Method of application

The method of applying the height-gain correction, $A_{h t}$ or $A_{h r}(\mathrm{~dB})$ is straightforward, and is shown in Fig. 3.
The steps to be added to the basic prediction procedure are as follows:
Step 1: Where the clutter type is known or can be safely assumed, the main procedure is used to calculate the basic transmission loss to the nominal height, $h_{a}$, for the appropriate clutter type, as selected from Table 4. The path length to be used is $d-d_{k}(\mathrm{~km})$. However where $d \gg d_{k}$ this minor correction for $d_{k}$ can safely be ignored.
Step 2: Where there is a "site-shielding" obstacle that will provide protection to the terminal this should still be included in the basic calculation, but the shielding loss ( $A_{s t}$ or $A_{s r}(\mathrm{~dB})$ ) should be calculated to the height $h_{a}$ at distance $d_{s}$, rather than to $h$ at $d_{L}$ as would otherwise be the case.
Step 3: Once the main procedure is complete, the height gain correction from equation (57) can be added, as indicated in equation (64).

Step 4: Where information on the clutter is not available, the basic calculation should be undertaken using distances $d$ and $d_{L}$ (if appropriate) and height $h$.

NOTE 1 - Clutter height-gain corrections should be added to both ends of the path where this is appropriate. NOTE 2 - Where both the land height-gain correction and the sea duct coupling correction ( $A_{c t}$ or $A_{c r}(\mathrm{~dB})$ ) are required (i.e. the antenna is close to the sea but there is intervening clutter), the two corrections can be used together as they are complementary and compatible.
NOTE 3 - If $d$ is not significantly greater than $d_{k}$ this model is not suitable.

### 4.6 The overall prediction

The following procedure should be applied to the results of the foregoing calculations for all paths.
Calculate an interpolation factor, $F_{j}$, to take account of slope parameters:

$$
\begin{equation*}
F_{j}=1.0-0.5\left(1.0+\tanh \left(3.0 \xi \frac{\left(S_{t i m}-S_{t r}\right)}{\Theta}\right)\right) \tag{58}
\end{equation*}
$$

where:
$\xi$ : adjustable parameter currently set to 0.8
( $S_{t i m}-S_{t r}$ ): slope parameters defined in equations (14) and (15)
$\Theta$ : adjustable parameter currently set to 0.3 mrad .
Calculate an interpolation factor, $F_{k}$, to take account of the great circle path distance:

$$
\begin{equation*}
F_{k}=1.0-0.5\left(1.0+\tanh \left(3.0 \kappa \frac{\left(d-d_{s w}\right)}{d_{s w}}\right)\right) \tag{59}
\end{equation*}
$$

where:
$d: \quad$ great circle path length $(\mathrm{km})$ (defined in Table 3)
$d_{s w}$ : fixed parameter determining the distance range of the associated blending, set to 20
$\kappa$ : fixed parameter determining the blending slope at the ends of the range, set to 0.5
Calculate a notional minimum basic transmission loss, $L_{\text {minb0p }}(\mathrm{dB})$ associated with LoS propagation and over-sea sub-path diffraction.

$$
L_{\min b 0 p}=\left\{\begin{array}{lr}
L_{b 0 p}+(1-\omega) L_{d p} & \text { for } p<\beta_{0}  \tag{60}\\
L_{b d 50}+\left(L_{b 0 \beta}+(1-\omega) L_{d p}-L_{b d 50}\right) \cdot F_{i} & \text { for } p \geq \beta_{0}
\end{array} \quad \mathrm{~dB}\right.
$$

where:
$L_{b 0 p}$ : notional LoS basic transmission loss not exceeded for $p \%$ time, given by equation (11)
$L_{b 0 \beta}$ : notional LoS basic transmission loss not exceeded for $\beta \%$ time, given by equation (12)
$L_{d p}: \quad$ diffraction loss not exceeded for $p \%$ time, calculated using the method in $\S 4.2$
$F_{i}: \quad$ diffraction interpolation factor, given by equation (41).
Calculate a notional minimum basic transmission loss, $L_{\text {minbap }}(\mathrm{dB})$, associated with LoS and transhorizon signal enhancements:

$$
\begin{equation*}
L_{\text {minbap }}=\eta \ln \left(\exp \left(\frac{L_{b a}}{\eta}\right)+\exp \left(\frac{L_{b 0 p}}{\eta}\right)\right) \quad \mathrm{dB} \tag{61}
\end{equation*}
$$

where:
$L_{b a}$ : ducting/layer reflection basic transmission loss not exceeded for $p \%$ time, given by equation (46)
$L_{b 0 p}$ : notional line-of-sight basic transmission loss not exceeded for $p \%$ time, given by equation (11)
$\eta=2.5$.
Calculate a notional basic transmission loss, $L_{b d a}(\mathrm{~dB})$, associated with diffraction and $\operatorname{LoS}$ or ducting/layer-reflection enhancements:

$$
L_{b d a}=\left\{\begin{array}{lll}
L_{b d} & \text { for } \quad L_{\text {minbap }}>L_{b d}  \tag{62}\\
L_{\text {minbap }}+\left(L_{b d}-L_{\text {minbap }}\right) F_{k} & \text { for } \quad L_{\text {minbap }} \leq L_{b d}
\end{array} \quad \mathrm{~dB}\right.
$$

where:
$L_{b d}$ : basic transmission loss for diffraction not exceeded for $p \%$ time from equation (44)
$F_{k}$ : interpolation factor given by equation (59) according the value of the great-circle path distance, $d$.
Calculate a modified basic transmission loss, $L_{\text {bam }}(\mathrm{dB})$, which takes diffraction and LoS or ducting/layer-reflection enhancements into account:

$$
\begin{equation*}
L_{b a m}=L_{b d a}+\left(L_{\text {minb0p }}-L_{b d a}\right) F_{j} \quad \mathrm{~dB} \tag{63}
\end{equation*}
$$

Calculate the final basic transmission loss not exceed for $p \%$ time, $L_{b}(\mathrm{~dB})$, as given by:

$$
\begin{equation*}
L_{b}=-5 \log \left(10^{-0.2 L_{b s}}+10^{-0.2 L_{b a m}}\right)+A_{h t}+A_{h r} \quad \mathrm{~dB} \tag{64}
\end{equation*}
$$

where:
$A_{h t h r}$ : additional losses to account for clutter shielding the transmitter and receiver. These should be set to zero if there is no such shielding.

### 4.7 Calculation of transmission loss

The method described in $\S \S 4.1$ to 4.6 above provides the basic transmission loss between the two stations. In order to calculate the signal level at one station due to interference from the other it is necessary to know the transmission loss, which takes account of the antenna gains of the two stations in the direction of the radio (i.e. interference) path between them.
The following procedure provides a method for the calculation of transmission loss between two terrestrial stations. As intermediate steps in the method, it also provides formulae for the calculation of the great-circle path length and angular distance based on the stations' geographic coordinates, as opposed to the derivations of these quantities from the path profile, as assumed in Table 3.
Calculate the angle subtended by the path at the centre of the Earth, $\delta$, from the stations' geographic coordinates using:

$$
\begin{equation*}
\delta=\arccos \left(\sin \left(\varphi_{t}\right) \sin \left(\varphi_{r}\right)+\cos \left(\varphi_{t}\right) \cos \left(\varphi_{r}\right) \cos \left(\psi_{t}-\psi_{r}\right)\right) \quad \operatorname{rad} \tag{65}
\end{equation*}
$$

The great circle distance, $d$, between the stations is:

$$
\begin{equation*}
d=6371 \cdot \delta \quad \mathrm{~km} \tag{66}
\end{equation*}
$$

Calculate the bearing (azimuthal direction clockwise from true North) from station $t$ to station $r$ using:

$$
\begin{equation*}
\alpha_{t r}=\arccos \left(\left\{\sin \left(\varphi_{r}\right)-\sin \left(\varphi_{t}\right) \cos (\delta)\right\} / \sin (\delta) \cos \left(\varphi_{t}\right)\right) \quad \operatorname{rad} \tag{67}
\end{equation*}
$$

Having implemented equation (67), if $\psi_{t}-\psi_{r}>0$ then:

$$
\begin{equation*}
\alpha_{t r}=2 \pi-\alpha_{t r} \quad \operatorname{rad} \tag{68}
\end{equation*}
$$

Calculate the bearing from station $r$ to station $t$, $\alpha_{r t}$, by symmetry from equations (67) and (68).
Next, assume that the main beam (boresight) direction of station $t$ is ( $\varepsilon_{t}, \alpha_{t}$ ) in (elevation, bearing), while the main beam direction of station $r$ is ( $\varepsilon r, \alpha_{r}$ ). To obtain the elevation angles of the radio (i.e. interference) path at stations $t$ and $r, \varepsilon_{p t}$ and $\varepsilon_{p r}$, respectively, it is necessary to distinguish between line-of-sight and trans-horizon paths. For example, for line-of-sight paths:

$$
\begin{equation*}
\varepsilon_{p t}=\frac{h_{r}-h_{t}}{d}-\frac{d}{2 a_{e}} \quad \quad \mathrm{rad} \tag{69a}
\end{equation*}
$$

and:

$$
\begin{equation*}
\varepsilon_{p r}=\frac{h_{t}-h_{r}}{d}-\frac{d}{2 a_{e}} \quad \mathrm{rad} \tag{69b}
\end{equation*}
$$

where $h_{t}$ and $h_{r}$ are the heights of the stations above mean sea level $(\mathrm{km})$, while for trans-horizon paths, the elevation angles are given by their respective horizon angles:

$$
\begin{equation*}
\varepsilon_{p t}=\frac{\theta_{t}}{1000} \quad \operatorname{rad} \tag{70a}
\end{equation*}
$$

and:

$$
\begin{equation*}
\varepsilon_{p r}=\frac{\theta_{r}}{1000} \quad \mathrm{rad} \tag{70b}
\end{equation*}
$$

Note that the radio horizon angles, $\theta_{t}$ and $\theta_{r}(\mathrm{mrad})$, are first introduced in Table 3 and are defined in $\S \S 5.1 .1$ and 5.1.3, respectively, of Attachment 2 to Annex 1.
To calculate the off-boresight angles for stations $t$ and $r, \chi_{t}$ and $\chi_{r}$, respectively, in the direction of the interference path at stations $t$ and $r$, it is recommended to use:

$$
\begin{equation*}
\chi_{t}=\arccos \left(\cos \left(\varepsilon_{t}\right) \cos \left(\varepsilon_{p t}\right) \cos \left(\alpha_{t r}-\alpha_{t}\right)+\sin \left(\varepsilon_{t}\right) \sin \left(\varepsilon_{p t}\right)\right) \tag{71a}
\end{equation*}
$$

and:

$$
\begin{equation*}
\chi_{r}=\arccos \left(\cos \left(\varepsilon_{r}\right) \cos \left(\varepsilon_{p r}\right) \cos \left(\alpha_{r t}-\alpha_{r}\right)+\sin \left(\varepsilon_{r}\right) \sin \left(\varepsilon_{p r}\right)\right) \tag{71b}
\end{equation*}
$$

Using their respective off-boresight angles, obtain the antenna gains for stations $t$ and $r, G_{t}$ and $G_{r}$, respectively $(\mathrm{dB})$. If the actual antenna radiation patterns are not available, the variation of gain with off-boresight angle may be obtained from the information in Recommendation ITU-R S. 465 .
To obtain the transmission loss, $L$, use:

$$
\begin{equation*}
L=L_{b}(p)-G_{t}-G_{r} \quad \mathrm{~dB} \tag{72}
\end{equation*}
$$

For clear-air interference scenarios where radio propagation is dominated by troposcatter, the elevation angles will be slightly greater than the radio horizon angles, $\theta_{t}$ and $\theta_{r}$. The use of these should introduce negligible error, unless these also coincide with their respective stations' boresight directions.

## $5 \quad$ Hydrometeor-scatter interference prediction

In contrast to the preceding clear-air prediction methods described above, the hydrometeor-scatter interference prediction methodology described below develops expressions for the transmission loss between two stations directly, since it requires a knowledge of the interfering and victim antenna radiation patterns for each station.
The method is quite general, in that it can be used with any antenna radiation pattern which provides a method for determining the antenna gain at any off-boresight axis angle. Radiation patterns such as those in Recommendations ITU-R P.620, ITU-R F.699, ITU-R F.1245, ITU-R S. 465 and ITU-R S.580, for example, can all be used, as can more complex patterns based Bessel functions and actual measured patterns if these are available. The method can also be used with omnidirectional or sectoral antennas, such as those characterized in Recommendation ITU-R F.1336, the gain of which is generally determined from the vertical off-boresight axis angle (i.e. the elevation relative to the angle of maximum gain).

The method is also general in that it is not restricted to any particular geometry, provided that antenna radiation patterns are available with $\pm 180^{\circ}$ coverage. Thus, it includes both main beam-to-main beam coupling and side lobe-to-main beam coupling, and both great-circle scatter and side-scatter geometries. The method can compute interference levels for both long-path (> 100 km ) and shortpath geometries (down to a few kilometres) with arbitrary elevation and azimuthal angles at either station. The methodology is therefore appropriate to a wide range of scenarios and services, including the determination of rain-scatter interference between two terrestrial stations, between a terrestrial station and an earth station, and between two earth stations operating in bidirectionally allocated frequency bands.

### 5.1 Introduction

The methodology is based on application of the bistatic radar equation, which can be written in terms of the power $P_{r}$ received at a receiving station from scattering by rain of the power $P_{t}$ transmitted by a transmitting station:

$$
\begin{equation*}
P_{r}=P_{t} \frac{\lambda^{2}}{(4 \pi)^{3}} \iiint_{\text {all space }} \frac{G_{t} G_{r} \eta A}{r_{t}^{2} r_{r}^{2}} \mathrm{~d} V \quad \mathrm{~W} \tag{73}
\end{equation*}
$$

where:
$\lambda$ : wavelength
$G_{t}$ : gain (linear) of the transmitting antenna
$G_{r}$ : gain (linear) of the receiving antenna
$\eta$ : scattering cross-section per unit volume, $\delta V\left(\mathrm{~m}^{2} / \mathrm{m}^{3}\right)$
$A$ : attenuation along the path from transmitter to receiver (in linear terms)
$r_{t}$ : distance from the transmitter to the scattering volume element
$r_{r}$ : distance from the scattering volume element to the receiver.

Expressed in terms of the transmission loss, (dB), for scattering between two stations, Station 1 and Station 2, the bistatic radar equation becomes:

$$
\begin{equation*}
L=178-10 \log N-20 \log f-10 \log Z_{R}-10 \log C-10 \log S+A_{g}-M \quad \mathrm{~dB} \tag{74}
\end{equation*}
$$

where:
$N$ : refractive index dependent Rayleigh Scattering term

$$
\begin{equation*}
N=\left|\frac{m^{2}-1}{m^{2}+2}\right|^{2} \tag{74a}
\end{equation*}
$$

$m$ : complex refractive index depending on frequency and atmospheric conditions
$f: \quad$ frequency ( GHz )
$Z_{R}: \quad$ radar reflectivity at ground level, which can be expressed in terms of the rainfall rate, $R(\mathrm{~mm} / \mathrm{h})$ :

$$
\begin{equation*}
Z_{R}=400 R^{1.4} \tag{75}
\end{equation*}
$$

$10 \log S$ : correction (dB), to account for the deviation from Rayleigh scattering at frequencies above 10 GHz :
$10 \log S= \begin{cases}R^{0.4} \cdot 10^{-3}\left[4(f-10)^{1.6}\left(\frac{1+\cos \varphi_{S}}{2}\right)+5(f-10)^{1.7}\left(\frac{1-\cos \varphi_{S}}{2}\right)\right] & \text { for } f>10 \mathrm{GHz} \\ 0 & \text { for } f \leq 10 \mathrm{GHz}\end{cases}$
where:
$\varphi s$ : scattering angle
$A_{g}$ : attenuation due to atmospheric gases along the path from transmitter to receiver (dB), calculated from Recommendation ITU-R P. 676 Annex 2
$M$ : any polarization mismatch between transmitting and receiving systems (dB).
In the model given here, scattering is confined to that within a rain cell, which is defined as being of circular cross-section, with a diameter depending on the rainfall rate:

$$
\begin{equation*}
d_{c}=3.3 R^{-0.08} \quad \mathrm{~km} \tag{77}
\end{equation*}
$$

Within the rain cell, the rainfall rate, and hence the radar reflectivity, is assumed to be constant up to the rain height, $h_{R}$. Above the rain height, the reflectivity is assumed to decrease linearly with height at a rate of $-6.5 \mathrm{~dB} / \mathrm{km}$.

The scatter transfer function, $C$, is then the volume integral over the rain cell and can be written, in cylindrical coordinates, as:

$$
\begin{equation*}
C=\int_{0}^{h_{\max }} \int_{0}^{2 \pi} \int_{0}^{\frac{d_{c}}{2}} \frac{G_{1} G_{2}}{r_{1}^{2} r_{2}^{2}} A \zeta \cdot r \mathrm{~d} r \mathrm{~d} \varphi \mathrm{~d} h \tag{78}
\end{equation*}
$$

where:
$G_{1}, G_{2}$ : linear gains of Station 1 and Station 2, respectively
$r_{1}, r_{2}$ : distances (km) from the integration element $\delta V$ to Station 1 and Station 2, respectively

A: attenuation due to rain, both inside and outside the rain cell, expressed in linear terms
$\zeta$ : height dependence of the radar reflectivity:

$$
\zeta= \begin{cases}1 & \text { for } h \leq h_{R}  \tag{79}\\ 10^{-0.65\left(h-h_{R}\right)} & \text { for } h>h_{R}\end{cases}
$$

$h_{R}: \quad$ rain height (km)
$r, \varphi, h: \quad$ variables of integration within the rain cell.
The integration is carried out numerically, in cylindrical coordinates. However, it is convenient initially to consider the geometry of the scattering from the transmitting station through a rain cell to the receiving station in terms of a Cartesian coordinate system with Station 1 taken as the origin, since the actual position of the rain cell will not immediately be defined, especially in the case of side scattering.

Within the Cartesian coordinate reference, it is advantageous, in terms of simplicity, first to convert the various geometrical parameters from their actual curved-Earth values to a plane-Earth representation.

The existence of main beam-to-main beam coupling between the antennas is established from the geometry, and the rain cell is then located at the point of intersection between the main beam axes. If main beam-to-main beam coupling does not exist, then the rain cell is located along the main beam axis of Station 1, centred at the point of closest approach to the main beam axis of Station 2. In this case, the transmission losses should be determined for a second case with the parameters of each station interchanged, and the worst-case loss distribution taken as representative of the likely interference levels.

### 5.2 Input parameters

Table 5 lists all the input parameters which are required for implementation of the method to calculate the cumulative distribution of transmission loss between two stations due to rain scatter.

TABLE 5

## List of input parameters

(Suffix 1 refers to parameters for Station 1, suffix 2 refers to parameters for Station 2)

| Parameter | Units | Description |
| :---: | :---: | :--- |
| $d$ | km | Distance between stations |
| $f$ | GHz | Frequency |
| $h_{1 \_l o c}, h_{2 \_l o c}$ | km | Local heights above mean sea level of Station 1, Station 2 |
| $G_{\text {max-1, }}, G_{\text {max-2 }}$ | dB | Maximum gains for each antenna |
| $h_{R}\left(p_{h}\right)$ | km | Cumulative distribution of rain height exceeded as a function of <br> percentage of time $p_{h}($ see Note 1$)$ |
| $M$ | dB | Polarization mismatch between systems |
| $P$ | hPa | Surface pressure (default 1013.25 hPa) |
| $R\left(p_{R}\right)$ | $\mathrm{mm} / \mathrm{h}$ | Cumulative distribution of rainfall rate exceeded as a function of <br> percentage of time $p_{R}$ |
| $T$ | ${ }^{\circ} \mathrm{C}$ | Surface temperature (default $15^{\circ} \mathrm{C}$ ) |

TABLE 5 (end)

| Parameter | Units | Description |
| :---: | :---: | :--- |
| $\alpha_{1 \_l o c,}, \alpha_{2 \_l o c}$ | rad | Local bearings of Station 1 from Station 2, and Station 2 from <br> Station 1, in the clockwise sense |
| $\varepsilon_{H \_l o c}, \varepsilon_{H 2 \_l o c}$ | rad | Local horizon angles for Station 1 and Station 2 |
| $\rho$ | $\mathrm{g} / \mathrm{m}^{3}$ | Surface water-vapour density (default 8 $\left.\mathrm{g} / \mathrm{m}^{3}\right)$ |
| $\tau$ | degrees | Polarization angle of link $\left(0^{\circ}\right.$ for horizontal polarization, $90^{\circ}$ for <br> vertical polarization) |

NOTE 1 - If the distribution is not available, use the median rain height, $h_{R}$, together with Table 6.

### 5.3 The step-by-step procedure

## Step 1: Determination of meteorological parameters

In order to derive the cumulative distribution of transmission loss due to rain scatter in terms of the percentage of time such losses are exceeded, the input parameters required are the probability distributions of rainfall rate and rain height. If local values for these are available, then these should be used. In the absence of local values, Recommendation ITU-R P. 837 can be used to obtain the cumulative distributions of rainfall rate for any location, while the median rain height can be obtained from Recommendation ITU-R P.839. As a default for the cumulative distribution of rain heights, the distribution of rain height relative to the median value in Table 6 can be used.

TABLE 6
Cumulative distribution of rain height relative to its median value

| Rain height difference <br> $(\mathbf{k m})$ | Probability of exceedance <br> $(\%)$ |
| :---: | :---: |
| -1.625 | 100.0 |
| -1.375 | 99.1 |
| -1.125 | 96.9 |
| -0.875 | 91.0 |
| -0.625 | 80.0 |
| -0.375 | 68.5 |
| -0.125 | 56.5 |
| 0.125 | 44.2 |
| 0.375 | 33.5 |
| 0.625 | 24.0 |
| 0.875 | 16.3 |
| 1.125 | 10.2 |
| 1.375 | 6.1 |
| 1.625 | 3.4 |
| 1.875 | 1.8 |
| 2.125 | 0.9 |
| 2.375 | 0.0 |

The cumulative distributions of both rainfall rate and rain height are converted into probability density functions in the following way. For each interval between two adjacent values of rainfall-rate or rainheight, the mean value is taken as being representative for that interval, and its probability of occurrence is the difference between the two corresponding exceedance probabilities. Any values for which $h_{R}$ is less than 0 km when using Table 5 are set to 0 km with their probabilities being added together.
It is assumed that rainfall rate and rain height are statistically independent of each other, so that the probability of occurrence for any given pair of rainfall-rate/rain-height combinations is simply the product of the individual probabilities.
For each pair of rainfall-rate/rain-height values, the transmission loss is calculated according to the following steps.

## Step 2: Conversion of geometrical parameters to plane-Earth representation

The geometry of rain scattering between two stations is determined from the basic input parameters of the great-circle distance $d$ between the two stations, the local values for the elevation angles of each station antenna, $\varepsilon 1$-loc and $\varepsilon 2$-loc, and azimuthal offsets of the antenna main-beam axes for each station from the direction of the other station defined as positive in the clockwise sense, $\alpha_{1-l o c}$ and $\alpha_{2}-$ loc. Station 1 is taken as the reference position, i.e. the origin, for the Cartesian coordinate system, and the reference parameters are thus:

$$
\begin{equation*}
\varepsilon_{1}=\varepsilon_{1_{-} l o c}, \alpha_{1}=\alpha_{1 \_l o c} \text { and: } \varepsilon_{H 1}=\varepsilon_{H 1 \_l o c} \quad \mathrm{rad} \tag{80}
\end{equation*}
$$

First convert all the geometrical parameters to a common Cartesian coordinate system, taking Station 1 as the origin, with the horizontal plane as the $x-y$ plane, the $x$-axis pointing in the direction of Station 2 and the $z$-axis pointing vertically upwards. Figure 4 illustrates the geometry on the curved Earth (for the simplified case of forward scattering, i.e. along the great circle), where $r_{\text {eff }}$ is the effective radius of the Earth,

$$
\begin{equation*}
r_{e f f}=k_{50} R_{E} \quad \mathrm{~km} \tag{81}
\end{equation*}
$$

where:

$$
\begin{array}{ll}
k_{50}: & \text { median effective Earth radius factor }=1.33 \\
R_{E}: & \text { true Earth radius }=6371 \mathrm{~km} .
\end{array}
$$

The two stations are separated by the great-circle distance $d(\mathrm{~km})$, subtending an angle $\delta$ at the Earth's centre:

$$
\begin{equation*}
\delta=\frac{d}{r_{e f f}} \quad \text { rad } \tag{82}
\end{equation*}
$$

The local vertical at Station 2 is tilted by the angle $\delta$ from the local vertical at Station 2, i.e. the $Z$-axis. The elevation and azimuthal angles of Station 2 are thus converted to the plane-Earth representation as follows, where the subscript loc refers to the local values.
Calculate the elevation angle of Station 2:

$$
\begin{equation*}
\varepsilon_{2}=\arcsin \left(\cos \varepsilon_{2_{-} l o c} \cos \alpha_{2_{-} l o c} \sin \delta+\sin \varepsilon_{2_{-} l o c} \cos \delta\right) \tag{83}
\end{equation*}
$$

and the horizon angle at Station 2:

$$
\begin{equation*}
\varepsilon_{H 2}=\arcsin \left(\cos \varepsilon_{H 2 \_l o c} \cos \alpha_{2_{-} l o c} \sin \delta+\sin \varepsilon_{H 2_{-} l o c} \cos \delta\right) \tag{84}
\end{equation*}
$$

The azimuthal offset of Station 2 from Station 1 is:

$$
\begin{equation*}
\alpha_{2}=\arctan \left(\frac{\cos \varepsilon_{2 \_l o c} \sin \alpha_{2_{-}} l o c}{\cos \varepsilon_{2_{-}} l o c} \cos \alpha_{2_{-} l o c} \cos \delta-\sin \varepsilon_{2_{-} l o c} \sin \delta\right) ~ \tag{85}
\end{equation*}
$$

and the height of Station 2 above the reference plane is given by:

$$
\begin{equation*}
h_{2}=h_{2 \_l o c}-h_{1}-d \frac{\delta}{2} \quad \mathrm{~km} \tag{86}
\end{equation*}
$$

The azimuthal separation between the two stations at the point of intersection between ground-plane projections of the main-beam axes is:

$$
\begin{equation*}
\alpha_{S}=\pi-\left(\alpha_{1}-\alpha_{2}\right) \quad \operatorname{rad} \tag{87}
\end{equation*}
$$

FIGURE 4
Geometry of stations on curved Earth


Step 3: Determination of link geometry
The method for determining the geometry of the scatter links uses vector notation, in which a vector in three-dimensional space is represented by a three-element single-column matrix comprising the lengths of the projections of the line concerned onto the Cartesian $x, y$ and $z$ axes. A vector will be represented by a symbol in bold typeface. Thus, a vector assignment may, in general, be written:

$$
\mathbf{V}=\left[\begin{array}{l}
x \\
y \\
z
\end{array}\right]
$$

A unit-length vector will, in general, be represented by the symbol $\mathbf{V}$, while a general vector (i.e. including magnitude) will be represented by another, appropriate symbol, for example $\mathbf{R}$.

The basic geometry for rain scattering is illustrated schematically in Fig. 5 for the general case of side scattering, where the two main-beam axes do not, in fact, intersect. In other words, this example represents side-lobe to main-lobe coupling. The interference path may be from the Station 2 sidelobes into the Station 1 main beam, or vice versa.

FIGURE 5
Schematic of rain scatter geometry for the general case of side scattering


The centre of the rain cell is located along the main beam antenna axis of Station 1 at the point of closest approach between the two antenna beams. The geometry is established in vector notation as follows.

The vector from Station 1 to Station 2 is defined as:

$$
\mathbf{R}_{\mathbf{1 2}}=\left[\begin{array}{l}
d  \tag{88}\\
0 \\
h_{2}
\end{array}\right] \quad \mathrm{km}
$$

The vectors $\mathbf{R}_{\mathbf{1 2}}, r_{2} \mathbf{V}_{\mathbf{2 0}}, r_{s} \mathbf{V}_{\mathbf{S 0} 0}$ and $r_{1} \mathbf{V}_{\mathbf{1 0}}$ form a closed three-dimensional polygon, with the vector $\mathbf{V}_{\mathbf{S 0}}$ perpendicular to both $\mathbf{V}_{\mathbf{1 0}}$ and $\mathbf{V}_{\mathbf{2 0}}$. In the example illustrated in Fig. 5, the vector $\mathbf{V}_{\mathbf{5 0}}$ is directed into the page.

Taking the curvature of the Earth into account, calculate the unit-length vector $\mathbf{V}_{\mathbf{1 0}}$ in the direction of the Station 1 antenna main beam:

$$
\mathbf{V}_{\mathbf{1 0}}=\left[\begin{array}{c}
\cos \varepsilon_{1} \cos \alpha_{1}  \tag{89}\\
-\cos \varepsilon_{1} \sin \alpha_{1} \\
\sin \varepsilon_{1}
\end{array}\right]
$$

and the unit-length vector $\mathbf{V}_{\mathbf{2 0}}$ in the direction of the Station 2 antenna main beam:

$$
\mathbf{V}_{\mathbf{2 0}}=\left[\begin{array}{c}
\sin \varepsilon_{2_{-} l o c} \sin \delta-\cos \varepsilon_{2_{-} l o c} \cos \alpha_{2_{-} l o c} \cos \delta  \tag{90}\\
\cos \varepsilon_{2_{-} l o c} \sin \alpha_{2_{-}} l o c \\
\sin \varepsilon_{2_{-} l o c} \cos \delta+\cos \varepsilon_{2_{-} l o c} \cos \alpha_{2_{-} l o c} \sin \delta
\end{array}\right]
$$

The method now uses the scalar product of two vectors, which is written and evaluated as:

$$
\mathbf{V}_{\mathbf{1}} \cdot \mathbf{V}_{\mathbf{2}}=x_{1} x_{2}+y_{1} y_{2}+z_{1} z_{2}
$$

where:

$$
\mathbf{V}_{\mathbf{1}}=\left[\begin{array}{l}
x_{1} \\
y_{1} \\
z_{1}
\end{array}\right]
$$

The scattering angle $\varphi s$, i.e. the angle between the two antenna beams, is determined from the scalar product of the two vectors $\mathbf{V}_{10}$ and $\mathbf{V}_{\mathbf{2 0}}$ :

$$
\begin{equation*}
\varphi_{S}=\arccos \left(-\mathbf{V}_{\mathbf{2 0}} \cdot \mathbf{V}_{\mathbf{1 0}}\right) \tag{91}
\end{equation*}
$$

If $\varphi s<0.001 \mathrm{rad}$, then the two antenna beams are approximately parallel, and it can be assumed that any coupling by rain scatter will be negligible.
As indicated in Fig. 5, the four vectors $\mathbf{R}_{\mathbf{1 2}}, r_{\mathbf{2}} \mathbf{V}_{\mathbf{2 0}}, r_{s} \mathbf{V}_{\mathbf{S 0}}$ and $r_{1} \mathbf{V}_{\mathbf{1 0}}$ form a closed three-dimensional polygon, i.e.:

$$
\begin{equation*}
\mathbf{R}_{\mathbf{1 2}}+r_{2} \mathbf{V}_{20}-r_{S} \mathbf{V}_{\mathbf{S} 0}-r_{1} \mathbf{V}_{\mathbf{1 0}}=0 \tag{92}
\end{equation*}
$$

and this can be solved for the distances $r_{i}$. The method uses the vector product of two vectors, which is written and evaluated as follows. The vector (or cross) product is:

$$
\mathbf{V}_{\mathbf{1}} \times \mathbf{V}_{\mathbf{2}}=\left[\begin{array}{l}
y_{1} z_{2}-z_{1} y_{2} \\
z_{1} x_{2}-x_{1} z_{2} \\
x_{1} y_{2}-y_{1} x_{2}
\end{array}\right]
$$

The unit-length vector $\mathbf{V}_{\mathbf{S} \mathbf{0}}$, which is perpendicular to both antenna beams, is calculated from the vector product $\mathbf{V}_{\mathbf{2 0}} \times \mathbf{V}_{\mathbf{1 0}}$ :

$$
\begin{equation*}
\mathbf{V}_{\mathbf{S} \mathbf{0}}=\frac{\mathbf{V}_{\mathbf{2 0}} \times \mathbf{V}_{\mathbf{1 0}}}{\sin \varphi_{S}} \tag{93}
\end{equation*}
$$

Equation (92) can now be solved using the determinant of three vectors, which is written and evaluated thus:

$$
\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{\mathbf{1}} & \mathbf{V}_{\mathbf{2}} & \mathbf{V}_{\mathbf{3}}
\end{array}\right]=\operatorname{det}\left[\begin{array}{lll}
x_{1} & x_{2} & x_{3} \\
y_{1} & y_{2} & y_{3} \\
z_{1} & z_{2} & z_{3}
\end{array}\right]=x_{1}\left(y_{2} z_{3}-y_{3} z_{2}\right)+x_{2}\left(y_{3} z_{1}-y_{1} z_{3}\right)+x_{3}\left(y_{1} z_{2}-y_{2} z_{1}\right)
$$

Calculate the distance between the two beams at their closest approach:

$$
r_{S}=\frac{\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{10} & \mathbf{V}_{20} & \mathbf{R}_{12}
\end{array}\right]}{\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{10} & \mathbf{V}_{20} & \mathbf{V}_{\mathbf{S 0}} \tag{94}
\end{array}\right]}
$$

The slant-path distance $r_{1}$ from Station 1 along its main beam to the point of closest approach to the Station 2 main beam is:

$$
r_{1}=\frac{\operatorname{det}\left[\begin{array}{lll}
\mathbf{R}_{12} & \mathbf{V}_{20} & \mathbf{V}_{\mathbf{S 0}}
\end{array}\right]}{\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{\mathbf{1 0}} & \mathbf{V}_{\mathbf{2 0}} & \mathbf{V}_{\mathbf{S 0}} \tag{95}
\end{array}\right]}
$$

While the corresponding slant-path distance $r_{2}$ from Station 2 along its main beam to the point of closest approach to the Station 1 main beam (noting the unary minus) is:

$$
r_{2}=\frac{-\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{\mathbf{1 0}} & \mathbf{R}_{12} & \mathbf{V}_{\mathbf{S 0}}
\end{array}\right]}{\operatorname{det}\left[\begin{array}{lll}
\mathbf{V}_{\mathbf{1 0}} & \mathbf{V}_{\mathbf{2 0}} & \mathbf{V}_{\mathbf{S 0}} \tag{96}
\end{array}\right]}
$$

Calculate the off-axis squint angle $\psi_{1}$ at Station 1 of the point of closest approach on the Station 2 main beam axis:

$$
\begin{equation*}
\Psi_{1}=\arctan \left(\frac{\left|r_{S}\right|}{r_{1}}\right) \tag{97}
\end{equation*}
$$

and the corresponding off-axis squint angle at Station 1 of the point of closest approach on the Station 1 main beam axis:

$$
\begin{equation*}
\Psi_{2}=\arctan \left(\frac{\left|r_{S}\right|}{r_{2}}\right) \tag{98}
\end{equation*}
$$

From these parameters, determine whether or not there is main beam-to-main beam coupling between the two stations. For there to be main beam-to-main beam coupling, the squint angle should be less than the 3 dB beamwidth of the relevant antenna. For squint angles greater than this, there will effectively be little or no main beam-to-main beam coupling, and the transmission path will be influenced predominantly by side-lobe-to-main beam coupling. If this be the case, two possibilities should be investigated, with the centre of the rain cell located along the main-beam axis of each antenna in turn, and the lowest transmission loss taken to represent the worst-case situation. Since the
default location of the rain cell is at the point of closest approach along the main-beam axis of Station 1, this can easily be accomplished by substituting the parameters of Station 2 for those of Station 1, and vice versa.
Finally, it is necessary also to determine the horizontal projections of the various distances calculated above, from which the location of the rain cell can be established. Figure 6 shows a plan view for the general case of side scattering.

FIGURE 6


Calculate the horizontal distance from Station 1 to the centre of the rain cell, defined as that point on the ground immediately below the point of closest approach on the Station 1 main-beam axis:

$$
\begin{equation*}
d_{1}=r_{1} \cos \varepsilon_{1} \quad \mathrm{~km} \tag{99}
\end{equation*}
$$

and the corresponding horizontal distance from Station 2 to the ground-plane projection of its point of closest approach:

$$
\begin{equation*}
d_{2}=r_{2} \cos \varepsilon_{2} \quad \mathrm{~km} \tag{100}
\end{equation*}
$$

The height above the ground of the point of closest approach on the Station 1 main-beam axis is:

$$
\begin{equation*}
h_{0}=\left|r_{1}\right| \sin \varepsilon_{1} \quad \mathrm{~km} \tag{101}
\end{equation*}
$$

while, for cases where there is no main beam-to-main beam coupling, the height of the point of closest approach on the Station 2 main-beam axis is:

$$
\begin{equation*}
h_{1,2_{-} 0}=\left|r_{1,2}\right| \sin \varepsilon_{1,2}-h_{c 1,2} \quad \mathrm{~km} \tag{102}
\end{equation*}
$$

The height parameters associated with the rain cell need to be corrected for any offset from the greatcircle path in the case of side scattering. The distance from the great-circle path between the two stations is:

$$
\begin{equation*}
d_{p}=d_{1} \sin \alpha_{1} \tag{103}
\end{equation*}
$$

and the angular separation is then:

$$
\begin{equation*}
\delta_{p}=\frac{d_{p}}{r_{e f f}} \quad \mathrm{~km} \tag{104}
\end{equation*}
$$

Now determine the correction for side scattering:

$$
\begin{equation*}
h_{c 1,2}=\left(r_{e f f}+h_{1,2}\right)\left(\frac{1}{\cos \left(\delta_{p}\right)}-1\right) \quad \mathrm{km} \tag{105}
\end{equation*}
$$

Note that this correction is also be applied to other parameters associated with the rain cell, i.e. the rain height, $h_{R}$ and the upper limit for integration, $h_{\text {top }}$, and in the determination of gaseous attenuation (see Step 8), which requires the use of local parameters.

This now establishes the main static geometrical parameters for locating the rain cell with respect to the stations and for evaluating the transmission loss due to rain scatter. It is necessary now to consider the geometry for the integration element, which can be anywhere within the rain cell, up to a predetermined upper limit for the integration, $h_{\text {top }}$, in order to determine the antenna gains at each point within the rain cell and the path attenuations within the rain cell in the directions of each station. To do this, the coordinate system is changed to cylindrical coordinates $(r, \varphi, h)$, centred on the rain cell.

## Step 4: Determination of geometry for antenna gains

In order to calculate the gain of each antenna at the integration element at coordinates $(r, \varphi, h)$ using such an antenna radiation pattern, and the path attenuation within the rain cell, it is necessary to calculate the off-axis boresight angle at the position of the integration element and the path lengths from the integration element to the edge of the rain cell in the directions of each station. Figure 7 illustrates the geometry, where point A represents an arbitrary integration element at coordinates $(r, \varphi$, $h$ ), and point B is the projection of this point on the ground plane. A plan view of the geometry is shown in Fig. 8.

FIGURE 7
Geometry for determination of antenna gains and path attenuation within the rain cell


FIGURE 8
Plan view of geometry to determine antenna gains


Calculate the horizontal distance from Station 1 to point B:

$$
\begin{equation*}
d_{B 1}=\sqrt{r^{2}+d_{1}^{2}+2 r d_{1} \cos \varphi} \quad \mathrm{~km} \tag{106}
\end{equation*}
$$

and the angle between this path and the horizontal projection of the Station 1 antenna main-beam axis:

$$
\begin{equation*}
\delta \alpha_{1}=\arcsin \left(\frac{r \sin \varphi}{d_{B 1}}\right) \tag{107}
\end{equation*}
$$

The elevation angle of point A from Station 1 is given by:

$$
\begin{equation*}
\varepsilon_{A 1}=\arctan \left(\frac{h}{d_{B 1}}\right) \tag{108}
\end{equation*}
$$

The unit-length vector from Station 1 to point A is defined as:

$$
\mathbf{V}_{\mathbf{A 1}}=\left[\begin{array}{c}
\cos \varepsilon_{A 1} \cos \left(\alpha_{1}-\delta \alpha_{1}\right)  \tag{109}\\
-\cos \varepsilon_{A 1} \sin \left(\alpha_{1}-\delta \alpha_{1}\right) \\
\sin \varepsilon_{A 1}
\end{array}\right]
$$

Determine the antenna off-axis boresight angle of the point $(r, \varphi, h)$ for the Station 1 antenna:

$$
\begin{equation*}
\theta_{b 1}=\arccos \left(\mathbf{V}_{\mathbf{A} \mathbf{1}} \cdot \mathbf{V}_{\mathbf{1 0}}\right) \tag{110}
\end{equation*}
$$

The distance from Station 1 to point A is:

$$
\begin{equation*}
r_{A 1}=\frac{d_{B 1}}{\cos \varepsilon_{A 1}} \quad \mathrm{~km} \tag{111}
\end{equation*}
$$

and, noting that the vectors $\mathbf{R}_{12}, \mathbf{R}_{\mathbf{A} 2}$ and $\mathbf{R}_{\mathbf{A} 1}=r_{A 1} \mathbf{V}_{\mathbf{A} 1}$ form a closed triangle, the vector from Station 2 towards the point A at $(r, \varphi, h)$ can be found from:

$$
\begin{equation*}
\mathbf{R}_{\mathrm{A} 2}=\mathbf{R}_{\mathbf{1 2}}-r_{A 1} \mathbf{V}_{\mathrm{A} \mathbf{1}} \quad \mathrm{~km} \tag{112}
\end{equation*}
$$

The distance from Station 2 to point A is then calculated from:

$$
\begin{equation*}
r_{A 2}=\left|\mathbf{R}_{\mathbf{A} 2}\right| \quad \mathrm{km} \tag{113}
\end{equation*}
$$

while the unit vector from Station 1 in the direction of the integration element is:

$$
\begin{equation*}
\mathbf{V}_{\mathbf{A} 2}=\frac{\mathbf{R}_{\mathbf{A} 2}}{r_{A 2}} \tag{114}
\end{equation*}
$$

Then determine the Station 2 antenna off-axis boresight angle of the integration element at point A, with coordinates $(r, \varphi, h)$ :

$$
\begin{equation*}
\theta_{b 2}=\arccos \left(-\mathbf{V}_{\mathbf{A} \mathbf{2}} \cdot \mathbf{V}_{\mathbf{2 0}}\right) \tag{115}
\end{equation*}
$$

The above method for determining the antenna gains is appropriate only to circular antennas. Should the Station 1 antenna be a sector or omnidirectional antenna, as deployed in point-to-multipoint broadcast systems, for example, a slightly different method is used to determine the antenna gain, which will vary only in the vertical direction (within the area covered by the rain cell). In this case, the off-axis boresight angle in the vertical direction is determined more simply from:

$$
\begin{equation*}
\theta_{b 1}=\left|\varepsilon_{A 1}-\varepsilon_{1}\right| \tag{116}
\end{equation*}
$$

Similarly, if the Station 2 antenna is a sector or omnidirectional antenna, the off-axis boresight angle in the vertical direction is determined from:

$$
\begin{equation*}
\theta_{b 2}=\left|\varepsilon_{A 2}-\varepsilon_{2}\right| \tag{117}
\end{equation*}
$$

where:

$$
\begin{equation*}
\varepsilon_{A 2}=\arctan \left(\frac{h}{d_{B 2}}\right) \tag{118}
\end{equation*}
$$

and:

$$
\begin{equation*}
d_{B 2}=\sqrt{d^{2}+d_{B 1}^{2}-2 d \cdot d_{B 1} \cos \left(\alpha_{1}-\delta \alpha_{1}\right)} \quad \mathrm{km} \tag{119}
\end{equation*}
$$

It is important to remember that the off-axis boresight angles are customarily specified in degrees when used in typical antenna radiation patterns, whereas the trigonometrical functions in most software packages generally calculate in radians. A simple conversion from radians to degrees is thus generally necessary before these angles are used in the integration procedures.
The antenna gains can then be obtained from the antenna radiation pattern, from the maximum gain of the antenna and the off-axis boresight angle, which is a function of the location within the rain cell. As a default, the radiation patterns in either Recommendation ITU-R P. 620 (also ITU-R F.699) or ITU-R F. 1245 can be used, noting that the latter has lower side lobe levels. Note that the gains are required in linear terms for the integration.

## Step 5: Determination of path lengths within the rain cell

The losses from the integration element towards each of the stations, $A_{1}$ and $A_{2}$, which depend on the path lengths and position of the integration element within the rain cell, are now determined.
The rain cell is divided into three volumes, shown in Fig. 9. In the lower volume, the scattering crosssection is constant throughout the rain cell and is determined by the radar reflectivity $Z_{R}$ at ground level, with $\zeta(h)=1$. The paths within the rain cell in the directions toward each station, $x_{1}$ and $x_{2}$, are subject to attenuation by rain. In the middle volume, the integration element is above the rain height, and the scattering cross-section decreases as a function of height above the rain height, at a rate of $-6.5 \mathrm{~dB} / \mathrm{km}$. However, a fraction $f$ of each path may still pass through the rain below the rain height, depending on the geometry, and these paths are thus subject to additional attenuation by rain along those fractional path lengths $f_{x 1,2}$ which pass through the cell.

In the upper volume, the integration element is above the rain cell and no portion of the paths passes through the rain cell below the rain height. Such paths therefore do not suffer any attenuation by rain.

The path lengths in these volumes are now evaluated in the following steps.

FIGURE 9

P.0452-09

## Lower volume

In the lower volume, the integration element is always below the rain height $h_{R}$, and the paths within the rain cell are all subject to attenuation by rain, i.e.:

$$
\begin{equation*}
A_{1,2}=\gamma_{R 1,2} x_{1,2} \quad \mathrm{~dB} \tag{120}
\end{equation*}
$$

where $\gamma_{R 1,2}=k_{1,2} R^{\alpha_{1,2}}$ is the rain specific attenuation, $(\mathrm{dB} / \mathrm{km})$, and the coefficients $k_{1,2}$ and $\alpha_{1,2}$ are given as functions of frequency $f$, polarization $\tau$ and path elevation $\varepsilon_{1,2}$ in Recommendation ITU-R P.838. Note that the specific rain attenuation depends on the path elevation angle and, in principle, should be calculated for each integration element for each value of the coordinates ( $r, \varphi, h$ ). However, the variation with elevation angle is small, and it is sufficient to determine the values for $\gamma_{R}$ only once for the paths toward each station based on the respective antenna elevation angles.
The path lengths $r_{x 1}, r_{x 2}, x_{1}$ and $x_{2}$ are derived from the geometry, as follows. Figure 10 shows a horizontal plan view through the ground-plane projection point $B$ of the integration element $A$. Here, the corrected height of Station $2, h_{2}$, is assumed initially to be zero. This is taken into account later.

FIGURE 10
Plan view of scatter geometry through the integration element


Calculate the horizontal distance $d_{x 1}$ from Station 1 to the edge of the rain cell (point $\mathrm{X}_{1}$ ) is found from the cosine rule (taking the negative sign, since this is to the nearest edge):

$$
\begin{equation*}
d_{x_{1}}=d_{1} \cos \delta \alpha_{1}-\sqrt{d_{1}^{2} \cos ^{2} \delta \alpha_{1}-d_{1}^{2}+\left(\frac{d_{c}}{2}\right)^{2}} \quad \mathrm{~km} \tag{121}
\end{equation*}
$$

The slant-path distance to the edge of the rain cell is then:

$$
\begin{equation*}
r_{x 1}=\frac{d_{x 1}}{\cos \varepsilon_{A 1}} \quad \quad \mathrm{~km} \tag{122}
\end{equation*}
$$

Determine the offset angle of the integration element at point A for Station 2:

$$
\begin{equation*}
\delta \alpha_{2}=\arctan \left(\frac{-r \sin \left(\varphi+\alpha_{S}^{\prime}\right)}{d_{2}^{\prime}+r \cos \left(\varphi+\alpha_{S}^{\prime}\right)}\right) \tag{123}
\end{equation*}
$$

where $\alpha_{S}^{\prime}$ is given by:

$$
\begin{equation*}
\alpha_{S}^{\prime}=\arcsin \left(\frac{d}{d_{2}^{\prime}} \sin \alpha_{1}\right) \tag{124}
\end{equation*}
$$

and:

$$
\begin{equation*}
d_{2}^{\prime}=\sqrt{d^{2}+d_{1}^{2}-2 d \cdot d_{1} \cos \alpha_{1}} \quad \mathrm{~km} \tag{125}
\end{equation*}
$$

The horizontal distance $d_{x 2}$ is then found from the cosine rule:

$$
\begin{equation*}
d_{x 2}=d_{2}^{\prime} \cos \delta \alpha_{2}^{\prime}-\sqrt{\left(\frac{d_{c}}{2}\right)^{2}-d_{2}^{\prime 2} \sin ^{2} \delta \alpha_{2}^{\prime}} \quad \mathrm{km} \tag{126}
\end{equation*}
$$

Calculate the distance from Station 2 to the edge of the cell:

$$
\begin{equation*}
r_{x 2}=\frac{d_{x 2}}{\cos \varepsilon_{A 2}} \quad \mathrm{~km} \tag{127}
\end{equation*}
$$

Now, two cases need to be considered:
Case 1: when Station 1 is located outside the rain cell, i.e. when $d_{1}>d_{d} / 2$. In this case, only a portion of the path from the integration element A to Station 1 will be within the rain cell and hence subject to attenuation.

Case 2: when the elevation angle is very high and Station 1 is located within the rain cell, when $d_{1} \leq d_{c} / 2$. In this case, the entire path up to the rain height will always be within the rain cell and will thus suffer attenuation.
The path length $x_{1}$ for rain attenuation along the path towards Station 1 is determined from the following expression:

$$
x_{1}=\left\{\begin{array}{ll}
r_{A 1}-r_{x 1} & \text { if } d_{1}>\frac{d_{c}}{2}  \tag{128}\\
r_{A 1} & \text { if } d_{1} \leq \frac{d_{c}}{2}
\end{array} \quad \mathrm{~km}\right.
$$

and the path length $x_{2}$ for rain attenuation along the path towards Station 2 is determined from:

$$
x_{2}=\left\{\begin{array}{ll}
r_{A 2}-r_{x 2} & \text { if } d_{2}>\frac{d_{c}}{2}  \tag{129}\\
r_{A 2} & \text { if } d_{2} \leq \frac{d_{c}}{2}
\end{array} \quad \mathrm{~km}\right.
$$

Thus, for cases where the integration element is below the rain height, the attenuation through the rain cell can be determined, in linear terms, from:

$$
\begin{equation*}
A_{b}=\exp \left[-k\left(\gamma_{R 1} x_{1}+\gamma_{R 2} x_{2}\right)\right] \quad \text { if } h \leq h_{R} \tag{130}
\end{equation*}
$$

where:

$$
k=0.23026 \text { is a constant to convert attenuation in } \mathrm{dB} \text { to Nepers. }
$$

## Middle and upper volumes

In these volumes, the integration element is above the rain height, $h_{R}$, but some portions of the paths towards each of the stations may pass through the rain below $h_{R}$. This will occur only when the elevation angles of the integration element $\mathrm{A}, \varepsilon_{A 1,2}$, is less than the angles $\varepsilon_{C 1,2}$ subtended at each station by the nearest upper corner of the rain cell, i.e. if:

$$
\varepsilon_{A 1}<\varepsilon_{C 1}=\arctan \left(\frac{h_{R}}{d_{x 1}}\right)
$$

and:

$$
\varepsilon_{A 2}<\varepsilon_{C 2}=\arctan \left(\frac{h_{R}-h_{2}}{d_{x 2}}\right)
$$

In these cases, the resultant attenuation must be taken into account. This is particularly relevant for Case 2 above, when one of the antennas has a very high elevation angle and the station is located within the rain cell.

From Fig. 9, the heights at which the rays from the integration element at point A pass through the edges of the rain cell can be determined from the ratios of the horizontal distances from each station to the edge of the rain cell and to point B:

$$
\begin{align*}
& h_{e 1}=h \cdot \frac{d_{x 1}}{d_{B 1}} \\
& h_{e 2}=\left(h-h_{2}\right) \cdot \frac{d_{x 2}}{d_{B 2}}+h_{2} \tag{131}
\end{align*}
$$

The fractional of the path lengths $f x_{1,2}$ which pass through the rain cell can then be determined from ratios:

$$
f_{x 1,2}=\left\{\begin{array}{lll}
x_{1,2}\left(\frac{h_{R}-h_{e 1,2}}{h-h_{e 1,2}}\right) & \text { if } h>h_{R}>h_{e 1,2} & \text { and } \varepsilon_{A 1,2}<\varepsilon_{\mathrm{C} 1,2} \tag{132}
\end{array} \quad \mathrm{~km}\right.
$$

Finally, calculate the attenuation, in linear terms, for cases where the integration element is above the rain height, $h_{R}$ :

$$
\begin{equation*}
A=\exp \left[-k\left\{6.5\left(h-h_{R}\right)+\gamma_{R 1} f_{x 1}+\gamma_{R 2} f_{x 2}\right\}\right] \quad \text { for } h \geq h_{R} \tag{133}
\end{equation*}
$$

This Step then defines the integrand for the scatter transfer function.

## Step 6: Attenuation outside the rain cell

In the formulation used here, rain is confined solely to a cell with diameter $d_{c}$, defined by the geometry in Step 2, and the rainfall rate is considered uniform within that cell. In general, the rain will extend beyond this region, decreasing in intensity as the distance from the cell centre increases, and this must be taken into account. However, if the station is located inside the rain cell, then there will be no external rain attenuation to be considered for that station. Furthermore, if the integration element is sufficiently far above the rain height that no part of the path to either station passes through the rain cell, then no external attenuation is included along that path.
As an approximation, the rain outside the rain cell is assumed to decay with a scaling distance defined by:

$$
\begin{equation*}
r_{m}=600 R^{-0.5} 10^{-(R+1)^{0.19}} \quad \mathrm{~km} \tag{134}
\end{equation*}
$$

For scattering below the rain height, calculate the attenuation outside the rain cell using the following expression:

$$
A_{e x t 1,2}= \begin{cases}\frac{\gamma_{R 1,2} r_{m}}{\cos \varepsilon_{A 1,2}}\left[1-\exp \left(-\frac{d_{x 1,2}}{r_{m}}\right)\right] & \text { if } d_{1,2}>\frac{d_{c}}{2} \text { and } f_{x 1,2} \neq 0  \tag{135}\\ 0 & \text { if } d_{1,2} \leq \frac{d_{c}}{2} \text { or } f_{x 1,2}=0\end{cases}
$$

i.e. the attenuation along either path is set to zero if the relevant station is located within the rain cell ( $d_{1} \leq d_{c} / 2$ ) or if the integration element is above the rain cell and no part of the path passes through the rain cell, determined by whether or not the fractional paths $f_{x 1,2}$ are zero.

## Step 7: Numerical integration of the scatter transfer function

The integration is split into two sections, for scattering below the rain height and for scattering above the rain height:

$$
\begin{gather*}
C_{b}=\int_{h_{\min }}^{h_{R}} \int_{0}^{2 \pi} \int_{0}^{\frac{d_{c}}{2}} \frac{G_{1} G_{2}}{r_{A 1}^{2} r_{A 2}^{2}} \exp \left[-k\left(\gamma_{R 1} x_{1}+\gamma_{R 2} x_{2}+A_{\text {ext } 1}+A_{\text {ext } 2}\right)\right] \cdot r \mathrm{~d} r \mathrm{~d} \varphi \mathrm{~d} h  \tag{136}\\
C_{a}=\int_{h_{R}}^{h_{\text {top }}} \int_{0}^{2 \pi} \int_{0}^{\frac{d_{c}}{2}} \frac{G_{1} G_{2}}{r_{A 1}^{2} r_{A 2}^{2}} \exp \left[-k\left(6.5\left(h-h_{R}\right)+\gamma_{R 1} f_{x 1}+\gamma_{R 2} f_{x 2}+A_{\text {ext } 1}+A_{\text {ext } 2}\right)\right] \cdot r \mathrm{~d} r \mathrm{~d} \varphi \mathrm{~d} h \tag{137}
\end{gather*}
$$

where the antenna gains are specified in linear terms, as functions of the off-axis boresight angles $\theta_{b 1,2}(r, \varphi, h)$, and where:

$$
\begin{equation*}
r_{A 1,2}(r, h, \varphi)=\sqrt{\left(r \cos \varphi-d_{1,2}\right)^{2}+r^{2} \sin ^{2} \varphi+\left(h-h_{1,2}\right)^{2}} \quad \mathrm{~km} \tag{137a}
\end{equation*}
$$

The integration, in cylindrical coordinates, is carried out over the ranges: for $r$ from 0 to the radius of the rain cell, $d_{c} / 2$, and for $\varphi$ from 0 to $2 \pi$. Some constraints can be placed on the third integration variable, $h$, the height within the rain cell. The minimum height, $h_{\text {min }}$, is determined by the visibility of the rain cell from each of the stations.

If there be any shielding from terrain in the vicinity of either station, then scattering from heights within the rain cell which are not visible from either station should be precluded from the integration. The minimum height for integration can thus be determined from the horizon angles for each station, as:

$$
\begin{equation*}
h_{\min }=\max \left(d_{x 1} \tan \varepsilon_{H 1}, d_{x 2} \tan \varepsilon_{H 2}\right) \quad \mathrm{km} \tag{138}
\end{equation*}
$$

Note that local values are used here, since any inherent shielding due to the Earth's curvature at zero elevation is already taken into account in determining the off-axis boresight angles.
The maximum height for integration, $h_{t o p}$, can be defined, in order to minimize the computational requirements, since it will not, in general, be necessary to integrate the scattering cross-section at heights above which the antenna side lobe levels are significantly reduced. As a default value, the height above which the integration may be terminated without loss of accuracy is assumed to be 15 km.

The near field intensities of antennas are highly dependent on specific hardware details, and basic interference analysis may not have this information readily available. Therefore, it is appropriate to make an assumption that the field strength will be approximately on an order of magnitude as that found at the beginning of the far-field region. This approximation appears to be true in general with view to actual measurements of near field intensities.

Procedure to apply approximated near-field scatter power:

1) Determine if the transmitter or receiver near-field radius $d_{n f}=\frac{2 c G}{\pi^{2} f}$ is contained within the radius of the rain cell. The condition for this is $d_{1,2}+d_{n f}<d_{c} / 2$. If there is only partial containment such that $d_{1,2}-d_{n f}<d_{c} / 2$, then as an approximation assume full containment.
2) Apply the following condition to the integration procedure for equations (136) and (137):

$$
\text { if } \quad r_{A 1,2}<r_{n f} \quad \text { then } \quad r_{A 1,2}=r_{n f}
$$

Numerical integration: There are many methods available for numerical integration, and numerous mathematical software packages include intrinsic integration functions which can be exploited effectively. Where the user wishes to develop a dedicated package in other programming languages, methods based on iterative bisection techniques have proved effective. One such technique is the Romberg method, which is a higher-order variant of the basic trapezoidal (i.e. Simpson's) rule for integration by successive bisections of the integration intervals.
Romberg integration uses a combination of two numerical methods to calculate an approximation to a proper integral, i.e.:

$$
I=\int_{a}^{b} y(x) \mathrm{d} x
$$

The extended trapezoidal rule is used to calculate a sequence of approximations to the integral with the intervals between function evaluations being divided by two between each term. Polynomial extrapolation is then used to extrapolate the sequence to a zero-length interval.

The method can be summarized by the pseudo-code loop:

$$
\begin{aligned}
& \text { Index }=1 \\
& \text { WHILE estimated_error > desired_error DO }
\end{aligned}
$$

$$
\mathrm{S}(\text { Index })=\text { Trapezoidal Rule Approximation using } 2^{\text {Index }} \text { intervals }
$$

I = Polynomial Extrapolation of S

$$
\text { Index }=\operatorname{Index}+1
$$

ENDWHILE

## The extended trapezoidal rule

By linearly interpolating between $N+1$ equally spaced abscissae $\left(x_{i}, y_{i}\right)$ the integral can be approximated:

$$
I \approx T^{N}=h(N)\left(\frac{1}{2} y_{0}+y_{1} \cdots y_{N-1}+\frac{1}{2} y_{N}\right)
$$

where:

$$
h(N)=\frac{b-a}{N}: \quad \text { interval between abscissae. }
$$

The number of intervals can be doubled using the recursion:

$$
T^{2 N}=\frac{1}{2} T^{N}+h(2 N)\left(y_{1}+y_{3} \cdots y_{N-3}+y_{N-1}\right)
$$

The Romberg method recursively builds a sequence: $S(i)=T^{2^{i}}$.
Polynomial extrapolation: In the limit, the error in the extended trapezoidal approximation to $I$ is a polynomial in $h^{2}$, i.e.:

$$
I=T^{N}+\varepsilon^{N}
$$

where:

$$
\varepsilon^{N} \cong P\left(h^{2}(N)\right)
$$

and:

$$
P: \text { is an unknown polynomial. }
$$

The sequence of trapezoidal approximations, $T^{N}=\varepsilon^{N}$, is also a polynomial in $h^{2}$ and so polynomial extrapolation may be used to estimate the limit as $h \rightarrow 0$. If $m$ trapezoidal approximations are available, then a unique polynomial of degree $M-1$ may be fitted to the points $\left(h^{2}(n), T^{n}\right)$ for $n=1,2,4,8, \cdots, 2^{M-1}$. Evaluating this unique polynomial at $h=0$ yields an approximation to the limit of the trapezoidal method.
Usually Neville's method is used to calculate the value of the polynomial at $h=0$. Neville's method is efficient and yields an error estimate which may be used to terminate the Romberg integration. The method is a successive linear interpolation approximation to high degree Lagrangian polynomial interpolation.

The Lagrange method can be described as follows. For $M+1$ points ( $x_{i}, y_{i}$ ), a polynomial of degree $m$ can be defined as a linear combination of basic functions:

$$
P(x) \equiv \sum_{i=0}^{n} y_{i} L_{i}\left(x_{i}\right) \equiv \sum_{i=0}^{n} y_{i} \prod_{\substack{k=0 \\ k \neq i}}^{n} \frac{\left(x-x_{k}\right)}{\left(x_{i}-x_{k}\right)}
$$

i.e.

$$
L_{i}(x)=\frac{\left(x-x_{0}\right) \ldots\left(x-x_{i-1}\right)\left(x-x_{i+1}\right) \ldots\left(x-x_{n}\right)}{\left(x_{i}-x_{0}\right) \ldots\left(x_{i}-x_{i-1}\right)\left(x_{i}-x_{i+1}\right) \ldots\left(x_{i}-x_{n}\right)}
$$

This interpolation method requires all ordinates $y_{i}$ to be known in order to find an estimate of the solution at $x=0$, and for large problems this is not efficient, since it does not exploit previous interpolations when iterating to higher orders. Neville's method is a recursive process based on the relationship between one approximation to a polynomial and its two preceding approximations. Thus, for any two points $\left(x_{k}, y_{k}\right)$, there is a unique polynomial of degree 0 , i.e. a straight line, passing through those two points, $P_{k}=y_{k}$. A second iteration is performed in which the polynomial is fitted through pairs of point yielding $P_{12}, P_{23}, \ldots$, and the procedure repeated to build up a pyramid of approximations:


The final result can then be represented as:

$$
P_{i(i+1) \ldots(i+m)}=\frac{\left(x-x_{i+m}\right) P_{i(i+1) \ldots(i+m-1)}+\left(x_{i}-x\right) P_{(i+1)(i+2) \ldots(i+m)}}{x_{i}-x_{i+m}}
$$

Neville's method is thus a recursive process to complete the pyramid column-by-column, in a computationally efficient way.
In practice, the polynomial extrapolation becomes unstable when large numbers of points are fitted and so typically in Romberg integration, fourth degree polynomial extrapolation is used, fitting to the last five trapezoidal approximations.
Numerical integration methods, such as those which use bisection techniques, iterate until an accuracy (precision) criterion is met, whereby the iteration is terminated when the difference between successive iterations is smaller than a predetermined fraction of the previous result.
Typically, this fraction will be between $10^{-3}$ and $10^{-6}$, the latter value being close to the capabilities of 32 -bit processors. Care should be taken when using larger values above this range, since errors in the calculated losses may increase. As a general guide, a value of $10^{-4}$ is found to be a good compromise between accuracy and computational speed.

Three nested numerical integrations are required in order to carry out the three-dimensional volume integration over the rain cell, in cylindrical coordinates, with the outer integration being over the height parameter $h$, for example. This integration calls for the integral over the azimuthal parameter $\varphi$ at a particular value of $h$, which in turn calls for the integral over the radius parameter, $r$, for particular values of $(h, \varphi)$.
It should be noted that many iterations of the scatter transfer function are generally necessary in order to achieve the required precision, especially in cases where antenna gains are high and the product of the antenna gains can vary across the diameter of the rain cell by 60 dB or more. Computation times can therefore be many tens of minutes and even hours for more extreme cases, even with high-speed processors.

## Step 8: Determination of other loss factors

Calculate the deviation from Rayleigh scattering using equation (76) with the scattering angle $\varphi s$ given by equation (91).
Calculate the attenuation along the paths due to absorption by atmospheric gases using Annex 2 of Recommendation ITU-R P. 676 for the specific attenuations $\gamma_{o}$ and $\gamma_{w}$ and the equivalent heights $h_{o}$ and $h_{w}$ for dry air and water vapour respectively. The attenuations are determined using the following expressions for path attenuation between two altitudes above sea level, with the upper altitude being determined by the height of the quasi-intersection point between the two antenna beam main axes. This method is an approximation, since the actual gaseous attenuation will vary for each scattering element within the scattering volume. However, since gaseous attenuation is generally a minor component in the overall transmission loss, and its variability is small, when compared with the
uncertainties in other parameters such as rainfall rates, rain heights, and the geometry of the rain cell itself, this simplification is considered justifiable. The following method provides estimates of the gaseous attenuation with acceptable accuracy for the overall procedure.
The lower altitudes for each station are given by the local values $h l_{-l o c}=h_{2}$ loc . The upper altitude $h_{p}$ is the height of the quasi-intersection point, taking into account the Earth's curvature, i.e. the local value, which is found from:

$$
\begin{equation*}
h_{p}=h_{0}+\sqrt{d_{1}^{2}+r_{e f f}^{2}}-r_{e f f}+h_{c} \quad \mathrm{~km} \tag{139}
\end{equation*}
$$

For elevation angles between $5^{\circ}$ and $90^{\circ}$, the attenuation between two altitudes is determined from the difference between the total slant-path attenuations from each altitude:

$$
\begin{align*}
A_{o_{-} i} & =\frac{\gamma_{o} h_{o}-\gamma_{o} h_{o}\left[\exp \left(-\frac{h_{i_{-} l o c}}{h_{o}}\right)-\exp \left(-\frac{h_{p}}{h_{o}}\right)\right]}{\sin \varepsilon_{i_{-} l o c}}  \tag{140}\\
A_{w_{-} i}= & \frac{\gamma_{w} h_{o}-\gamma_{w} h_{o}\left[\exp \left(-\frac{h_{i_{-} l o c}}{h_{w}}\right)-\exp \left(-\frac{h_{p}}{h_{w}}\right)\right]}{\sin \varepsilon_{i_{-} l o c}} \tag{141}
\end{align*}
$$

where the index, $i$, refers to each of the two stations and $\varepsilon_{i_{-} l o c}$ are the local elevation angles of each antenna.

The water-vapour density, $\rho$, used to determine the specific attenuation $\gamma_{w}$ is the hypothetical sea-level value found from the ground-level value at the stations (which can be assumed to be the same):

$$
\begin{equation*}
\rho=\rho_{g} \exp \left(\frac{h_{i_{-} l o c}}{2}\right) \quad \mathrm{g} / \mathrm{m}^{3} \tag{142}
\end{equation*}
$$

For elevation angles between $0^{\circ}$ and $5^{\circ}$, it is necessary to take into account the effects of refraction. The elevation angles for the upper path are determined from:

$$
\begin{equation*}
\varepsilon_{1,2}^{\prime}=\arccos \left(\frac{h_{1,2}+r_{e f f}}{h_{p}+r_{e f f}} \cos \varepsilon_{1,2_{-} l o c}\right) \tag{143}
\end{equation*}
$$

The path attenuation is then given by the following expressions:
For dry air attenuation:

$$
A_{o_{-} i}=\gamma_{o} \sqrt{h_{o}}\left[\begin{array}{l}
\frac{\sqrt{h_{i_{-}} l o c}+r_{e f f}}{} \cdot F\left(\tan \varepsilon_{i} \sqrt{\frac{h_{i_{-}} l o c}{}+r_{e f f}}\right) \exp \left(-\frac{h_{i_{-} l o c}}{h_{o}}\right)  \tag{dB}\\
\cos \varepsilon_{i_{-} l o c} \\
-\frac{\sqrt{h_{p}+r_{e f f}} \cdot F\left(\tan \varepsilon_{i}^{\prime} \sqrt{\frac{h_{p}+r_{e f f}}{h_{o}}}\right) \exp \left(-\frac{h_{p}}{h_{o}}\right)}{\cos \varepsilon_{i}^{\prime}}
\end{array}\right] \mathrm{dB}
$$

and for water-vapour attenuation:

$$
A_{w_{-} i}=\gamma_{w} \sqrt{h_{w}}\left[\begin{array}{l}
\frac{\sqrt{h_{i_{-} l o c}+r_{e f f}} \cdot F\left(\tan \varepsilon_{i} \sqrt{\frac{h_{i_{-}} l o c}{}+r_{e f f}}\right) \exp \left(-\frac{h_{i_{-} l o c}}{h_{w}}\right)}{\cos \varepsilon_{i_{-} l o c}}  \tag{145}\\
-\frac{\sqrt{h_{p}+r_{e f f}} \cdot F\left(\tan \varepsilon_{i}^{\prime} \sqrt{\frac{h_{p}+r_{e f f}}{h_{w}}}\right) \exp \left(-\frac{h_{p}}{h_{w}}\right)}{\cos \varepsilon_{i}^{\prime}}
\end{array}\right] \mathrm{dB}
$$

where the function, $F$, is defined by:

$$
\begin{equation*}
F(x)=\frac{1}{0.661 x+0.339 \sqrt{x^{2}+5.51}} \tag{146}
\end{equation*}
$$

Include also any polarization mismatch, $M$, which is appropriate.
Step 9: Determination of the cumulative distribution of transmission loss
For each pair of rainfall rate and rain height values, calculate the transmission loss according to Steps 5 to 8, using the following expression:

$$
\begin{equation*}
L=178-10 \log N-20 \log f-10 \log Z_{R}-10 \log \left(C_{b}+C_{a}\right)-10 \log S+A_{g}-M \quad \mathrm{~dB} \tag{147}
\end{equation*}
$$

After all possible combinations of rainfall rate and rain height have been evaluated, the resulting values of transmission loss $(\mathrm{dB})$ are then truncated to the nearest higher integer dB value (using, for example a ceiling function), and the probabilities (in percentage terms) of all those combinations which yield the same loss are summed together, to derive the overall probability for each level of transmission loss. The resulting probability density function is then converted to the corresponding cumulative distribution of transmission loss, by summing the percentages for increasing values of loss.

# Attachment 1 <br> to Annex 1 

## Radio-meteorological data required for the clear-air prediction procedure

## 1 Introduction

The clear-air prediction procedures rely on radio-meteorological data to provide the basic location variability for the predictions. These data are provided in the form of maps which are contained in this Attachment.

## 2 Maps of vertical variation of radio refractivity data and surface refractivity

For the global procedure, the clear-air radio-meteorology of the path is characterized for the continuous (long-term) interference mechanisms by the average annual value of $\Delta N$ (the refractive index lapse-rate over the first 1 km of the atmosphere) and for the anomalous (short-term) mechanisms by the time percentage, $\beta_{0} \%$, for which the refractive gradient of the lower atmosphere is below -100 N -units $/ \mathrm{km}$. These parameters provide a reasonable basis upon which to model the clear-air propagation mechanisms described in $\S 2$ of Annex 1 . The value for average sea-level surface refractivity, $N_{0}$, is used for the calculation of the troposcatter model.
If local measurements are not available, these quantities may be obtained from the maps in the integral digital products supplied with this Recommendation in the supplement file R-REC-P.452-17-202109-I!!ZIP-E.zip. These digital maps were derived from analysis of a ten-year (1983-1992) global dataset of radiosonde ascents. The maps are contained in the files DN50.txt and N050.txt, respectively. The data are from $0^{\circ}$ to $360^{\circ}$ in longitude and from $+90^{\circ}$ to $-90^{\circ}$ in latitude, with a resolution of $1.5^{\circ}$ in both latitude and longitude. The data are used in conjunction with the companion data files LAT.txt and LON.txt containing respectively the latitudes and longitudes of the corresponding entries (grid points) in the files DN50.txt and N050.txt. For a location different from the grid points, the parameter at the desired location can be derived by performing a bi-linear interpolation on the values at the four closest grid points, as described in Recommendation ITU-R P. 1144.

## Attachment 2 <br> to Annex 1 <br> Path profile analysis

## 1 Introduction

For path profile analysis, a path profile of terrain heights above mean sea level is required. The parameters that need to be derived from the path profile analysis for the purposes of the propagation models are given in Table 7.

## 2 Construction of path profile

Based on the geographical coordinates of the interfering $\left(\varphi_{t}, \psi_{t}\right)$ and interfered-with $\left(\varphi_{r}, \psi_{r}\right)$ stations, terrain heights (above mean sea level) along the great-circle path should be derived from a topographical database or from appropriate large-scale contour maps. The distance between profile points should as far as is practicable capture significant features of the terrain. Typically, a distance increment between 30 m and 1 km is appropriate. In general, it is appropriate to use longer distance increments for longer paths. The profile should include the ground heights at the interfering and interfered-with station locations as the start and end points. The following equations take Earth curvature into account where necessary, based on the value of $a_{e}$ found in equation (6a).
Although equally-spaced profile points are considered preferable, it is possible to use the method with non-equally-spaced profile points. This may be useful when the profile is obtained from a digital map of terrain height contours. However, it should be noted that the Recommendation has been developed from testing using equally-spaced profile points; information is not available on the effect of non-equally-spaced points on accuracy.

For the purposes of this Recommendation the point of the path profile at the interferer is considered as point zero, and the point at the interfered-with station is considered as point $n$. The path profile therefore consists of $n+1$ points. Figure 11 gives an example of a path profile of terrain heights above mean sea level, showing the various parameters related to the actual terrain.

FIGURE 11

P.0452-11

Note to Fig.11: The value of $\theta_{t}$ as drawn will be negative.
Table 7 defines parameters used or derived during the path profile analysis.

TABLE 7
Path profile parameter definitions

| Parameter | Description |
| :---: | :--- |
| $a$ | Average physical Earth's radius (6 371 km) |
| $a_{e}$ | Effective Earth's radius (km) |
| $d$ | Great-circle path distance (km) |
| $d_{i}$ | Great-circle distance of the $i$-th terrain point from the interferer (km) |
| $d_{i i}$ | Incremental distance for regular path profile data (km) |
| $f$ | Frequency (GHz) |
| $\lambda$ | Wavelength (m) |
| $h_{t s}$ | Interferer antenna height (m) above mean sea level (amsl) |
| $h_{r s}$ | Interfered-with antenna height (m) (amsl) |
| $\theta_{t}$ | For a transhorizon path, horizon elevation angle above local horizontal (mrad), measured <br> from the interfering antenna. For a LoS path this should be the elevation angle toward <br> the interfered-with antenna |
| $\theta_{r}$ | For a transhorizon path, horizon elevation angle above local horizontal (mrad), measured <br> from the interfered-with antenna. For a LoS path this should be the elevation angle <br> toward the interfering antenna |
| $\theta$ | Path angular distance (mrad) |
| $h_{s t}$ | Height of the smooth-Earth surface (amsl) at the interfering station location (m) |
| $h_{s r}$ | Height of the smooth-Earth surface (amsl) at the interfered-with station location (m) |
| $h_{i}$ | Height of the $i$-th terrain point amsl (m) <br> $h_{0}:$ ground height of interfering station <br> $h_{n}:$ ground height of interfered-with station |
| $h_{m}$ | Terrain roughness (m) |
| $h_{t e}$ | Effective height of interfering antenna (m) |
| $h_{r e}$ | Effective height of interfered-with antenna (m) |

## 3 Path length

The path length can be obtained using great-circle geometry (based on the average physical Earth radius $a$ ) from the geographical coordinates of the interfering ( $\varphi_{t}, \psi_{t}$ ) and interfered-with ( $\varphi_{r}, \psi_{r}$ ) stations. Alternatively the path length can be found from a path profile. For general cases the path length, $d(\mathrm{~km})$, can be found from the path profile data:

$$
\begin{equation*}
d=\sum_{i=1}^{n}\left(d_{i}-d_{i-1}\right) \quad \mathrm{km} \tag{148}
\end{equation*}
$$

however, for regularly-spaced path profile data this simplifies to:

$$
\begin{equation*}
d=n \cdot d_{i i} \quad \mathrm{~km} \tag{149}
\end{equation*}
$$

where $d_{i i}$ is the incremental path distance (km).

## $4 \quad$ Path classification

The path must be classified into LoS or transhorizon only for the determination of distances $d_{l t}$ and $d_{l r}$, and elevation angles $\theta_{t}$ and $\theta_{r}$, see below.
The path profile must be used to determine whether the path is LoS or transhorizon based on the median effective Earth's radius of $a_{e}$, as given by equation (6a).
A path is trans-horizon if the physical horizon elevation angle as seen by the interfering antenna (relative to the local horizontal) is greater than the angle (again relative to the interferer's local horizontal) subtended by the interfered-with antenna.
The test for the trans-horizon path condition is thus:

$$
\begin{equation*}
\theta_{\max }>\theta_{t d} \quad \operatorname{mrad} \tag{150}
\end{equation*}
$$

where:

$$
\begin{equation*}
\theta_{\max }=\max _{i=1}^{n-1}\left(\theta_{i}\right) \quad \operatorname{mrad} \tag{151}
\end{equation*}
$$

$\theta_{i}$ : elevation angle to the $i$-th terrain point

$$
\begin{equation*}
\theta_{i}=1000 \arctan \left(\frac{h_{i}-h_{t s}}{10^{3} d_{i}}-\frac{d_{i}}{2 a_{e}}\right) \quad \mathrm{mrad} \tag{152}
\end{equation*}
$$

where:
$h_{i}$ : height of the $i$-th terrain point (m) amsl
$h_{t s}$ : interferer antenna height (m) amsl
$d_{i}$ : distance from interferer to the $i$-th terrain element $(\mathrm{km})$.

$$
\begin{equation*}
\theta_{t d}=1000 \arctan \left(\frac{h_{r s}-h_{t s}}{10^{3} d}-\frac{d}{2 a_{e}}\right) \quad \operatorname{mrad} \tag{153}
\end{equation*}
$$

where:
$h_{r s}$ : interfered-with antenna height (m) amsl
$d$ : total great-circle path distance ( km )
$a_{e}$ : median effective Earth's radius appropriate to the path (equation (6a)).

## 5 Derivation of parameters from the path profile

### 5.1 Trans-horizon paths and LoS paths

The parameters to be derived from the path profile are those contained in Table 7.

### 5.1.1 Interfering antenna horizon elevation angle, $\boldsymbol{\theta}_{t}$

The interfering antenna's horizon elevation angle is the maximum antenna horizon elevation angle when equation (151) is applied to the $n-1$ terrain profile heights.

$$
\begin{equation*}
\theta_{t}=\max \left(\theta_{\max }, \theta_{t d}\right) \quad \operatorname{mrad} \tag{154}
\end{equation*}
$$

with $\theta_{\max }$ as determined in equation (151). Thus, for a LoS path the interfering antenna's horizon elevation angle is considered to be the elevation angle of the line to the interfered-with antenna.

### 5.1.2 Interfering antenna horizon distance, $\boldsymbol{d}_{l t}$

The horizon distance is the minimum distance from the transmitter at which the maximum antenna horizon elevation angle is calculated from equation (151).

$$
\begin{equation*}
d_{l t}=d_{i} \quad \mathrm{~km} \quad \text { for } \max \left(\theta_{i}\right) \tag{155}
\end{equation*}
$$

For a LoS path, the index $i$ should be the value which gives the maximum diffraction parameter $v$ :

$$
\begin{equation*}
v_{\max }=\max \left\{\left[h_{i}+500 C_{e} d_{i}\left(d-d_{i}\right)-\frac{h_{t s}\left(d-d_{i}\right)+h_{r s} d_{i}}{d}\right] \sqrt{\frac{0.002 d}{\lambda d_{i}\left(d-d_{i}\right)}}\right\} \tag{155a}
\end{equation*}
$$

where the profile index $i$ takes values from 1 to $n-1$, and $C_{e}$ is effective Earth curvature as defined in § 4.2.1 of Annex 1.

### 5.1.3 Interfered-with antenna horizon elevation angle, $\boldsymbol{\theta}_{r}$

The receive antenna horizon elevation angle is the maximum antenna horizon elevation angle when equation (151) is applied to the $n-1$ terrain profile heights.
For a $\operatorname{LoS}$ path, $\theta_{r}$ is given by:

$$
\begin{equation*}
\theta_{r}=1000 \arctan \left(\frac{h_{t s}-h_{r s}}{10^{3} d}-\frac{d}{2 a_{e}}\right) \quad \operatorname{mrad} \tag{156a}
\end{equation*}
$$

Otherwise, $\theta_{r}$ is given by:

$$
\begin{gather*}
\theta_{r}=\max _{j=1}^{n-1}\left(\theta_{j}\right) \quad \operatorname{mrad}  \tag{156b}\\
\theta_{j}=1000 \arctan \left(\frac{h_{j}-h_{r s}}{10^{3}\left(d-d_{j}\right)}-\frac{\left(d-d_{j}\right)}{2 a_{e}}\right) \quad \mathrm{mrad} \tag{157}
\end{gather*}
$$

### 5.1.4 Interfered-with antenna horizon distance, $\boldsymbol{d}_{l r}$

The horizon distance is the minimum distance from the receiver at which the maximum antenna horizon elevation angle is calculated from equation (156b).

$$
\begin{equation*}
d_{l r}=d-d_{j} \quad \text { km } \quad \text { for } \max \left(\theta_{j}\right) \tag{158}
\end{equation*}
$$

For a LoS path, $d_{l r}$ is given by:

$$
\begin{equation*}
d_{l r}=d-d_{l t} \quad \mathrm{~km} \tag{158a}
\end{equation*}
$$

### 5.1.5 Angular distance $\boldsymbol{\theta}$ (mrad)

$$
\begin{equation*}
\theta=\frac{10^{3} d}{a_{e}}+\theta_{t}+\theta_{r} \quad \mathrm{mrad} \tag{159}
\end{equation*}
$$

### 5.1.6 "Smooth-Earth" model and effective antenna heights

### 5.1.6.1 General

A "smooth-Earth" surface is derived from the profile to calculate effective antenna heights both for the diffraction model, and for an assessment of path roughness required by the ducting/layerreflection model. The definitions of effective antenna heights differ for these two purposes.

Section 5.1.6.2 describes the derivation of uncorrected smooth-earth surface heights at the transmitter and receiver, $h_{s t}$ and $h_{s r}$ respectively.
Then § 5.1.6.3 describes the derivation of modified smooth-earth heights at the transmitter and receiver for the diffraction model, respectively $h_{s t d}$ and $h_{s r d}$, which in $\S 4.2 .3$ of Annex 1 are used to calculate the effective antenna heights for the diffraction model.
Section 5.1.6.4 describes the calculation of effective heights $h_{t e}$ and $h_{r e}$ and the terrain roughness parameter, $h_{m}$, for the ducting model.

### 5.1.6.2 Deriving the smooth-Earth surface

Derive a straight line approximation to the terrain heights (m) amsl of the form:

$$
\begin{equation*}
h_{s i}=\left[\left(d-d_{i}\right) h_{s t}+d_{i} h_{s r}\right] / d \quad \mathrm{~m} \tag{160}
\end{equation*}
$$

where:
$h_{s i}$ : height (m) amsl, of the least-squares fit surface at distance $d_{i}(\mathrm{~km})$ from the interference source
$h_{s t}$ : height (m) amsl, of the smooth-Earth surface at the path origin, i.e. at the interfering station
$h_{s r}$ : height (m) amsl, of the smooth-Earth surface at the path end, i.e. at the receiver station.
Evaluate $h_{s t}$ and $h_{s r}$ as follows using equations (161)-(164):

$$
\begin{equation*}
v_{1}=\sum_{i=1}^{n}\left(d_{i}-d_{i-1}\right)\left(h_{i}+h_{i-1}\right) \tag{161}
\end{equation*}
$$

where:
$h_{i}$ : real height of the $i$-th terrain point (m) amsl
$d_{i}$ : distance from interferer to the $i$-th terrain element $(\mathrm{km})$.

$$
\begin{equation*}
v_{2}=\sum_{i=1}^{n}\left(d_{i}-d_{i-1}\right)\left[h_{i}\left(2 d_{i}+d_{i-1}\right)+h_{i-1}\left(d_{i}+2 d_{i-1}\right)\right] \tag{162}
\end{equation*}
$$

The height of the smooth-Earth surface at the interfering station, $h_{s t}$, is then given by:

$$
\begin{equation*}
h_{s t}=\left(\frac{2 v_{1} d-v_{2}}{d^{2}}\right) \quad \mathrm{m} \tag{163}
\end{equation*}
$$

and hence the height of the smooth-Earth surface at the interfered-with station, $h_{s r}$, is given by:

$$
\begin{equation*}
h_{s r}=\left(\frac{v_{2}-v_{1} d}{d^{2}}\right) \mathrm{m} \tag{164}
\end{equation*}
$$

### 5.1.6.3 Smooth-earth surface heights for the diffraction model

Find the highest obstruction height above the straight-line path from transmitter to receiver $h_{o b s}$, and the horizon elevation angles $\alpha_{o b t}, \alpha_{o b r}$, all based on flat-earth geometry, according to:

$$
\begin{equation*}
h_{o b s}=\max _{i=1}^{n-1}\left\{H_{i}\right\} \quad \mathrm{m} \tag{165a}
\end{equation*}
$$

$$
\begin{gather*}
\alpha_{o b t}=\max _{i=1}^{n-1}\left\{H_{i} / d_{i}\right\} \quad \operatorname{mrad}  \tag{165b}\\
\alpha_{o b r}=\max _{i=1}^{n-1}\left\{H_{i} /\left(d-d_{i}\right)\right\} \quad \mathrm{mrad} \tag{165c}
\end{gather*}
$$

where:

$$
\begin{equation*}
H_{i}=h_{i}-\left[h_{t s}\left(d-d_{i}\right)+h_{r s} d_{i}\right] / d \quad \mathrm{~m} \tag{165d}
\end{equation*}
$$

Calculate provisional values for the heights of the smooth surface at the transmitter and receiver ends of the path:
If $h_{o b s}$ is less than or equal to zero, then:

$$
\begin{align*}
& h_{s t p}=h_{s t} \quad(\mathrm{~m}) \mathrm{amsl}  \tag{166a}\\
& h_{s r p}=h_{s r} \quad(\mathrm{~m}) \mathrm{amsl} \tag{166b}
\end{align*}
$$

otherwise:

$$
\begin{array}{ll}
h_{s t p}=h_{s t}-h_{o b s} g_{t} & \text { (m) amsl } \\
h_{s r p}=h_{s r}-h_{o b s} g_{r} & \text { (m) amsl } \tag{166d}
\end{array}
$$

where:

$$
\begin{align*}
& g_{t}=\alpha_{o b t} /\left(\alpha_{o b t}+\alpha_{o b r}\right)  \tag{166e}\\
& g_{r}=\alpha_{o b r} /\left(\alpha_{o b t}+\alpha_{o b r}\right) \tag{166f}
\end{align*}
$$

Calculate final values for the heights of the smooth surface at the transmitter and receiver ends of the path as required by the diffraction model:
If $h_{s t p}$ is greater than $h_{0}$ then:

$$
\begin{equation*}
h_{s t d}=h_{0} \quad(\mathrm{~m}) \mathrm{amsl} \tag{167a}
\end{equation*}
$$

otherwise:

$$
\begin{equation*}
h_{s t d}=h_{s t p} \quad(\mathrm{~m}) \mathrm{amsl} \tag{167b}
\end{equation*}
$$

If $h_{s r p}$ is greater than $h_{n}$ then:

$$
\begin{equation*}
h_{s r d}=h_{n} \quad(\mathrm{~m}) \mathrm{amsl} \tag{167c}
\end{equation*}
$$

otherwise:

$$
\begin{equation*}
h_{s r d}=h_{s r p} \quad(\mathrm{~m}) \mathrm{amsl} \tag{167d}
\end{equation*}
$$

### 5.1.6.4 Parameters for the ducting/layer-reflection model

Calculate the smooth-Earth heights at transmitter and receiver as required for the roughness factor given by:

$$
\begin{array}{ll}
h_{s t}=\min \left(h_{s t}, h_{0}\right) & \mathrm{m} \\
h_{s r}=\min \left(h_{s r}, h_{n}\right) &  \tag{168b}\\
\hline
\end{array}
$$

If either or both of $h_{s t}$ or $h_{s r}$ were modified by equation (168a) or (168b) then the slope, $m$, of the smooth-Earth surface must also be corrected:

$$
\begin{equation*}
m=\frac{h_{s r}-h_{s t}}{d} \quad \mathrm{~m} / \mathrm{km} \tag{169}
\end{equation*}
$$

The terminal effective heights for the ducting/layer-reflection model, $h_{t e}$ and $h_{r e}$, are given by:

$$
\begin{array}{ll}
h_{t e}=h_{t g}+h_{0}-h_{s t} & \mathrm{~m}  \tag{170}\\
h_{r e}=h_{r g}+h_{n}-h_{s r} & \mathrm{~m}
\end{array}
$$

The terrain roughness parameter, $h_{m}(\mathrm{~m})$ is the maximum height of the terrain above the smooth-Earth surface in the section of the path between, and including, the horizon points:

$$
\begin{equation*}
h_{m}=\max _{i=i_{l t}}^{i_{l+}}\left[h_{i}-\left(h_{s t}+m \cdot d_{i}\right)\right] \quad \mathrm{m} \tag{171}
\end{equation*}
$$

where:
$i_{l t}$ : index of the profile point at distance $d_{l t}$ from the transmitter
$i_{l r}$ : index of the profile point at distance $d_{l r}$ from the receiver.
The smooth-Earth surface and the terrain roughness parameter $h_{m}$ are illustrated in Fig. 12.

FIGURE 12
An example of the smooth-Earth surface and terrain roughness parameter


## Attachment 3

## to Annex 1

## An approximation to the inverse cumulative normal distribution function for $\boldsymbol{x} \leq 0.5$

The following approximation to the inverse cumulative normal distribution function is valid for $0.000001 \leq x \leq 0.5$ and is in error by a maximum of 0.00054 . It may be used with confidence in the expression for the interpolation function in equation (41b). If $x<0.000001$, which implies $\beta_{0}<0.0001 \%, x$ should be set to 0.000001 . The function $I(x)$ is then given by:

$$
\begin{equation*}
I(x)=\xi(x)-T(x) \tag{172}
\end{equation*}
$$

where:

$$
\begin{gather*}
T(x)=\sqrt{[-2 \ln (x)]}  \tag{172a}\\
\xi(x)=\frac{\left[\left(C_{2} \cdot T(x)+C_{1}\right) \cdot T(x)\right]+C_{0}}{\left[\left(D_{3} \cdot T(x)+D_{2}\right) T(x)+D_{1}\right] T(x)+1}  \tag{172b}\\
C_{0}=2.515516698  \tag{172c}\\
C_{1}=0.802853  \tag{172d}\\
C_{2}=0.010328  \tag{172e}\\
D_{1}=1.432788  \tag{172f}\\
D_{2}=0.189269  \tag{172~g}\\
D_{3}=0.001308 \tag{172h}
\end{gather*}
$$


[^0]:    * Radiocommunication Study Group 3 made editorial amendments to this Recommendation in the year 2022 in accordance with Resolution ITU-R 1.

