International Telecommunication Union

ITU-R
Radiocommunication Sector of ITU

Recommendation ITU-R P.1407-5
(09/2013)

Multipath propagation and parameterization of its characteristics

P Series

Radiowave propagation

International Telecommunication Union

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Note: *This ITU-R Recommendation was approved in English under the procedure detailed in Resolution ITU-R 1.*

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RECOMMENDATION ITU-R P.1407-5*

Multipath propagation and parameterization of its characteristics

(Question ITU-R 203/3)

(1999-2003-2005-2007-2009-2013)

Scope

Recommendation ITU-R P.1407 describes the nature of multipath propagation and defines the appropriate parameters for the statistical description of multipath effects, and provides examples of correlation effects among multiple propagation paths and their computation.

The ITU Radiocommunication Assembly,

considering

a)   the necessity of estimating the effects of multipath on services employing digital systems;

b)   that it is desirable to standardize the terminology and expressions used to characterize multipath,

recommends

1   that, to describe the concepts of multipath in a consistent manner, the terms and definitions given in Annex 1 should be employed;

2   that the correlation concepts of Annex 2 should be used to analyse the effects of multiple-input, multiple-output (MIMO) systems;

3   that for the generation of wideband channel, models in Annex 3 should be used to evaluate the performance of communication systems.

Annex 1

1   Introduction

In radio systems with low antenna heights, there are often multiple indirect paths between the transmitter and receiver due to reflections from surrounding objects, in addition to the direct path when there is line-of-sight. Such multipath propagation is particularly significant in urban environments, where the sides of buildings and paved road surfaces provide strong reflections. As a result, the received signal consists of the summation of several components having various amplitudes, phase angles and directions of arrival.

The resulting spatial variability of signal strength can be viewed as having two regimes:

a)   rapid fading which varies over distances of the order of a wavelength due primarily to changes in phase angles of different signal components;

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*   Radiocommunication Study Group 3 made editorial amendments to this Recommendation in April 2015 in accordance with Resolution ITU-R 1.

b)   slow fading which varies over larger distances due primarily to changes in shadowing loss by surrounding objects.

In addition, the various signal components can be Doppler shifted by different amounts due to the movement of the mobile or of reflecting objects such as vehicles.

The multipath mobile channel can be characterized in terms of its impulse response which varies at a rate dependent on the speed of the mobile and/or the scatterers. Therefore, a receiver has to be able to cope with the signal distortion arising from echoes in the channel as well as the rapid changes in the nature of this distortion. Such characteristics of the mobile radio channel are described by the power delay profiles and the Doppler spectra which are obtained from wideband channel sounding measurements.

Signals transmitted to and from moving vehicles in urban or forested environments exhibit extreme variations in amplitude due to multiple scattering. Fades of 30 dB or more below the mean level are common. The instantaneous field strength when measured over distances of a few tens of wavelengths is approximately Rayleigh-distributed. The mean values of these small sector distributions vary widely from area to area, depending on the height, density and distribution of hills, trees, buildings and other structures.

Physically, multipath propagation parameters are multipath number, amplitude, path-length difference (delay), Doppler shift and arrival angle. These parameters can be characterized from a series of complex impulse responses over a short distance or time interval that can be used to estimate the delay-Doppler spread function representing the multipath phenomenon in the three dimensions of excess delay, Doppler frequency and power density. The delay-Doppler spread function defines a linear transversal filter whose output is the sum of multiple delayed, attenuated and Doppler-shifted replicas of the input signal. This formulation is useful for realizing a hardware simulator in the form of a dynamic transversal filter. The delay-Doppler spread function is used to estimate the power delay profile and the Doppler spectrum, which can be related to the coherence time of the channel. Alternatively, the Fourier transform of the time variant complex impulse response results in the time variant complex frequency response whose amplitude vs frequency characteristics define the multipath frequency selectivity, which is related to the correlation bandwidth and whose time variability gives the fading characteristics at a particular frequency.

Definitions of small-sector (or small-scale) channel parameters are given in §§ 2, 3 and 4. Statistics of small-scale parameters are subsequently used to produce cumulative distribution functions (CDFs). The medium-scale CDF covers a particular route of measurement, which is of the order of tens to hundreds of metres. The combined data set from a number of medium-scale routes is considered to be a large-scale or global characterization, which is representative of the surveyed environment, e.g. hilly terrain, urban, suburban, indoor large rooms, corridors, etc.

2   Parameters of delay profiles

2.1   Definitions of power delay profiles

The appropriate parameters for the statistical description of regarding multipath delay time can be computed from any of three types of power delay profiles: the instantaneous power delay profile; short-term power delay profile; or long-term power delay profile, which are either time averages obtained when the receiver is stationary and represent variations in the environment, or spatial averages obtained when the receiver is in motion.

Definitions of power delay profiles are given as shown in Fig. 1.

The instantaneous power delay profile is the power density of the impulse response at one moment at one point.

The short-term (small-scale) power delay profile is obtained by spatially averaging the instantaneous power delay profiles over several tens of wavelengths within the range where the same multipath components are maintained in order to suppress the variation of rapid fading. Alternatively, it can be obtained from the delay-Doppler spread function shown in Fig. 2A by taking the sum of the magnitude squared along the Doppler frequency shift axis, as illustrated in Fig. 2B.
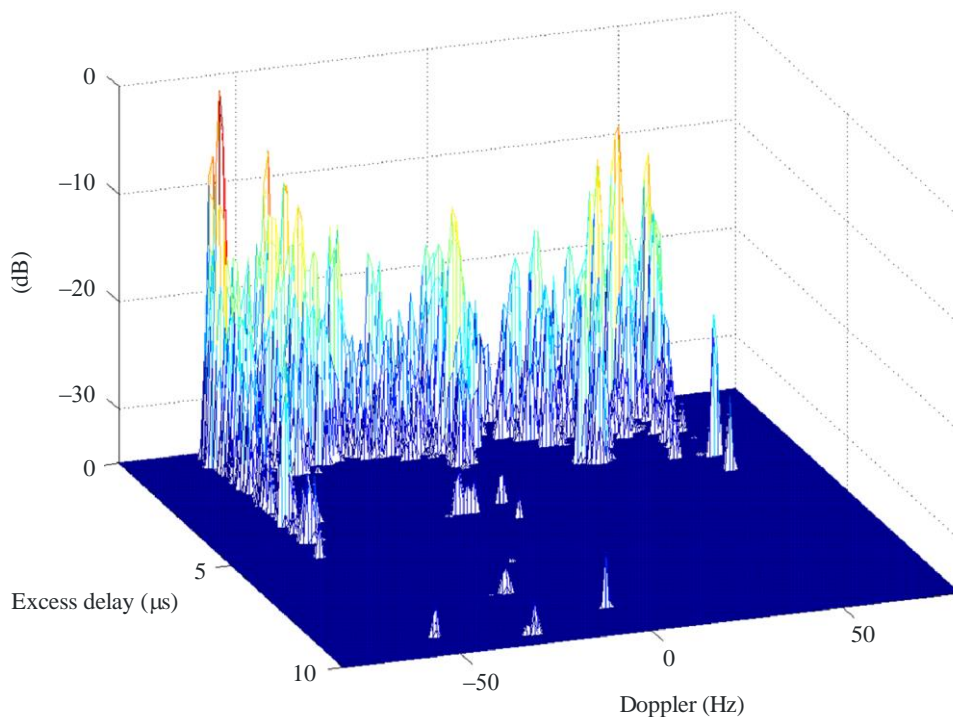
FIGURE 1

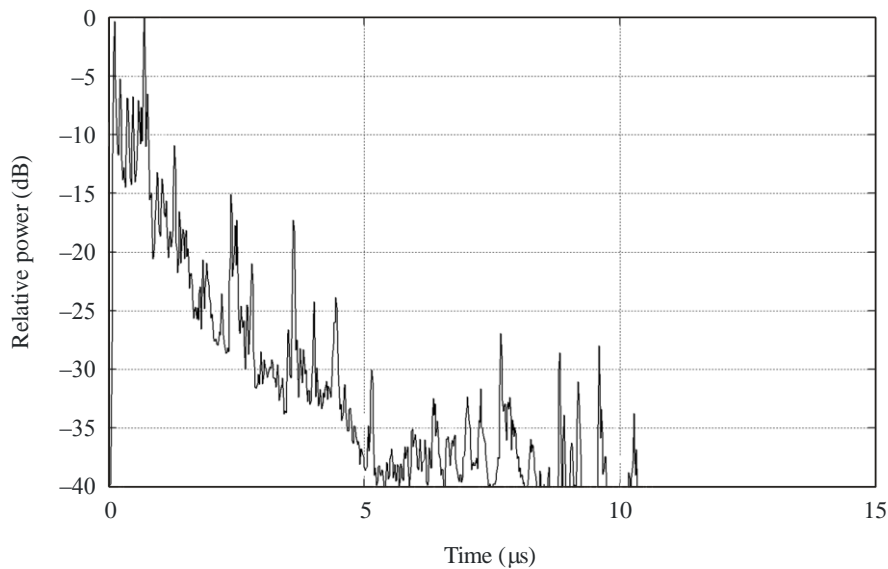**Definition of power delay profiles**
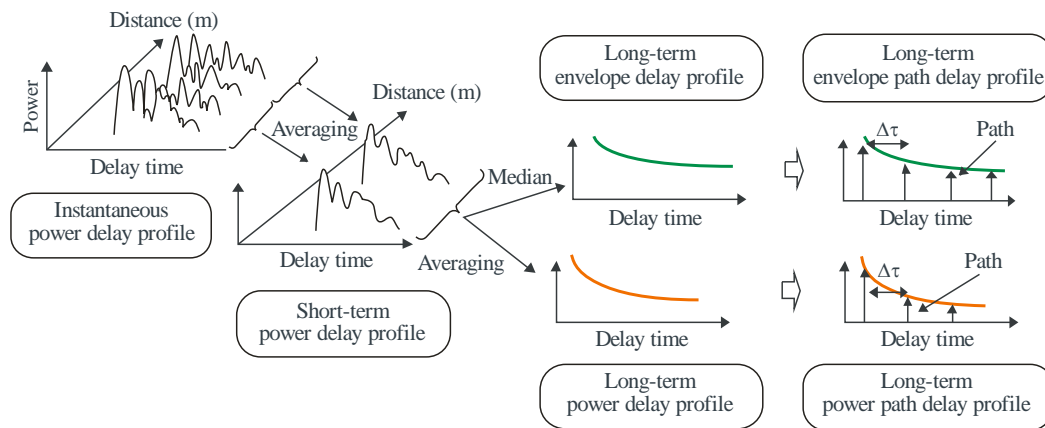
P.1407-01

FIGURE 2A

Delay-Doppler spread function

P.1407-02a

FIGURE 2B

Relative power vs. time response

P.1407-02b

The long-term power delay profile is obtained by spatially averaging the short-term power delay profiles at approximately the same distance from the base station (BS) in order to suppress the variations due to shadowing.

Long-term power delay profiles with a discrete excess delay time normalized by time resolution $1/B$, where B is the bandwidth, are defined as long-term power path delay profiles, instead of continuous power delay profiles.

On the other hand, the long-term envelope delay profile is the median value of the short-term power delay profiles at approximately the same distance from the base station; it expresses the shape of the delay profile at the area considered.

2.2 Definitions of statistical parameters

The appropriate parameters for the statistical description regarding multipath delay time are given below. The *average delay* is the power weighted-average of the excess delays measured and is given by the first moment of the power delay profile (the square of the amplitude of the impulse response).

The *r.m.s. delay spread* is the power weighted standard deviation of the excess delays and is given by the second moment of the power delay profile. It provides a measure of the variability of the mean delay.

The *delay window* is the length of the middle portion of the power delay profile containing a certain percentage (typically 90%) of the total power found in that impulse response.

The *delay interval* is defined as the length of the impulse response between two values of excess delay which mark the first time the amplitude of the impulse response exceeds a given threshold, and the last time it falls below it.

The *number of multipath or signal components* is the number of peaks in a power delay profile whose amplitude are within A dB of the highest peak and above the noise floor.

Definitions of the statistical parameters are given with reference to Figs 3A and 3B. It should be noted that the power delay profiles in the figures are represented in the decibel scale, however, the power summation equations are in linear units of power.

2.2.1 Total power

The *total power*, p_m, of the impulse response is:

$$p_m = \int_{t_0}^{t_3} p(t) \, dt \tag{1}$$

where:

$\qquad p(t):$ power density of the impulse response in linear units of power

$\qquad t:$ delay with respect to a time reference

$\qquad t_0:$ instant when $p(t)$ exceeds the cut-off level for the first time

$\qquad t_3:$ instant when $p(t)$ exceeds the cut-off level for the last time.

2.2.2 Average delay time

The average delay, T_D, is given by the first moment of the power delay profile:

$$T_D = \frac{\int_0^{\tau_e} \tau p(\tau) \, d\tau}{\int_0^{\tau_e} p(\tau) \, d\tau} - \tau_a \tag{2a}$$

where:

$\qquad \tau:$ excess time delay variable and is equal to $t - t_0$

$\qquad \tau_a:$ arrival time of the first received multipath component (first peak in the profile)

$\qquad \tau_e = t_3 - t_0.$

In discrete form with time resolution $\Delta\tau \, (= 1/B)$, equation (2a) becomes:

$$T_D = \frac{\sum_{i=1}^{N} \tau_i p(\tau_i)}{\sum_{i=1}^{N} p(\tau_i)} - \tau_M \tag{2b}$$

$$\tau_i = (i-1)\,\Delta\tau = (i-1)/B \qquad (i = 1, 2, \ldots, N)$$

where $i = 1$ and N are the indices of the first and the last samples of the delay profile above the threshold level, respectively, and M is the index of the first received multipath component (first peak in the profile).

The delays may be determined from the following relationship:

$$t_i(\mu s) = 3.3 r_i \qquad \text{km} \tag{3}$$

where r_i is the sum of the distances from the transmitter to the multipath reflector, and from the reflector to the receiver, or is the total distance from the transmitter to receiver for t_{LOS}.

2.2.3   r.m.s. delay spread

The root mean square (r.m.s.) delay spread, S, is defined by the square root of the second central moment:

$$S = \sqrt{\frac{\int_0^{\tau_e} (\tau - T_D - \tau_a)^2 \, p(\tau) \, d\tau}{\int_0^{\tau_e} p(\tau) \, d\tau}} \tag{4a}$$

In discrete form with time resolution $\Delta\tau$, equation (4a) becomes:

$$S = \sqrt{\frac{\sum_{i=1}^{N} (\tau_i - T_D - \tau_M)^2 \, p(\tau_i)}{\sum_{i=1}^{N} p(\tau_i)}} \tag{4b}$$

2.2.4   Delay window

The delay window, W_q, is the length of the middle portion of the power delay profile containing a certain percentage, q, of the total power:

$$W_q = (t_2 - t_1) \tag{5}$$

whereby the boundaries t_1 and t_2 are defined by:

$$\int_{t_1}^{t_2} p(t) \, dt = \frac{q}{100} \int_{t_0}^{t_3} p(t) \, dt = \frac{q}{100} \, p_m \tag{6}$$

and the power outside of the window is split into two equal parts $\left(\dfrac{100 - q}{200} \right) p_m$.

2.2.5   Delay interval

The delay interval, I_{th}, is defined as the time difference between the instant t_4 when the amplitude of the power delay profile first exceeds a given threshold P_{th}, and the instant t_5 when it falls below that threshold for the last time:

$$I_{th} = (t_5 - t_4) \tag{7}$$

2.2.6   Number of multipath components

The number of multipath or signal components can be represented from the delay profile as the number of peaks whose amplitudes are within A dB of the highest peak and above the noise floor, as shown in Fig. 3B.

2.2.7   Recommended parameters

Delay windows for 50%, 75% and 90% power, delay intervals for thresholds of 9, 12 and 15 dB below the peak are recommended when analysing data. It is worth noting that the effects of noise and spurious signals in the system (from RF to data processing) can be very significant. Therefore, it is important to determine the noise and/or spurious threshold of the systems accurately and to allow a safety margin on top of that. A safety margin of 3 dB is recommended, and in order to ensure the integrity of results, it is recommended that a minimum peak-to-spurious ratio of, for example, 15 dB (excluding the 3 dB safety margin) is used as an acceptance criterion before an

impulse response is included in the statistics. The threshold used for the identification of the number of multipath components depends on the dynamic range of the measuring equipment; a typical value is 20 dB below the peak level of the delay profile.

FIGURE 3A
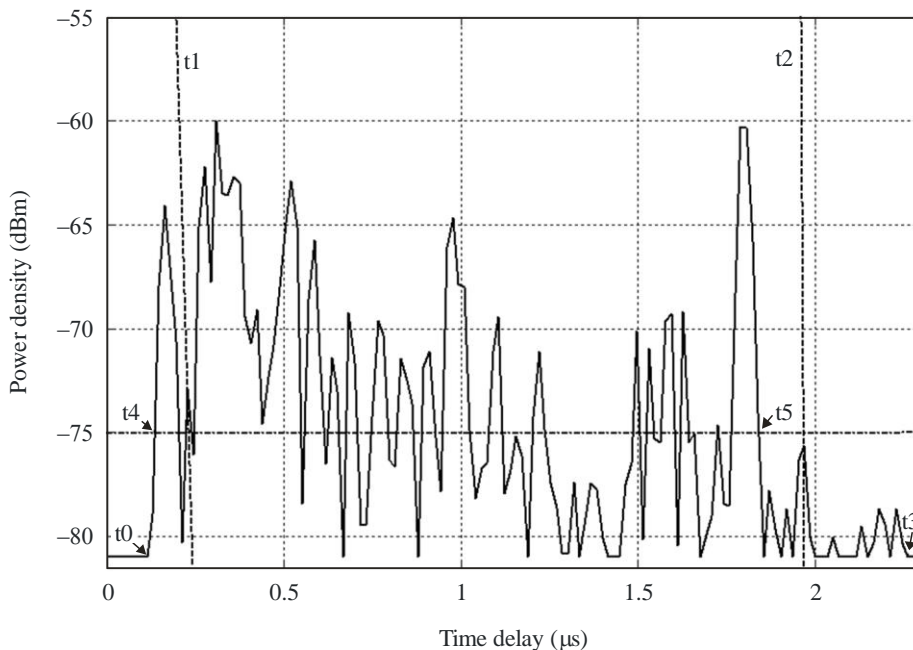
P.1407-03a

Power delay profile illustrating the following parameters: the delay window, W_{90}, containing 90% of the received power is marked between the two vertical dashed lines (t_1 and t_2), the delay interval, I_{15}, containing the signal above the level 15 dB below the peak, lies between t_4 and t_5. t_0 and t_3 indicate the start and the end of the profile above the noise floor.

FIGURE 3B

**Power delay profile indicating multipath components above threshold level**
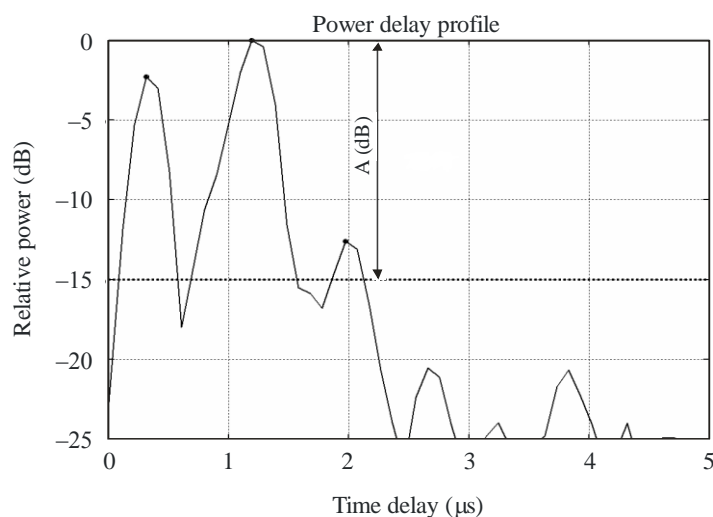
P.1407-03b

3   Parameters of direction of arrival

3.1   Definition of angle of arrival power profiles

The appropriate parameters for the statistical description regarding the angle of arrival of the multipath can be computed from any of three types of angle of arrival power profiles: instantaneous angle of arrival power profile; short-term angle of arrival power profile; or long-term angle of arrival power profile, which are either time averages obtained when the receiver is stationary and represent variations in the environment, or spatial averages obtained when the receiver is in motion.

Definitions of angle of arrival power profiles are given as shown in Fig. 4.

FIGURE 4

Definition of the angle of arrival power profiles
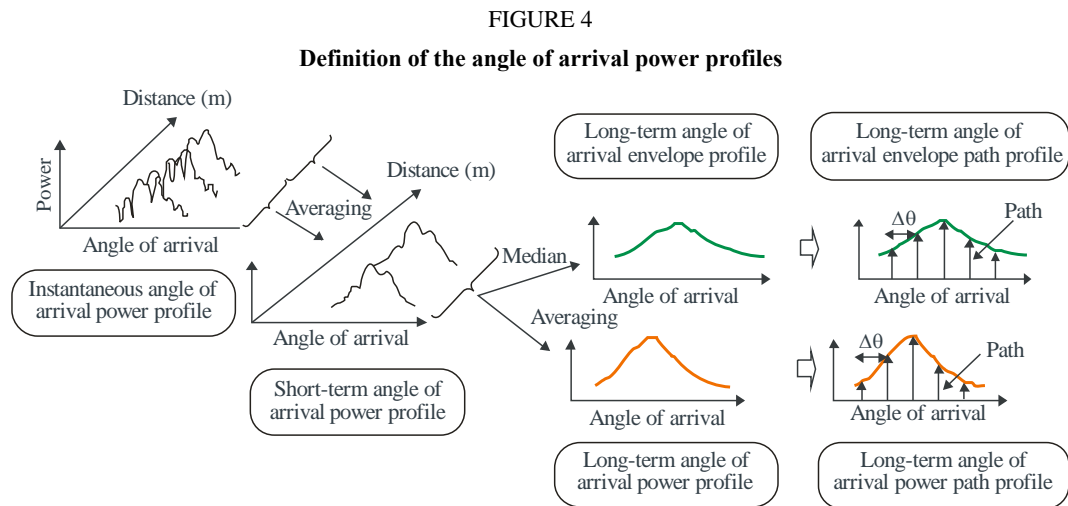
P.1407-04

The instantaneous angle of arrival power profile is the power density of the impulse response at one moment at one point.

The short-term angle of arrival power profile is obtained by spatially averaging the instantaneous angle of arrival power profiles over several tens of wavelengths within the range where the same multipath components are maintained in order to suppress the variations due to rapid fading.

The long-term angle of arrival power profile is obtained by spatially averaging the short-term angle of arrival power profiles at approximately the same distance from the base station (BS) in order to suppress the variation due to shadowing.

Long-term angle of arrival power profiles with a discrete angle normalized by the angular resolution of the antenna are defined as long-term angle of arrival power path profiles, instead of continuous angle of arrival power profiles.

On the other hand, the long-term angle of arrival envelope profile is the median value of the short-term angle of arrival power path profiles at approximately the same distance from the base station, and characterizes the shape of the angle of arrival power profile at the area considered.

3.2   Definitions of statistical parameters

The definitions of the appropriate parameters for the statistical description regarding the multipath angle of arrival are given below:

The *average angle* of arrival is the power-weighted average of the measured directions of arrival and is given by the first moment of the power azimuth spectrum. (It can also be called the power angular profile.)

The angle of arrival *power profile* is the angular power characteristic within the azimuth/horizontal plane.

The *r.m.s. angular spread* is the power-weighted standard deviation of the direction of arrival and is given by the second moment of the power angular profile. It provides a measure of the variability of the mean angle of arrival.

The *angular window* is the width of the middle portion of the angle of arrival power profile containing the defined certain percentage of the total power found in that angle of arrival power profile measurement.

The *angle interval* (or *angular spacing*) is defined as the width of the impulse response (or width of the angular profile) between two values of direction of arrival. It marks the first angle at which the amplitude of the angle of arrival power profile exceeds a given threshold, and the last angle at which it falls below that threshold. The threshold used depends on the dynamic range of the measuring equipment: a typical value is 20 dB below the peak level of the angle of arrival power profile.

3.2.1 Total power

Let the received power in the direction θ be $p(\theta)$.

The *total power*, p_0, of the angle of arrival power profile is defined as the power beyond the threshold level L_0 which is set to separate the signal from noise, as shown in Fig. 5:

$$p_0 = \int_{\theta_0}^{\theta_3} p(\theta)\,d\theta \tag{8a}$$

where:

 θ: measured from the direction of the principal signal (assumed to be stationary within the duration of the measurement) (rad)

  $p(\theta)$: angle of arrival power profile above the threshold level L_0; below L_0, $p(\theta) = 0$

   L_0: level with some margin (3 dB recommended) over the noise floor

   θ_0: angle of arrival when $p(\theta)$ exceeds the threshold level L_0 for the first time in $\theta_{max}(-\pi, \pi)$

   θ_3: angle of arrival when $p(\theta)$ exceeds the threshold level L_0 for the last time in $\theta_{max}(-\pi, \pi)$.

In discrete form equation (8a) becomes:

$$p_0 = \sum_{i=1}^{N} p(\theta_i) \tag{8b}$$

where $i = 1$ and N are the indices of the first and the last samples of the angle of arrival power profile above the threshold level, respectively.

FIGURE 5

Total power
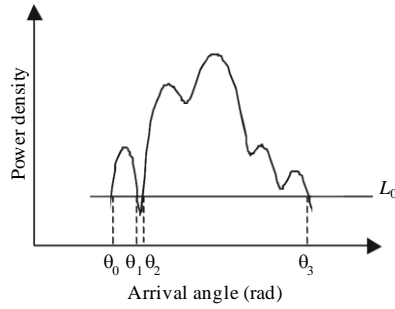
P.1407-05

3.2.2 Average arrival angle

The average angle of arrival, T_A, is given by the first moment of the power angular profile:

$$T_A = \frac{1}{p_0} \int_{\theta_0}^{\theta_3} \theta p(\theta) d\theta \tag{9a}$$

In discrete form with angular resolution $\Delta\theta$, equation (9a) becomes:

$$T_A = \frac{\sum_{i=1}^{N} \theta_i p(\theta_i)}{\sum_{i=1}^{N} p(\theta_i)} \tag{9b}$$

$$\theta_i = (i - 1) \, \Delta\theta \, (i = 1, 2, \dots.N)$$

where $i = 1$ and N are the indices of the first and the last samples of the angle of arrival power profile above the threshold level, respectively.

3.2.3 r.m.s. angular spread

The r.m.s. angular spread S_A of the direction of arrival is defined as follows:

$$S_A = \sqrt{\frac{1}{p_0} \int_{\theta_0}^{\theta_3} (\theta - T_A)^2 p(\theta) d\theta} \tag{10a}$$

In discrete form with angular resolution $\Delta\theta$, equation (10a) becomes:

$$S_A = \sqrt{\frac{\sum_{i=1}^{N} (\theta_i - T_A)^2 p(\theta_i)}{\sum_{i=1}^{N} p(\theta_i)}} \tag{10b}$$

where $i = 1$ and N are the indices of the first and the last samples of the angle of arrival power profile above the threshold level, respectively.

3.2.4 Angular window

The angular window, θ_w, is the width of the middle portion of the angle of arrival power profile containing a percentage q, of the total power as shown in Fig. 6:
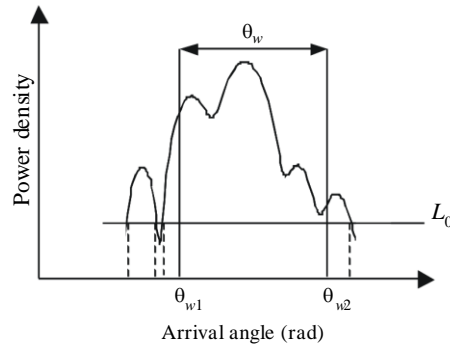
$$\theta_w = \theta_{w2} - \theta_{w1} \tag{11}$$

whereby the boundaries θ_{w1} and θ_{w2} are defined by:

$$\int_{\theta_{w1}}^{\theta_{w2}} p(\theta)\,d\theta = \frac{q}{100} \int_{\theta_0}^{\theta_3} p(\theta)\,d\theta = \frac{q}{100}\,p_0 \tag{12}$$

and the power outside of the window is split into two equal parts $\left(\dfrac{100-q}{200}\right)p_0$.
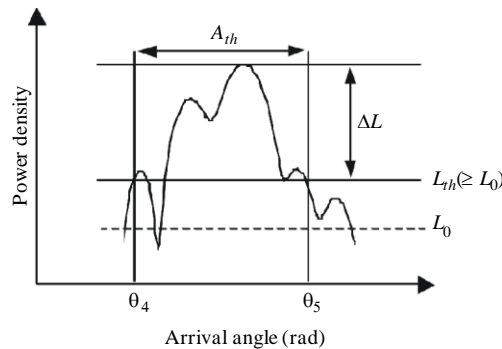
FIGURE 6

Angular window

P.1407-06

3.2.5 Angle interval (angular spacing)

The angle interval A_{th}, is defined as the angle difference between the angle θ_4 when the amplitude of the angle of arrival power profile first exceeds a given threshold L_{th}, and the angle θ_5 when it falls below that threshold for the last time as shown in Fig. 7:

$$A_{th} = \theta_5 - \theta_4 \tag{13}$$

FIGURE 7

Angle interval

P.1407-07

3.2.6 Spatial correlation distance

In particular for multiple-output multiple-input (MIMO) channels, the spatial correlation coefficient for different spacing d is obtained from the angle variant complex transfer function of the power angular profile. The spatial correlation coefficient $R(d)$, is defined as follows:

$$R(d) = \frac{\displaystyle\int_{\theta_0}^{\theta_3} p(\theta)\,\exp(-j2\pi\,d\sin\theta/\lambda)\,d\theta}{\displaystyle\int_{\theta_0}^{\theta_3} p(\theta)\,d\theta} \qquad (14)$$
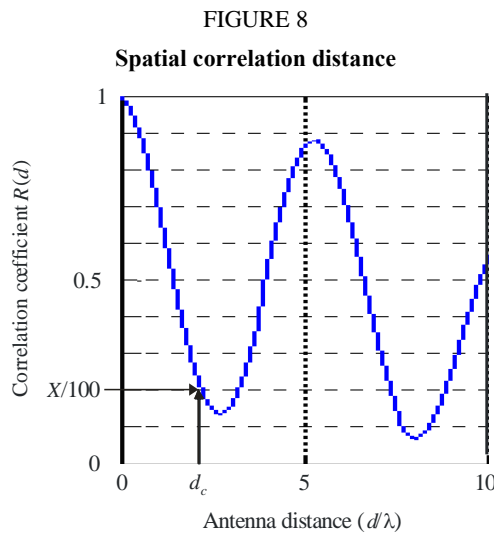
where:

d :   distance for different spacing

λ :   wavelength.

As shown in Fig. 8, the spatial correlation distance d_c is defined as the first-cut off distance at which $|R(d)|$ equals $x\%$ of $|R(d = 0)|$.

$$|R(d_c)|/|R(0)| = x/100 \qquad (15)$$

FIGURE 8

**Spatial correlation distance**

P.1407-08

3.2.7 Recommended parameters

Angular windows for 50%, 75% and 90% power, angle intervals for thresholds of 9, 12 and 15 dB below the peak, and correlation distances for 50% and 90% of correlation are recommended to permit a detailed analysis of data. Furthermore, it is worth noting that the effects of noise and spurious signals in the system (from RF to data processing) can be very significant. Therefore, it is important to determine the noise and/or spurious threshold of the systems accurately and to provide a safety margin on top of that. A safety margin of 3 dB is recommended, and in order to ensure the integrity of results, it is recommended that a minimum peak-to-spurious ratio of, for example, 15 dB (excluding the 3 dB safety margin) be used as an acceptance criterion limiting the angle of arrival power profiles included in the statistics. Figure 9 shows an example of the effect of setting the magnitude of minimum peak-to-L_{th} ratio (ΔL). In this figure, the angle of arrival power profile is assumed to be a Laplace distribution (double exponential distribution) with angular spread of 14°; angular spread and angular interval are calculated as functions of the peak power-to-L_{th} ratio. This figure shows that these parameters undergo significant changes even for essentially identical values. Therefore the value used as ΔL in the statistical evaluation should be specified.

FIGURE 9

Example of effect for minimum peak-to-L_{th} ratio (ΔL)

Laplace distribution (STD of 14°)
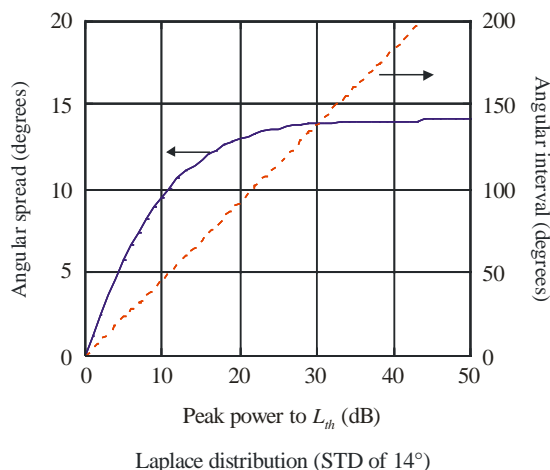
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4 Parameters of the received signal variations

4.1 Definition of the received signal variations as a function of time and frequency

The variations of the received signal in time and in frequency can be measured from: periodically sweeping across the frequency band of interest over a short time interval, or from the Fourier transform of the short-term impulse responses. The resulting small scale time variant frequency response H(f,t) illustrated in Fig. 10 can be used to generate the covariance function of the channel $R_H(f,f';t,t')$ as in equation (16) where E is the expectation:

$$R_H(f,f';t,t') = E\{H(f,t)H*(f',t')\} \tag{16}$$

Under the assumption of wide sense stationary uncorrelated scattering (WSSUS), the covariance function in equation (16) becomes a function of the difference in frequency, Δf, and difference in time, Δt, $R_H(\Delta f, \Delta t)$.

The degree of correlation is expressed by the normalized spaced-frequency spaced-time function, given by equation (17).

$$\rho(\Delta f,\Delta t) \;=\; \frac{R_H(\Delta f,\Delta t)}{\sqrt{E\left[|H(f,t)|^2\right]E\left[|H(f+\Delta f,t+\Delta t)|^2\right]}} \tag{17}$$

Parameters related to the covariance function in equation (16) and H(f,t) are defined in § 4.2.

FIGURE 10

Small scale time variant frequency function
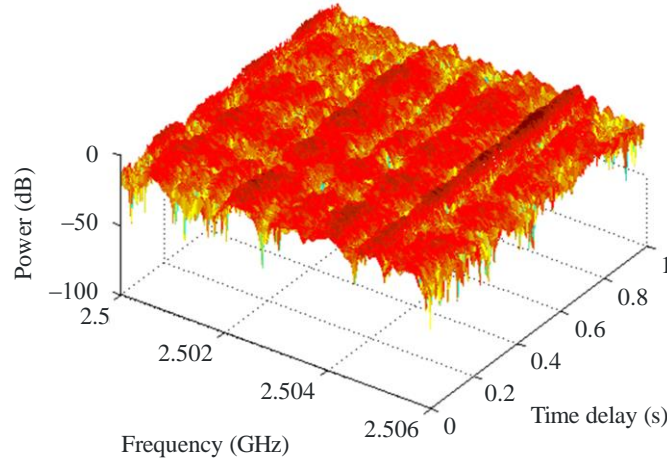
P.1407-10

4.2 Definitions of statistical parameters

4.2.1 Coherent bandwidth or frequency correlation

For WSSUS channels which have a dominant multipath component, the coherent (correlation) bandwidth is obtained from equation (18a). For power delay profiles which exhibit a significant structure of multipath, the coherent bandwidth can be estimated from the Fourier transform $C(f)$ of the power density of the impulse response $p(\tau)$ as in equation (18b):

$$R_H(\Delta f) = R_H(\Delta f, \Delta t)\big|_{\Delta t=0} \tag{18a}$$

$$C(f) = \int_0^{\tau_e} p(\tau)\exp(-j2\pi f\tau)d\tau \tag{18b}$$

The correlation bandwidth, B_x, is defined as the frequency for which $|R_H(\Delta f)|$ or $|C(f)|$ equals x% of $R_H(\Delta f = 0)$ or $C(f = 0)$.

4.2.2 Coherent time or time correlation

For WSSUS, the coherent time is estimated from the time correlation of the channel as in equation (19).

$$R_H(\Delta t) = R_H(\Delta\omega, \Delta t)\big|_{\Delta\omega=0} \tag{19}$$

The coherent time, T_x, is defined as the time interval for which $|R_H(\Delta t)|$ equals x% of $|R_H(\Delta t = 0)|$.

4.2.3 Level crossing rate and average fade duration

The level crossing rate (LCR) and average fade duration (AFD) are obtained from the received signal strength variations at a single frequency as a function of time or distance or from the amplitude of the time variant frequency function at a single frequency measured as a function of time or distance. For a given time interval, the LCR is the number of times the received signal crosses a particular level, whereas the AFD is the duration of time it spends below the specified level. For example for a level of −12.5 dB, Fig. 11 illustrates the LCR and the AFD where the double arrows indicate the time that the signal remains below the level and the vertical arrows indicate the times at which the specified level is crossed in the positive going direction.

FIGURE 11

Received signal strength versus time
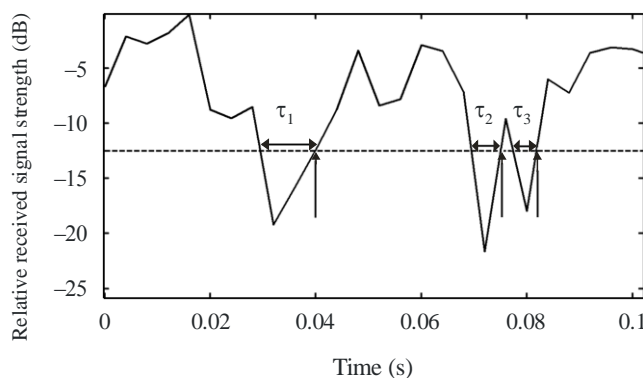
P.1407-11

4.2.4 Level crossing frequency and average fade bandwidth

The level crossing frequency (LCF) and average fade bandwidth (AFBW) are obtained from the received signal strength variations as a function of frequency or from the amplitude of the time variant frequency function at a single instant in time, as in Fig. 11 where the time axis is replaced by the frequency axis. For a given bandwidth, the LCF is the number for which the received signal crosses a particular level and the AFBW is the average frequency range that falls below the specified threshold level. Figure 12 illustrates the two parameters computed for threshold levels between –15 dB to 0 dB.

FIGURE 12

Normalized average fade bandwidth and level crossing frequency
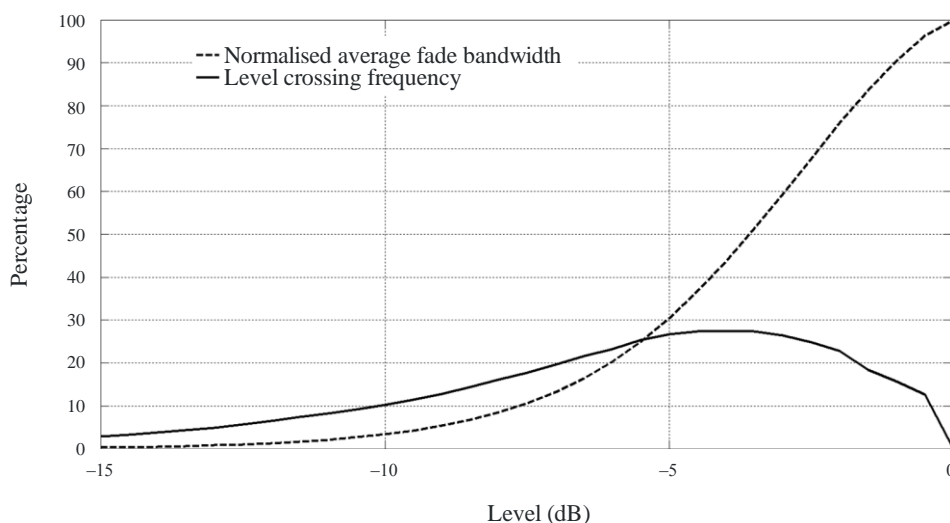
P.1407-12

4.2.5 Recommended parameters

The *correlation bandwidth* is defined as the band of frequencies for which the autocorrelation function of the transfer function is above a given threshold; typical threshold values are 0.5 and 0.9. The LCR is usually estimated for the number of level crossings per second and the LCF is the number of level crossings per MHz.

Annex 2

1   Introduction

This Annex illustrates some results of computing the correlation coefficients from a power angular profile and the effect of the correlation coefficients on MIMO capacity.

2   Computing the spatial correlation coefficients

The definition in equation (14) of Annex 1 has been used to compute the spatial correlation. This Annex briefly introduces a result and illustrates how the correlation is affected by antenna spacing.

Figure 13 shows an ideal truncated Laplacian power-azimuth spectrum (PAS) such as:

$$PAS_L(\varphi) = \sum_{k=1}^{N_c} \frac{Q_{L,k}}{\sigma_{L,k}\sqrt{2}} \exp\left[-\frac{\sqrt{2}|\varphi - \varphi_{0,k}|}{\sigma_{L,k}}\right] \left\{\varepsilon\left[\varphi - (\varphi_{0,k} - \Delta\varphi_k)\right] - \varepsilon\left[\varphi - (\varphi_{0,k} + \Delta\varphi_k)\right]\right\} \quad (20)$$

where $\varepsilon(\varphi)$ is the step function and N_c the number of clusters, $\varphi_{0,k}$ is the mean angle of incidence of k-th cluster, $\sigma_{L,K}$ is the angular spread. PAS is defined over $[\varphi_0 - \Delta\varphi, \varphi_0 + \Delta\varphi]$. The power normalization condition is assumed as:

$$\sum_{k=1}^{N_c} Q_{L,k}\left[1 - \exp\left(-\frac{\sqrt{2}\Delta\varphi_k}{\sigma_{L,k}}\right)\right] = 1 \quad (21)$$

Then the envelope correlation coefficient is given by:

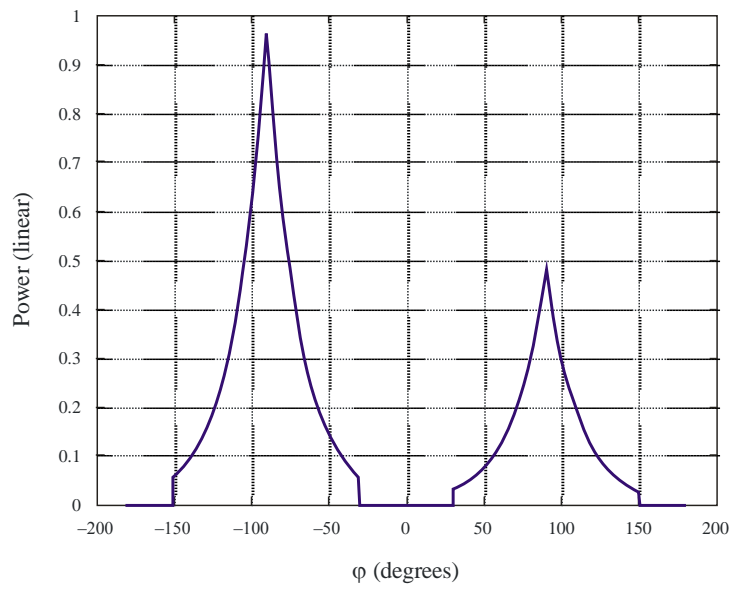$$\rho_e(D) = \left|R_{XX}(D) + jR_{XY}(D)\right|^2 \quad (22)$$

where:

$$D = \quad 2\pi d/\lambda$$

$\quad d$:   antenna spacing

$\quad \lambda$:   wavelength,

and the cross-correlation functions $R_{XX}(D)$ and $R_{XY}(D)$ are defined in equation (15).

FIGURE 13

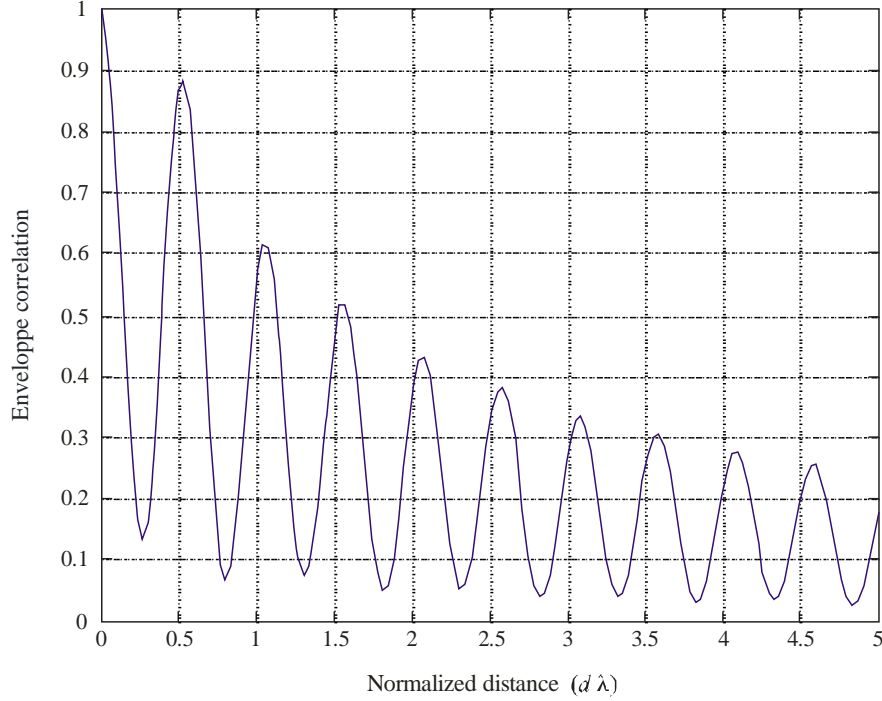**Ideal truncated Laplacian power-azimuth spectrum (PAS)**

P.1407-13

Normalized Laplacian PAS for a two-cluster case. $AS = 30°$, $\varphi_0 \in [-90°, +90°]$.
Additionally, the +90° cluster has half the power of the −90° case.

Figure 14 illustrates the resulting spatial correlation.

FIGURE 14

Resulting spatial correlation

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Envelope correlation coefficient versus the normalized distance = d/λ for the two-cluster case shown in Fig. 13.

3 Effect of the correlation coefficients on MIMO capacity

For Rayleigh fading channels, the ergodic MIMO capacity without channel knowledge at the transmitter is:

$$C = \log_2 \det\left(I_{n_R} + \frac{p}{n_T \sigma^2} R_R^{1/2} H_w R_T H_w^H \left(R_R^{1/2}\right)^H \right) = \log_2 \det\left(I_{n_R} + \frac{p}{n_T \sigma^2} H_w R_T H_w^H R_R^H \right) \qquad (23)$$

where:

n_R and n_T: number of receiver and transmitter antennas, respectively

p: average received power per antenna

σ^2: noise power at each receive antenna

I_{n_R}: $n_R \times n_R$ identity matrix

$(\cdot)^H$ and $\det(\cdot)$: Hermitian and determinant operation, respectively

H_w: matrix whose elements are independent identically-distributed complex Gaussian Random variables with zero mean and unit variance

$(\cdot)^{1/2}$: Hermitian square root of a matrix.

The matrices R_R and R_T determine the spatial correlations between the receivers and the transmitters, respectively, where the channel matrix H is defined by $H = R_R^{1/2} H_w R_T^{1/2}$, $R_R^{1/2}$, and $R_T^{1/2}$ are positive definite Hermitian matrices, and finally they are assumed to be normalized such that $[R_R]_{j,j}$ for $j = 1, K, n_R$ and $[R_T]_{i,i}$ for $i = 1, K, n_T$.

By assuming that R_R and R_T have full rank and $n_R = n_T = n$, then at high S/N (p/σ^2) the capacity can be approximated as:

$$C \approx \log_2 \det\left(\frac{p}{n_T \sigma^2} H_w H_w^H\right) + \log_2 \det(R_R) + \log_2 \det(R_T) \qquad (24)$$

If we denote the eigenvalues of R_R by λ_i, $i = 1, K, n$, then $\sum_{i=1}^{n} \lambda_i = n$. From the arithmetic mean-geometric mean inequality:

$$\prod_{i=1}^{n} \lambda_i \leq 1 \qquad (25)$$

Since $\det(R_R) = \prod_{i=1}^{n} \lambda_i$, it follows that $\log_2 \det(R_R) \leq 0$, and is zero only if all eigenvalues of R_R are equal, i.e. $R_R = I_n$. Thus, the correlation determines the MIMO capacity and the loss in the ergodic capacity at high S/N is given by ($\log_2 \det(R_R) + \log_2 \det(R_T)$) bit/s/Hz.

Figure 15 illustrates the effect of spatial correlations on the ergodic capacity of a MIMO channel with $n_R = n_T = 2$. In the figure $R_T = I_2$, is assumed. The receiver correlation matrix is chosen according to:

$$R_R = \begin{bmatrix} 1 & \rho_R \\ \rho_R^* & 1 \end{bmatrix} \qquad (26)$$

where ρ_R denotes the spatial correlation between the receive antennas.

FIGURE 15

Ergodic capacity with low and high receive correlation


P.1407-15
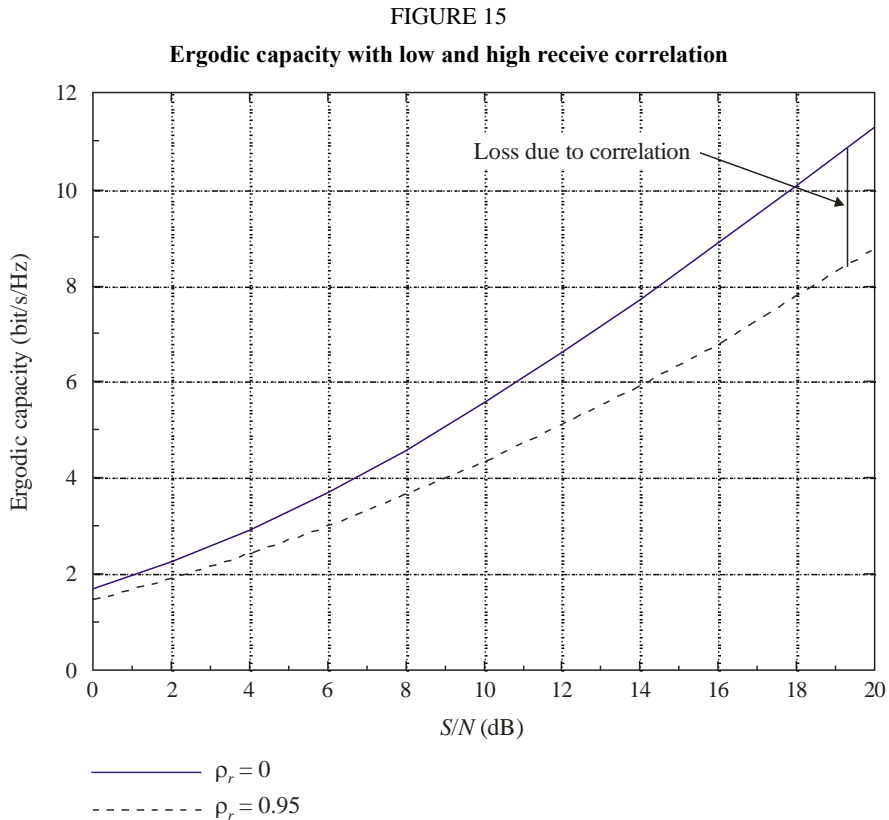
Annex 3

1   Introduction

The resolution of multipath components in measured data depends on the bandwidth of the waveform used in the measurements. The unresolved multipath components give rise to signal variations in time or in space due to the movement of either the transmitter or receiver or changes in the environment as illustrated in Fig. 1. These variations can be modelled by probability density functions such as Rayleigh and Rice as given in Recommendation ITU-R P.1057.

2   Generation of wideband channel

The time variant impulse response can be used to model the channel as a tapped delay line as in Fig. 16A where each tap is delayed by $\Delta\tau$ which corresponds to the time delay resolution of multipath and a tap coefficient which represents the time variations of the unresolved group of multipath components in that time delay interval.

FIGURE 16A

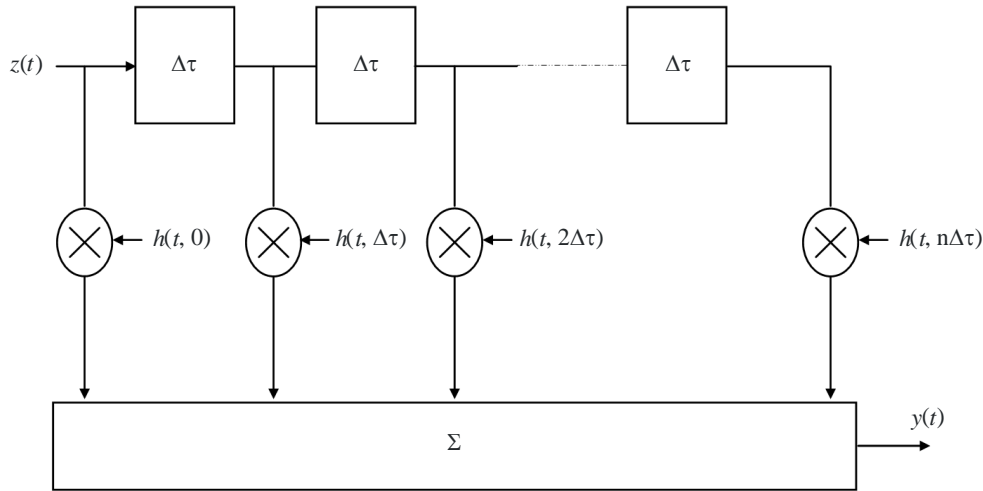**Example of multipaths used to generate the channel**

P.1407-16a
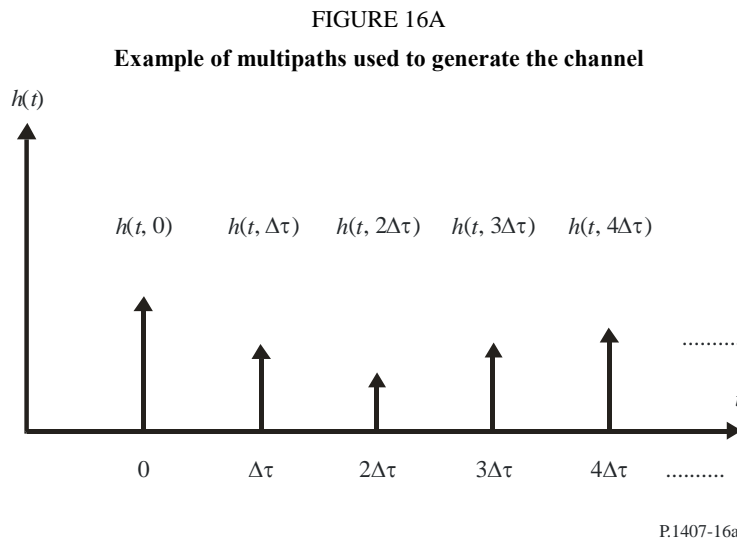
For system simulation, it is sufficient to replace the many scattered paths that may exist in a real channel with only a few $m=n+1$ multipath components in the model as in Fig. 16B. This gives the channel response $h(t)$ in equation (27):

$$h(t) = \sum_{i=0}^{n} h_i \delta(t - i\Delta\tau)$$

(27)

FIGURE 16B

Tapped delay line model of multipath

P.1407-16b

For time delays which have a dominant or line-of-sight (LOS) component, the channel model for each group of multipath components is given by a Rician probability density function. When the Rice factor, K, is equal to zero, the Rayleigh model can be used. The generalized channel model is given in equation (28):

$$h(t) = \sum_{i=0}^{n} \left\{ \sqrt{\frac{K_i p_i}{K_i + 1}} e^{j(2\pi f_{o,i}t + \varphi_{o,i})} + \sqrt{\frac{p_i}{K_i + 1}} g_i(t) \right\} \delta(t - i\Delta\tau) \qquad (28)$$

where:

K_i: Rician K-factor for the ith component defined as the ratio of the power of the dominant or LOS component to the scattered component. When $K_i = 0$, the resulting distribution is Rayleigh

p_i: the averaged power of the ith component in $h(t)$ and is equal to $p_i = E\left[|h_i(t)|^2\right]$

$f_{o,i}$: Doppler frequency of the dominant or LOS component of the ith component in $h(t)$ and is equal to $F_{D\max,i} \cos\theta_{o,i}$ where $f_{D\max,i}$ is the maximum Doppler shift and $\theta_{o,i}$ is the azimuthal angle of arrival

$\varphi_{o,i}$: initial phase of the LOS component of the ith component in $h(t)$

$g_i(t)$: unit power, zero-mean, complex signal representing the diffuse scattering components. For large number of scatters, $g_i(t)$ can be treated as a complex Gaussian random process with unit variance passed through the ith Doppler filter.